Cora Alkinson Sudon Qut.

ELEMENTARY ARITHMETIC

FOR

CANADIAN SCHOOLS,

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REV. BARNARD SMITH, M.A.,

%T PETER'S COLLEGE, CAMBRIDGE,

AND

ARCHIBALD MCMURCHY M.A.

ARCHIBALD McMURCHY, M.A.,
** University College, Toronto.

Authorized by the Minister of Education for use in the Public Schools of Ontario.

TORONTO: WILLIAM WARWICK.

Entered according to Act of Provincial Legislature, in the Year One Thousand Eight Hundred and Sixtyseven, by the Reverend EGERTON RYERSON, LL.D., Chief Superintendent of Education for Ontario, in the Office of the Registrar of the Province of Canada. in this ELEMENTARY ARITHMETIC the same method of treating the subject that was adopted in Mr. Barnard Smith's Arithmetic for Schools has been retained; and especial care has been taken to adapt the book, in every respect, to the wants of the Junior Pupils in the Schools of the Dominion

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ARITHMETIC

SECTION L

- 1. ARITHMETIC teaches us the use of NUMBERS.
- 2. A UNIT or ONE is any single object or thing, as 44 orange, a tree.
- 3. A WHOLE NUMBER, or AN INTEGER, is a UNIT or ONE, or a collection of UNITS or ONES: if a boy, for instance, have one orange, and then another orange is given to him, he will have two oranges; if another be given to him he will have three oranges; if another, he will have four oranges, and so on. One, two, three, four, &c., are called WHOLE NUMBERS OF INTEGERS.
- 4. Notation is the art of writing any number in figures or letters.

There are two methods of Notation: 1st, The Arabic; 2nd, The ROMAN.

5. The Arabic Notation is the method of expressing numbers by means of the following figures, called sometimes digits.

1, 2, 3, 4, 5, 6, 7, 8, 9, called one, two, three, four, five, six, seven, eight, nine, representing (if we express a unit by a dot; thus.),

or one or two or three or four or five or six unit, units, units, units, units, units, units,

-units, units, units, and 0, called nought, because when standing by itself, it was no value, and represents nothing. 0 is sometimes called zero or cupher.

Note. Any one of the figures 1, 2, 3, 4, 5, 6, 7, 8, 9, when standing alone, or as the last figure on the right hand of any number. expresses so many single objects or things, or ones.

..... or nine units are the greatest number of units

which can be expressed by one figure.

If another unit be placed to the right hand of the nine units, we have or ten units, written in figures thus, 10; the 1 in 10 standing in the second place from the right hand, now expresses not one unit, but one ten units.

Hence we see that although 0, when standing by itself, has no value, still when placed to the right hand of any

figure, it alters the value of that figure.

The number next after ten represents or eleven units, written in figures thus, 11, where the 1 in the second place from the right hand expresses ten units, and the 1 in the right-hand place of the number one unit. Thus 11 units equal 1 ten units and 1 unit more.

Next we come to 12 (twelve) or one ten units and 2 more units, 13 (thirteen), 14 (fourteen), 15 (fifteen), 16 (sixteen), 17 (seventeen), 18 (eighteen), 19 (nineteen), which represent 1 ten units, and 3, 4, 5, 6, 7, 8, 9, more units respectively.

Next we come to 20 (twenty), 21 (twenty-one), 22 (twenty-two), 23 (twenty-three), 24 (twenty-four), 25 (twenty-five), 26 (twenty-six), 27 (twenty-seven), 28 (twenty-eight), 29 (twenty-nine); the 2, when followed by 0 or any single figure, representing two tens or twenty units, the figures in the right-hand place of each number expressing so many single units.

Next we come to 30 (thirty), 31 (thirty-one), &c., 3 express ing three tens, or thirty, and so on up to 40 (forty), 4 expressing four tens or forty, to 50 (fifty), to 60 (sixty), to 70 (seventy), to 80 (eighty), to 90 (ninety), 5, 6, 7, 8, 9, expressing five, su, seven, eight, nine tens respectively; the numbers between any two of them as 40 and 50, being formed in the same way as those between 20 and 30.

We thus come at length to 99 ninety-nine) or nine tens and nine, the greatest number which can be expressed by

two figures.

Ex. I.

Write the following numbers in figures.

- (1) Three, four, two, seven, nine, six, eight.
- (2) Ten, one, twelve, nineteen, five, eleven, sixteen.
- (3) Fourteen, twenty, twenty-seven, thirty-three, forty nine, sixty, fifty-five, seventeen, thirty-six.
- (4) Eighty-eight, thirty-five, sixty-three, twenty-nine, seventy six, eighty, ninety-fewe, thirteen, fifty-two.

(5) Write down in figures all the numbers between eight and eighteen, between forty-five and fifty-one, and between eighty-seven and ninety-nine.

The next number after 99 is one hundred, written in figures, thus 100; the 1 in 100, standing in the third place from the right hand, now expressing not one unit, nor one ten units, but one hundred units.

All numbers from 100 to 200 (two hundred) are formed exactly in the same way, as we formed those from 0 to 100; thus we go on 101 (one hundred and one), 102, &c., up to 110 (one hundred and ten), then 111 (one hundred and eleven), 112, &c., up to 120 (one hundred and twenty), then 121 (one hundred and twenty-one), 122, &c., up to 130 (one hundred and thirty), and so on up to 200; then 201, 202, &c., up to 300 (three hundred), and so on up to 400 (four hundred), 500 (five hundred), 600 (six hundred), 700 (seven hundred), 800 (eight hundred), 900 (nine hundred), 999 (nine hundred and ninety-nine), or nine hundreds, nine tens, and nine, the greatest number which can be expressed by three figures.

Ex. II.

Write down the following numbers in figures.

(1) One hundred and six, one hundred and fifty, two hundred, two hundred and eighty-seven, three hundred and ten, four hundred and thirty-one, five hundred and fifty-five, nine hundred and nineteen, eight hundred and sixty-seven.

(2) Write all the numbers in figures from one hundred and ninety-five to two hundred and fourteen, from six hundred and eleven to six hundred and twenty, and from nine hundred and forty-seven to nine hundred and seventy.

The next number after 999 is one thousand, written in figures thus, 1000; the 1 in 1000, standing in the fourth place from the right hand, now expressing one thousand units.

All numbers from 1000 up to 9999 (nine thousand nine hundred and ninety-nine) are formed thus, 1001 (one thousand and one), 1002, &c., up to 2000 (two thousand) up to 3000 (three thousand), and so on.

The next number after 9999 is ten thousand, written in agures thus, 10000; the 1 in 10000, standing in the fifth

place from the right hand, now express ng one ten thousand units.

All numbers from 10000 up to 99999 (ninety-nine thousand nine hundred and nine 'y-nine), are formed thus, 10001 (ten thousand and one), 10002, &c., up to 20000 (twenty thousand), then 20001 (twenty thousand and one), 20002, &c., up to 30000 (thirty thousand), and so on.

Ex. III.

Write the following numbers in figures.

- (1) Four thousand five hundred and eighty-five, seven thousand three hundred and twenty-one, nine thousand seven hundred and ninety-eight, seven thousand and six.
- (2) Five thousand and four, five thousand four hundred, five thousand and forty, eight thousand and thirth-six, eight thousand three hundred and six, eight thousand three hundred and sixty, nine thousand nine hundred and nine.
- (3) Seventy-five thousand six hundred and thirty-five, inety thousand nine hundred and nine, ten thousand and four, eighty-seven thousand and fifty, ninety thousand and one, sixty-four thousand and sixty-four, eighty-three thousand.

The next number after 99999 is one hundred thousand, written in figures thus, 100000, the 1 in 100000 standing in the sixth place from the right hand, now expressing one hundred thousand units, and so on up to 999999 (nine hundred and ninety-nine thousand nine hundred and ninety-nine), then we come to one million, written in figures thus, 1000000, the 1 expressing one million units, and so on up to tens of millions, (10000000), hundreds of millions (100000000), billions (100000000), and so on.

hus	oneis written	. 1
	ten	
	one hundred	
	one thousand	
	ten thousand	
-	one hundred thousand	
- 4	one million	
-9	ten million	
	one hundred million	
	one billion	1,000,000,000
	D 11 1 table that divide	na anti mum.

6. From the above table we see that dividing any num-

ber into periods of three figures each, beginning at the right hand, the names of those periods will be.

First period Units.
Second "Thousands.
Third "Millions.
Fourth "Billions.
Fifth "Trillions.

Also, that the names of the places in each of those periods are the same, namely:

First place, Units.
Second "Tens.
Third "Hundreds.

7. The following plan is recommended to enable the scholar to write in figures any number dictated by the teacher.

Let the scholar write on his slate a number of noughts, or zeros; thus 000,000,000,000, marking them off into periods of three places each from the right:

Put U over the first period for Units.

TsecondThousands.

MthirdMillions.

BfourthBillions.

вмти

and so on. Thus 000,000,000,000. Then when a number is dictated to the pupil, all he has to do is to put each figure ander its proper place and fill up vacancies, if any, with 0's. Thus, two thousand and five will be writ-

Ex. IV.

Write the following numbers in figures.

- (1) One hundred and five, eight thousand seven hundred and ninety, thirty-seven thousand and seventy-one, thirty thousand four hundred and two, seventy-seven thousand seven hundred, twenty-four thousand eight hundred and seventeen.
 - (2) One hundred and five thousand four hundred and

nine, eight millions eight thousand and thirteen, seven millions six hundred and fifty thousand and ninety, sixty-four millions four hundred, eighty-nine millions forty-four thousand and one, five hundred and four millions six hundred and twenty-three thousand and twenty-four, nine hundred millions three hundred thousand eight hundred, fifty-three millions five hundred and three.

(3) Six billions six millions seventy thousand and seven, eighty-three billions four hundred and one millions one thousand and ten, seven billions and four millions eighty-nine thousand two hundred, nine hundred and ninety millions.

3. Numeration is the art of writing in words the meaning any number, which is already given in figures.

This follows from what has been already said; thus

27 means two tens and seven units, or twenty-seven.

503 means five hundreds, no tens, and three units, or five hundred and three.

0610 means no thousands, six hundreds, one ten, and no units, or six hundred and ten.

onits, or six numbered and ten. 5634 means five thousands, six hundreds, three tens, and

four units, or five thousand six hundred and thirty-four.

6,070,084 means six millions, seven tens of thousands, eight tens and four units, or six millions seventy thousand and eighty-four.

803,968,005 means eight hundreds of millions, three millions, nine hundreds of thousands, six tens of thousands, eight thousands, and five units, or eight hundred and three millions

nine hundred and sixty-eight thousand and five.

Ex. V.

Write in words the meaning of

(1) 7, 13, 4, 9, 18, 5, 20, 11, 05, 50, 34, 29, 3, 17, 53.

(2) 19, 8, 041, 88, 27, 72, 94, 49, 16, 61, 98, 80, 56, 28. (3) 107, 170, 017, 430, 691, 080, 800, 008, 956, 803, 684.

(4) 4506, 5870, 5087, 6900, 6009, 02580, 7045, 7591, 6275. (5) 24714, 12500, 10025, 10205, 70457, 74007, 77000.

(6) 300863, 30086630. 96400250, 800400307, 572060495. (7) 120192703, 890647560, 1050060429, 1000000000001.

SIMPLE ADDITION.

9. SIMPLE ADDITION is the method of finding a number,

which is equal to two or more numbers of the same kind taken together.

By the same kind we mean all apples, or all horses, or all

pence, and so on.

The numbers to be added are called ADDENDS. The SUM, or AMOUNT, is the number so found.

Before learning the Rule for Simple Addition, is will be well for a child to learn the following Table, called the ADDITION TABLE. The child should satisfy himself that this Table is true by means of counters, or strokes on a slate.

2 and	3 and	4 and	5 and
1 make 3	l make 4	1 make 5	1 make 6
2 4	2 5	2 . 6	2 7
$\begin{bmatrix} 2 & \dots & 4 \\ 3 & \dots & 5 \end{bmatrix}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3 7	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
4 6	4 7	4 8 5 9	4 9
4 6 5 7 6 8	4 7 5 8 6 9	5 9	5 10
6 8	6 9	6 10	6 11
7 9	7 10	6 10 5 11	7 12
7 9 8 10	7 10 8 11	8 12	8 13
9 13	9 12	9 13	9 14
10 12	10 13	10 14	10 15
10 12	10 13	10 14	10 10
6 and	7 and	and	9 and
l make 7	1 make 8	1 make 9	l make 10
2 8	2 9	2 10	2 11
3 9	3 10	3 11	3 12
4 10	4 11	4 12	4 13
5 11	5 12	5 13	5 14
6 12	6 13	6 14	6 15
7 13	7 . 14	7 15	7 16
8 14	8 15	8 16	8 17
9 15	9 16	9 17	9 18
10 16	10 17	10 18	10 19
10 10	10 17	10 10	10 19

This Table can easily be carried on for numbers larger than 10; for instance since 2 and 1 make 3, 2 and 11 make 10 more than 2 and 1, i. e. make 13. Again since 9 and 4 make 13, 9 and 14 will make 23, and so on, the result in each case being 10 more than in the corresponding case in the Table. Also 2 and 51 make 53, 9 and 54 makes 63, and so on, the result in each case being 50 more than the corresponding result in the Table.

10. The sign +, called Plus, placed between two numbers, means that the numbers are to be added together; thus 2 apples + 3 apples, means that 2 apples and 3 apples are to be added together, therefore 2 apples + 3 apples make 5 apples. Again 2 + 3 + 4 means that 2 and 3 and 4 are to be added together; 2 + 3 make 5, therefore 2 + 3 + 4 make 5 + 4, which make 9.

The sign = called EQUAL, placed between two numbers,

means that the numbers are equal to one another.

The sign . . means THEREFORE.

Ex. 1. Find the sum of, or add together 5 if so, we say 5, 4, and 7. 4 7 and 4 make We add thus, 5 and 4 make 9, 9 and 7 7 11, 11 and 5

make 16; or thus 16 make 16.

.: the sum of 5, 4, and 7, or 5 + 4 + 7 = 16.

Ex. 2. Add together 4, 8, 3, 0, 9.
4 and 8 make 12, 12 and 3 make 15,
15 and 0 make 15, 15 and 9 make 24,
3 12 and 8 make 20,
4 + 8 + 3 + 0 ? 9 = 24;
9 20 and 4 make 24.

or thus 24

Ex. 3. Find the sum of 9, 3, 7, 6, 9 8

Ex. 3. Find the sum of 9, 3, 7, 6, 5, 9, and 8. 3 17 and 5 make 22, 9 and 3 make 12, 12 and 7 make 19, 19 and 6 make 25, 25 and 5 make 30, 30 and 9 make 28, 33 and 8 make 47, sum of 9, 3, 7, 6, 5, 9, and 8 = 47; 38 and 9 make 47, 38 and 9 make 48,

or thus 47

		Ex. VL	
Add (1)	1	(2) 3	(L, 5
. ,	3	7	6
	8	- 8	5
	6	9	7
	_	_	

(4), Find the sum of to o, seven and two; of five, seven and four; of six, three, and nine; of five, five, aud eight; of nine, eight, nought, and six; of six, transand nine; of four, eight and three; of seven, nine and two: of nine, five, three and eight.

- (6). Find the value of 3+4+8+3+2+5; 6+4+0+0+7+3; 5+8+1+6+5+9; 3+6+8+5+4+2; 9+5+7+8+3+4; 6+9+9+8+8+5; 5+8+3+9+9+6+6.
- (6). In a boys' school there are four classes. In the first cass there are six boys; in the second class seven boys; in the third class one more than in the first class; in the fourth class two more than in the second class. How many boys are there in the school?
- (7). John's age is 2 years, Ellen is two years older than John, Walter's age is the sum of the ages of the other two. Find the sum of all their ages.
- (8). A woman sold two chickens to A, to B three more than to A, to C as many as to A and B, to D four more than to B; had C bought as many more chickens as he did buy, the woman would have sold all her chickens; how many chickens had she to sell?

Rule for Simple Addition.

11. Rule. Write down the given numbers under each other, so that units may come under units, tens under tens, hundreds under hundreds, and so on: then draw a line nuder the lowest number.

Find the sum of the column of units: if it be less than ten, write it down under the column of units below the line just drawn, but if it be greater than ten, then write down the units' figure (i.e. the last figure on the right hand) of the sum under the column of units, and carry to the column of tens the remaining figure or figures.

Add the column of tens and the figure or figures you carry as you have added the column of units, and treat its sum in exactly the same way as you have treated the column of units.

Treat each succeeding column (viz. hundreds, thousands, &c.) in the same way.

Write down the full sum of the last column on the left hand.

The entire sum thus obtained will be the sum or amount of the given numbers.

Ex. 1. Add together 35, 56, and 282.

By the Rule.

35 Method of adding. 2 and 6 are \$, 8 and 5 at. 56 13. i.e. I ten and 3 units; write down ? ande: 282

the column of units, and carry 1 ten.

Then I and S are 9, 9 and 5 are 14, 14 and sum = 3733 are 17, i.e. 17 tens, or 10 tens (1 hundred), and 7 tens, write down 7 under the column of tens and carry one hundred.

Then I and 2 are 3. i.e. 3 hundreds, write down a in the

hundreds' place.

Ex. 2. Find the sum of three thousand eight hundred and sixty-seven, seven hundred and nine, fifty-six thousand and thirty, eight thousand eight hundred and ninety-six, and fifteen thousand and twenty-nine, and write down the meaning of the sum in words.

By the Rule,

9 and 6 are 15, 15 and 9 are 24, 24 and 7 3867are 31, or 3 tens and 1 unit: write down 1 709 under the units, and carry 3 tens. 56030 Then 3 and 2 are 5, 5 and 9 are 14, 14 8896 and 3 are 17, 17 and 6 are 23, i.e. 23 tens, 15029 or 2 hundreds and 3 tens; write down 3 84531 tess, and carry 2 hundreds.

Then ? and 8 are 10, 10 and 7 are 17, 17 eighty-four thousand five and 8 are 25, i.e. 25 hundreds, or 2 thoushundred and ands and 5 Fundreds; write down 5 hund-

reds, and carry ? thousands. thirty-one.

Then 2 and 5 are 7, 7 and 8 are 15, 15 and 6 are 21, 21 and 3 are 24, i.e. 24 thousands, or 2 tens of thousands and 4 thousands; write down 4 thousands, and carry 2 tens of thousands.

Then 2 and 1 are 3, 3 and 5 are 8, ie. 8 tens of thousands;

write down 8 tens of thousands.

Note 1. Though the method of adding, as in the above examples, is the one a teacher can follow at first with his oupils; the fellowing method should be insisted on as soon as possible.

Suppose we have to add:

Add thus: 7, 16, 22; put down 2 under the 276 381 units and 2 to be added to the tens, then 2, 8, . .. 7 16, 23, &c., &c.: thus saving much time; instead of saying 7 and 9 make 16, 16 and 7 make 1132 23, &c.

Note 2. The truth of all sums in Addition may be proved by adding the columns first upwards, and afterwards downwards; if the result be the same in both cases, the numbers will probably have been added correctly.

			Ex. VI	I.	•		
	(1)		(3) (4)	(5)	(6)	(7)	
Add	11		33 10	27	33	24	
	12	13	45 8	15	22	56	
	14	34	21 81	53	16	35	
					_		
	(8)		10) (11)		(13)	(14)	
	12		87 98	43	68	78	
	56		6 8 5 5	69	48	66	
	42	94	59 60	74	98	97	
	-			_	_	_	
(15)				(19)	(20)	(21)	
310	342			889	500	682	
46	523	3 45	0 867	803	775	962	
147	876	3 97	9 586	509	89	276	
		-					
(22)	(23)) (24	(25)	(26)	(27)	(28)	
378	797	82	8 654	729	888	674	
423	46	5 93	9 546	909	517	789	
748	289	9 74	7 465	813	743	555	
				_			
(29)	(30)	(31)	(32)	(33) (3	4) (3	35)
2865	785	6769	9479	604	$\dot{5}$ $\dot{5}$ 8	5 3 98	30 6
758	8756	8007	9921	450	0 90		932
7632	3540	5367	6468				580
3403	8559	7689		964			889
		, , , ,					

⁽³⁶⁾ the boy had nineteen marbles, another had seventeen more than the first, and another had nine more than the second, how many marbles had they among them?

(38) 5 apple trees produced as follows: the lst, six hundred and fifty-seven: the 2nd, two hundred and thirty-one

⁽³⁷⁾ In a school section there are two and thirty men, sixty-five more women than men; the number of young men, young women and school children all together equals the number of men and women together, and there are twenty-nine infants; what is the population of the school section?

more than the 1st; the 3rd, eight hundred and ninety-two; the 4th, eleven more than all the first three; the 5th, as many as all the others. How many apples were there on all the trees?

- (39) A gentleman left his property by will, thus: to his wife, nine thousand and eighty dollars; to each of his two younger sons, five thousand eight hundred and ninety-four dollars; the rest of his property in two equal shares between his three daughters and eldest son; the eldest son's share was fifteen hundred and twenty dollars more than the mother's share; what did the gentleman die worth?
- (40) A grocer bought 4 chests of oranges. In the 1st chest there were five hundred and eighty-nine oranges; in the 2nd, two hundred and fifteen more than in the 1st; in the 3rd, one hundred and ninety-seven more than in the 1st; in the 4th, as many as there were in the 1st and 3rd. How many oranges did he buy?

Ex. VIII.

				EX.	A TIT				
Adı	(1)	22 + 30	+29+6	37		(6)	219 + 3	15+612+	70
	(2)	63 + 93	+87 + 7	73		(7)	602 + 5	28 + 346 + 6	648
	(3)	72 + 90	+37 + 3	57 + 39		(8)	736 + 9	32 + 712 + 3	836
	(4)	38 + 47	+96+8	33 + 27		(9)	968 + 8	64 + 345 + 9	989
	(5)	78 + 89	+68+	58 + 47		(10)	940 + 7	60 + 712 + 3	562
	(11)		(12)		(13)		(14)	(15)	
	71407	7	82079	9	6748		33456	1516]
	9078	l	88099	2	5003		84771	809	s
	68943	3	67005	8	4067		66854	95	8
	32600)	74387	9	5674		72984	4979	0
	7277	7	12345	9	8765		99999	7836	8
	0	6)		7)		(18)		(19)	_
		349 5		0821		275910		76840	n
		5478		0146		57680		9532008	
		9099		4889		39039		694	
		3607		7400		5964		8498275	
		2929		3709	,	785348		70089	
		3210		4793		198276		7856341	-
			.,,,						_

(20) Add together nine hundred and twelve, two thousand and fifty-eight, three thousand four hundred and forty-five, nineteen thousand three hundred and sixty, twenty-seven thousand six hundred and forty-three, thirty-nine

thousand seven hundred and ninety, fifty-five thousand eight hundred and seventy-nine, sixty-four thousand nine hundred and seventy-seven, eight thousand two hundred and eleven.

- (21) In the census of 1861, the population of the counties on Lake Huron, was as follows: Of Lambton, twenty-four thousand nine hundred and sixteen; of Huron, fifty-one thousand nine hundred and fifty-four; of Bruce, twenty-seven thousand four hundred and ninety-nine; of Grey, thirty-seven thousand seven hundred and fifty; of Simcoe, forty-four thousand seven hundred and twenty. What was the whole population of the above five counties in 1861?
- (22) In 1861 the population of the counties on the Ottawa river, was: of Prescott, fifteen thousand four hundred and ninety-nine; of Russell, six thousand eight hundred and twenty four; of Carlton, twenty-nine thousand six hundred and twenty; of Renfrew, twenty thousand three hundred and twenty-five. What was the total population of these four counties in 1861?
- (23) In 1861 Toronto contained forty-foor thousand eight hundred and twenty-one inhabitants; Montreal, ninety thousand three hundred and twenty-three; Hamilton, nineteen thousand and ninety-six; Ottawa, fourteen thousand six hundred and sixty-nine; Kingston, thirteen thousand seven hundred and forty-three; London, eleven thousand five hundred and fifty-five. Find the total population of these cities in 1861?

	Ex. IX.		
the sum of	(1)	(2)	(3)
	20712	2012	22793
	212907	75005	27812
	616848	700764	38614
	703003	93869	45693
	1090090	4202573	92075
	-		
(4)	(5)		(6,
278653	2612856	3	761390€
972009	8906783	2	73056 38
2673627	912227	20	9617382
5009607	6804398	37	2637867
27693	27635398	96	836335 2
9 8673 5	33297653	2	7306468
	(4) 278653 972003 2673627 5009607 27693	the sum of (1) 20712 212907 616848 703003 1090090 (4) (5) 278653 2612856 972009 8906783 2673627 912227 5009607 6804398 27693 27635398	the sum of (1) (2) 20712 2012 212907 75005 616848 700764 703003 93869 1090090 4202573 (4) (5) 278653 2612856 3 972009 8906783 2 2673627 912227 20 5009607 6804398 37 27693 27635398 96

(7)	(8)	(9)
276608567	3 06738672	397 203685
76293568	68345658	28678326
683927285	9 28327368	206738638
938668589	9283678	728397328
211839297	238906594	563435639
26302562	93567836	912368834
397612397	207867398	6383563
583967323	30673612	83297609
960039368	928327563	603536239
543832586	568302126	736397564
782395678	202386517	932506593
(10)	(11)	(12)
72867853	368936709	378684976
97605812	763856 73	79683886
7638516	46730875 3	468976395
316527308	900009900	786347512
275607836	90909999	927607038
97673904	938568378	90809008
268937318	712050750	758385006
718768926	77807689	703209600
203685738	234593368	87967339
96359568	99213567	862006764
397569387	837346395	993387535

(13) Add together nine millions four hundred and sixty-six thousand four hundred and ninety-five, three hundred and seventy-five millions five hundred and seventy-three thousand seven hundred and thirty-five, seven hundred and fifty-four thousand five hundred and forty-seven, three millions seven hundred and eighty nine thousand two hundred and eighty-four, twenty-nine millions eight hundred and eighty-six thousand seven hundred and ninety-nine, nine hundred and ninety-two thousand and eighty-four, two hundred and ninety-three thousand six hundred and ninety-five, two millions six hundred and eighty-four thousand four hundred and eighty-seven, three millions five hundred and ninety-two thousand eight hundred and seventy-three, seven millions eight hundred and forty-nine thousand three hundred and forty-six.

(14) A farmer had forty-four sheep, thirty-five head of cattle, fifteen pigs, six horses. How many animals had he altogether?

- (15) In one year a farmer's crop was as follows: Five hundred and twenty-three bushels of wheat, a hundred and twenty bushels of oats, sixty-four bushels of peas, two hundred and thirty-seven bushels of potatoes, thirty-eight bushels of turnips. How many bushels had he?
- (16) A man bought a farm for sixteen mandered and fifty dollars, he spent a hundred and sixty in putting on it new fences, five hundred and seventy-five in building a new house, in repairing the barn and sheds two hundred; he then sold it and made a profit of six hundred dollars. How much did he get for the farm?
- (17) In 1861 the population of the counties on Lake Erie was: Essex, twenty-five thousand two hundred and eleven; Elgin, thirty-two thousand and fifty; Kent, thirty-one thousand one hundred and eighty-three; Norfolk, twenty-eight thousand five hundred and ninety; Haldimand, twenty-three thousand seven hundred and eighty; Welland, twenty-four thousand nine hundred and eighty-eight. What was the total population of the six counties on Lake Erie.

SIMPLE SUBTRACTION.

12. SIMPLE SUBTRACTION is the method of finding what number remains, when a smaller number is taken from a greater number of the same kind.

The number so found is called the REMAINDER, or DIF-

FERENCE.

The number subtracted from, is called the Minuend; the number subtracted, the Subtrahend.

13. The sign—called MNUs, placed between two numbers, means that the second number is to be subtracted from the first number: thus 7—3, or 7 minus 3 means that 3 is to be subtracted from 7...7—3 = 4.

Rule for Simple Subtraction.

14. RULE. Write down the less number under the greater number, so that units may come under units, tens un der tens, hundreds under hundreds, and so on; then draw a straight line under the lower number.

Take, if you can, the number of units in each figure of the lower number from the number of units in each figure of the upper number which stands directly over it, and place the remainder under the line just drawn, units under units, tens under tens, and so on.

But, if the units in any figure in the lower number be

greater than the number of unres in the figure just above it, then add ten to the upper figure, and then subtract the number of units in the lower tigure from the number in the upper figure thus increased, and write down the remainder as ociore.

Add one to the next number in the lower number, and then take this figure thus increased from the figure just above it, by one of the methods already explained.

Go on thus with all the figures.

The whole difference, or remainder, so written down, will be the difference or remainder of the given numbers.

Ex. l. Subtract 547 from 859.

By the Rule,

859 Method. 7 from 9 leave 2, 1. cunits from 9 547 units leave 2 units; write down 2 in the units

diff. = 312 place. 4 from 5 leave 1; i.e. 4 ters from 5 tens leave 1 ten; write down 1 in the tens' place.

5 from 8 leave 3, i.e. 5 hundreds from 3 hundreds leave 3 hundreds; write down 3 in the hundreds' place.

Ex. 2. Find the difference between seven hundred and forty-two and two hundred and sixty-eight.

By the Rule,

742 I cannot take 8 from 2, i.e. 8 units from 2 268 units, : I add 10 to 2, which makes 12, 8 from

diff. = 474 12 leave 4; write 4 in the units' place.

must .. add 10 to the lower number 268 (so as not to alter the difference between 742 and 268), i.e. 268 must be made 278, or 1 must be added to the 6.

Then I cannot take 7 from 4, i.e. 7 tens from 4 tens, . . 1 add 10 to the 4, really 10 tens or 1 hundred to the 4 tens, which makes it 14, really 14 tens, then 7 from 14 leave 7,

really 7 tens: write 7 in the tens' place.

I have just added 10 tens, or 1 hundred to the upper number, I must ... add 1 hundred to the lower number, i.e. 1 must add 1 to the 2, really 1 hundred to 2 hundreds, making it 3, really 3 nundreds, then 3 from 7 leave 4, really 4 hundreds; write 4 in the hundreds' place.

Ex. 3. How much greater is eight thousand two nundred

than six thousand three hundred and nine?

8200 9 from 0 I cannot, then 9 from 10 leave 1; 6309 write 1 in the units' place; carry 1, really 1 ten, then 1 from 0 I cannot, then 1 from 10 leave 9, really 1 ten from 10 tens leaves 9 tens write 9 in the tens' place; carry 1, really 1 hundred, tnen 4 from 2 I (cannot, then 4 from 12 leave 8, really 4 hundreds from 12 hundreds leave 8 hundreds; write 8 in the hundreds' place, carry 1, really 1 thousand, then 7 from 8 leave 1, really 7 thousands from 8 thousands leave 1 thousand; write 1 in the thousands' place.

Note, The truth of all sums in subtraction may be proved by adding the less number to the difference or remainder; if this sum equals the larger number, the sum will probably have been worked correctly.

Thus, Proof of Ex. 3. Less number + vemainder = 6309 + 1891 = 8200, the greater number.

		Ex. X.								
From Take	(i) 18 14	(2) 27 15	(3) 39 11	(4) 55 5	(5) 86 60	(6) 568 22	(7) 759 603			
	(8)	(9)	(10)	(11)	(12)	(13)	(14)			
	24	51	64	83	98	70	64			
	18	49	6	47	89	54	29			
	75)	(16)	(17)	(18)	(19)	(20)	(21)			
	200	547	896	702	800	650	912			
	16	380	708	504	199	56	707			
	22)	(23)	(24)	(25)	(26)	(27)	(28)			
	563	209	608	486	843	900	505			
	476	+20	499	307	745	791	107			

- (29) Subtract thirty-seven from fifty, twenty-nine from seventy-one, sixty-six from one hundred and tour; ninety-seven from two hundred and eleven, one hundred and five from three hundred and three, four hundred and seventy-five from six hundred and forty one
- (30) A gentleman bought a horse and a carriage for five hundred and sixty dollars, the horse was valued at three hundred dollars. How much was the carriage worth? and how much was the horse worth more than the carriage?
- (31) In a school there are 75 children, there are 28 girls. How many more boys than girls are there?
 - (32) Charles had 167 marhles, he gave John 49, James 65,

Thomas all the rest but 19; how many marbles had Thomas less than James?

- (33) By how much does the sum of 6 and 4 exceed their difference?
- (34) A boy's father gave him 40 cents to pay 10 cents for a slate, 3 cents for pencils, 8 cents for a copy-book, 5 cents for ink, 3 cents for a postage stamp; after paying for the above he lost all but 4 cents through a hole in his pocket; how much did he lose?

			Ex. XI	•		
From Take	(1) 5467 3546	(2) 7601 3890	(3) 300 200	0	(4) 453 6 2297	(5) 5480 996
	(6) 7009 5080	(7) 8052 4847	(8) 5281 597	(9) 7210 3809	(10) 8888 999	5600
	(12) 14748 13942	(13) 54832 29648	(14) 80408 59385	70	15) 0007 9999	(16) 43520 25347
	(17) 44 56 73 27 7594	9200 560		(19) 8712539 6805009		(20) 550030042 94090096

- (21) What number taken from three thousand will leave one hundred and one? What number added to seventytwo thousand five hundred and seventy-six will make one million seventy thousand four hundred and nine.
- (22) The sum of three numbers is twenty-three thousand two hundred and fifty-seven; the first is 3277, and the second is twelve hundred and eighty-three less than the first; find the third number.
- (23) What is the difference between 23047 + 175 368 + 495 132 and 10000 8406 704 + 7305?
- (24) When will the Prince of Wales, who was born in the year 1841, be as old as the Queen now, in the year 1869, s, who was born in the year 1819? How old will the Queen hen be?
 - (25) John says to Henry, I have 97 marbles: Henry re-

plies, I have 29 less than you: Charlie adds, I have as many as both of you, less 25. How many marbles had Henry, and how many had Charlie?

- (26) A man whose yearly income is 1000 dollars, spends 84 dollars for house rent, 135 dollars for servants, 39 dollars in travelling, 58 dollars in clothing, as much on his garden as in travelling and clothing, 804 dollars in household bills. Will he have saved anything, or be in debt at the end of the year, and to what amount?
- (27) Harry goes up sixteen steps of a ladder, which has 45 steps, then down 7 steps, then up 10, then down 2, then down 4, then up 11, then down 9, then up 7, then up 5, then down 8, what step from top and bottom will he then be standing upon?
- (28) In a union workhouse there are 133 inmates. The number is made up thus: infirm and able-bodied 70; able-bodied and children 105; children and officers 63; officers 5. Find the number of each class.
- (29) A basket contained oranges, nuts, and eggs; in all 1769; there were 1696 oranges and nuts, and 1262 nuts and eggs. How many more nuts were there than oranges?
 - (30) The population of the counties on the river St. Lawrence in 1861, was one hundred and seventeen thousand nine hundred and eighty-six, that of those on the Ottawa river was seventy-two thousand two hundred and sixty-eight. Find the difference between the population of these counties?
 - (31) What is the difference between thirty-seven millions nine hundred and six thousand seven hundred and three, and forty-five millions three thousand and eight?
 - (32) The subtrahend is fifty-six millions two hundred and twelve thousand three hundred, the remainder seventy-seven thousand three hundred and thirteen. What is the minuend?
 - (33) The minuend is sixty-six millions three hundred and four thousand, the difference twelve thousand five hundred and eighty-six. Find the subtrahend.
 - (34) A man bought 305 sheep for 3 dollars a head, and after spending 45 dollars on them for food, so them for 4 dollars a head; how many dollars did he gair by his bargain?
 - (35) For the year 1861 the Imports into Canada were forty-three millions fifty-four thousand eight hundred and thirty-six dollars, and the Exports were thirty-four millions

seven hundred and seventeen thousand two hundred and forty-eight dollars. Find by how much the Imports exceeded the Exports for the year 1861.

15. ROMAN NOTATION. I, denotes one; V, five; X, ten; L, fifty; C, one hundred; D, five hundred; M, one thousand.

RULE. Where any one of the above letters is after, or to the right hand of, one of equal or greater value, it is to be added to it, but when put before one of greater value, it is to be subtracted from it.

Thus II = 1 + 1 = 2, III = 1 + 1 + 1 = 3, IV = 5 less 1 = 4, VI = 5 + 1 = 6, VIII = 5 + 1 + 1 + 1 = 8, IX = 10 less 1 = 9, XIII = 10 + 1 + 1 + 1 = 13, XIV = 10 plus 5 less 1 = 10 + 4 = 14, LXXIX = 50 + 10 + 10 + 10 less 1 = 70 + 9 = 79, XC = 100 less 10 = 90.

Note. A line over a letter or letters, increases their value a thousandfold: thus V=5, V=5000; C=100, C=100000.

Ex. XII.

1. Express 1.2 the Roman Notation, three; seven; eleven; nine; twelve; sixteen; 18; 25; 28; 37; 40; 53; 59; 62; 77; 84; 103; 157; 190; 200; 651; 783; 1204; 1527; 1865.

2. Express in words, and also in Arabic figures, III; VI; VIII; XIII; XV; XVII; XX; LIV; LXXXI; CXI. DCV; VII; MC; MM; DCCXLIX; MDCCCLXV.

SIMPLE MULTIPLICATION.

46. SIMPLE MULTIPLICATION is a short method of repeated addition; thus, when 2 is multiplied by 3, the number obtained is the sum of 2 repeated three times, which sum =2+2+2=6.

The number, which is to be repeated or added to itself, is called the MULTIPLICAND: thus, in the above example, 2 is the multiplicand.

The number which shows how often the multiplicand is to be repeated, is called the MULTIPLIES: thus, in the above example, 3 is the multiplier.

The number found by multiplication, for instance 6 in the

above example, is called the PRODUCT.

The multiplier and multiplicand are sometimes called Facrons, because they are factors, or makers, of the product.

The sign x, called into, or multiplied by, placed be-

tween two numbers means that the numbers are to be multiplied together.

The following Table, called the MULTIPLICATION TABLE,

ought to be learned correctly:

Twice	•				•					
2	Twic	e 3	times	4 tin	nes	5 tin	nes 6	times	7 ti	mes
3	l mak	es 2 1 m	akes :	3 l mak	es 4	l mak	es 5 l 1	makes 6	l ma	kes7
4	2	4 2	(6 2	. 8	2 .	. 10 2	12	2 .	. 14
5	3	6 3	9	9 3	. 12	3 .	. 15 3	18	3 .	. 21
6 . 12 6 . 18 6 . 24 6 . 30 6 . 36 6 . 42 7 . 14 7 . 21 7 . 28 7 . 35 7 . 42 7 . 49 8 . 16 8 . 24 8 . 32 8 . 40 8 . 45 8 . 56 9 . 18 9 . 27 9 . 36 9 . 45 9 . 54 9 . 63 10 . 20 10 . 30 10 . 40 10 . 50 10 . 60 10 . 70 11 . 22 11 . 33 11 . 44 11 . 55 11 . 66 11 . 77 12 . 24 12 . 36 12 . 48 12 . 60 12 . 72 12 . 84 8 times	4	8 4	19	2 4	16	4 .	. 20 4	24	4 .	. 28
6	5	10 5	18	5 5	20	5 .	. 25 5	30	5 .	. 35
7	6	12 6	18	6	24	6.				
8		14 7	2	1 7	28	7 .	. 35 7		7 .	49
9 . 18 9 . 27 9 . 36 9 . 45 9 . 54 9 . 63 10 . 20 10 . 30 10 . 40 10 . 50 10 . 60 10 . 70 11 . 22 11 . 33 11 . 44 11 . 55 11 . 66 11 . 77 12 . 24 12 . 36 12 . 48 12 . 60 12 . 72 12 . 84 8 times		16 8	24	1 8						
10		18 9			36	9 .	45 9		9 .	
11 . 22 11 . 33 11 . 44 11 . 55 11 . 66 11 . 77 12 . 84 12 . 60 12 . 72 12 . 84 8 times 9 times 10 times 11 times 12 times 1 makes 8 1 makes 9 1 makes 10 1 makes 11 1 makes 12 1 makes 12 2 . 20 2 . 22 2 . 24 3 . 24 3 . 27 3 . 30 3 . 33 3 . 36 4 . 32 4 . 36 4 . 40 4 . 44 4 . 48 5 . 40 5 . 45 5 . 50 5 . 55 5 . 66 6 . 72 7 . 56 7 . 63 7 . 70 7 . 77 7 . 84 8 . 64 8 . 72 8 . 80 8 . 88 8 . 96 9 . 72 9 . 81 9 . 90 9 . 99 9 . 108 10 . 80 19 . 90 10 . 100 10 . 110 10 . 120 11 . 88 11 . 99 11 . 110 11 . 121 11 . 132	10					10 .				
12 . 24 12 . 36 12 . 48 12 . 60 12 . 72 12 . 84 8 times 9 times 10 times 11 times 12 times 1 makes 8 1 makes 9 1 makes 10 1 makes 11 1 makes 12 2 16 2 18 2 20 2 22 2 22 2 3 24 3 27 3 30 3 33 3 36 3 4 32 4 36 4 40 4 44 4 44 4 5 40 5 45 5 50 5 5 55 5 6 66 72 7 6 48 6 54 6 60 6 66 6 67 7 7 56 7 63 7 70 7 77 77 7 84 8 64 8 72 8 80 8 88 8 96 9 72 9 81 9 90 9 99 9 108 10 80 19 90 10 100 100 110 10 120 11 88 11 99 11 110 11 121 11 132										
8 times 9 times 10 times 11 times 12 times 1 makes 8 1 makes 9 1 makes 10 1 makes 11 1 makes 12 2										
1 makes 8 1 makes 9 1 makes 10 1 makes 11 1 makes 12 2 16 2 18 2 20 2 22 2 24 3 24 3 27 3 30 3 33 3 36 4 32 4 36 4 40 4 44 4 48 5 40 5 45 5 50 5 55 5 60 6 48 6 54 6 60 6 66 6 72 7 56 7 63 7 70 7 77 7 84 8 64 8 72 8 80 8 88 8 96 9 72 9 81 9 90 9 99 9 108 10 80 10 90 10 100 10 110 10 120 11 88 11 99 11 110 11 121 11 132				1					1	. 01
1 makes 8 1 makes 9 1 makes 10 1 makes 11 1 makes 12 2 16 2 18 2 20 2 22 2 24 3 24 3 27 3 30 3 33 3 36 4 32 4 36 4 40 4 44 4 48 5 40 5 45 5 50 5 55 5 60 6 48 6 54 6 60 6 66 6 72 7 56 7 63 7 70 7 77 7 84 8 64 8 72 8 80 8 88 8 96 9 72 9 81 9 90 9 99 9 108 10 80 10 90 10 100 10 110 10 120 11 88 11 99 11 110 11 121 11 132	Q tim	200	0 tim	00 110) +im		11 +:	1	10 4:	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$										
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$					шаы					~ ~ -
4 32 4 36 4 40 4 44 4 48 5 40 5 45 5 50 5 55 5 60 6 48 6 34 6 60 6 66 6 72 7 56 7 63 7 70 7 77 7 84 8 64 8 72 8 80 8 88 8 96 9 72 9 81 9 90 9 9 9 108 10 80 19 90 10 100 10 110 10 120 11 88 11 99 11 110 11 121 11 132					••					
5 .40 5 .45 5 .50 5 .55 5 .60 6 .48 6 .54 6 .60 6 .66 6 .72 7 .56 7 .63 7 .70 7 .77 7 .84 8 .64 8 .72 8 .80 8 .88 8 .96 9 .72 9 .81 9 .90 9 .99 9 .108 10 .80 10 .100 10 .110 10 .120 11 .88 11 .99 11 .110 .11 .121 .132							4			
6 .48 6 .54 6 .60 6 .66 6 .72 7 .56 7 .63 7 .70 7 .77 7 .84 8 .64 8 .72 8 .80 8 .88 8 .96 9 .72 9 .81 9 .90 9 .99 9 .108 10 .80 10 .100 .						1				
7 56 7 63 7 70 7 77 7 84 8 84 8 72 8 80 8 88 8 96 9 72 9 81 9 90 9 90 9 108 10 80 10 90 10 100 10 110 10 120 11 88 11 99 11					••				• •	
8 64 8 72 8 80 8 88 8 96 9 72 9 81 9 90 9 108 10 80 10 100 10 110 10 120 11 88 11 99 11 110 11 121 11 132					••				• •	
9 72 9 81 9 90 9 99 9 108 10 80 19 90 10 100 10 110 10 120 11 88 11 99 11 110 11 121 11 132					• •				• •	
10 80 ¹ 19 90 10 100 10 110 10 120 11 88 11 99 11 110 11 121 11 132					• •				• •	
11 88 11 99 11 110 11 121 11 132					••				• •	
			• • •		••				••	
$12 \dots 96 \ 12 \dots 108 \ 12 \dots 120 \ 12 \dots 132 \ 12 \dots 144$					••				• •	
	12	96 12	• • •	108 12	••	120 1	2	132,12	• •	144

17. Rule for Simple Multiplication, we en the multiplier is a number not larger than 12.

RULE. Place the multiplier under the multiplicand, units under units, and (if the multiplier be 10, 11, or 12) tens under tens; then draw a line under the multiplier.

Multiply each figure of the multiplicand, beginning with the units, by the figure, or figures of the multiplier (by means

of the Multiplication Table).

Write down and carry as in Simple Addition

Ex. 1. Multiply 531 by 2.

By the Rule.

Twice 1 unit makes 2 units; write 2 in the units' place of the product. Twice 3 tens of units make 6 tens of units; write 6 in the tens' place 10 hundreds of units, or 1 thousand 0 hundred; write 0 in the hundreds' place, and 1 in the thousands' place.

Ex. 2. Find the product of 5063 and 6.

By the Rule.

5063
6 times 3 units = 18 units = 1 ten and 8 units;
write 8 units, carry 1 ten. Next 6 times 6

30378
4 tens = 36 tens, which added to the 1 ten carried
= 37 tens = 3 hundreds and 7 tens; write 7

tens and carry 3 hundreds.

Next 6 times 0 hundreds = 0, which added to the 3 hundreds carried = 300 hundreds, write 3 in the hundreds' place.

Next, 6 times 5 thousands = 30 thousands = 3 tens of thousands and 0 thousands; write 0 in the thousands' place, and

3 in the tens of thousands' place.

Note. It will be seen from the Multiplication Table, that to multiply any number by ten, we have only to write 0 to the right-hand of the number, thus, $3 \times 1 = 3$, $3 \times 10 = 30$; also $5893 \times 10 = 58930$, and $58930 \times 10 = 589300$.

Similarly $3 \times 100 = 300$, $3 \times 1000 = 3000$, and so on.

Also if any number be multiplied by 20, the result is the same as if the number were multiplied by 2, and 0 written on the right hand of the product; thus, $6 \times 20 = 6 \times 2 \times 10 = 12 \times 10 = 120$; also, $60 \times 20 = 1200$, for $60 \times 20 = 60 \times 2 \times 10 = 120 \times 10 = 1200$; and so of any other number.

Similarly $60 \times 200 = 12000$, $60 \times 2000 = 120000$, and so on.

			E	x. XII	I.				
Multiply B y	$ \begin{array}{c} (1) \\ 53 \\ \hline 2 \end{array} $	(2) 47 2	(3) 88 2	(4) 56 2	(5) 48 3	(6) 60 3		(8) 75 3	(9; 27 4
(10) 51 4	(11) 83 4	(12) 90 5	(13) 67	(14) 43 5	(18 36	3	(16) 99 6	(17) 78 6	(18) 27 7

(19)	(20)	(21)	(22)	(23)	(24)	(25)	(26)	(27)
53	45	77	69	54	20	99	53	87
7	8	8	9	9	20	10	11	11
(28)	(29)	(30)	(31)	(32)	(33)	(34)	(35)	(36)
91	60	49	687	800	697	276	777	497
11	12	12	2	3	3	4	5	6
(37) 479 7	(38) 905 7	(39) 835 8	(40 48		41) 560 10	(42) 538 11	(43) 888 12	(44) 704 12

(45) Supposing an acre of land to produce 39 bushels of wheat, how many bushels will 11 of such acres produce, and what will be their value at 6 shillings a bushel?

(46) There are 21 shillings in 1 guinea, and 12 pence in 1 shilling; how many pence are there in 3, 7, 12 guineas?

(47) Charlie bought of Quintin 11 rabbits at 23 cents each, and Quintin bought of Charlie 9 hens at 33 cents each, how many cents had Quintin to give to Charlie?

(48) What is the difference between 12 dozen and 8, and 8 dozen and 12? [Note, 1 dozen=12.]

(49) A has seven thousand four hundred and one potatoes; he sells B fifty-seven dozen and five; C one hundred and twelve dozen and eleven; D two hundred and fifty-nine dozen and nine; and E the remainder. How many more did E buy than C?

Ex. XIV.

	(1) Sy 9048 By 2	(2) 5849 2	(3) 9873 3	38076 3	(5) 6057 4	(6) 97068 5
(7) 69360 6	(8) 80965 5	4390		(10) 48508 8	(11) 33069 7	(12) 38476 9
	(13) 49216 12	(14) 6943		(15) 21357 11	(16) 91537 12	

- (17) Multiply (1) 3870492, (2) 4609758, (3) 85973864, (4) 9090853, (5) 55880092, (6) 987654321, by each of the following, 2, 5, 3, 7, 4, 9, 6, 8, 11, and 12.
- (18) Two persons start from the same place, and trave in the same direction, one at the rate of 93 miles a day, the other at the rate of 79 miles a day; how far apart will they be at the end of a week?
- (19) If the second person at the end of two days turn back, and travel each day in the opposite direction the same number of miles as before; how far will they be apart at the end of a week?
- 18. Rule for Simple Multiplication, when the Multiplier is a number larger than 12.

RULE. Place the multiplier under the multiplicand, units under units, tens under tens, and so on; then draw a line under the multiplier.

Multiply each figure of the multiplicand, beginning with the units, by the figure in the units' place of the multiplier (by means of the table given for Multiplication); write down

and carry as in Addition.

Then multiply each figure of the multiplicand, beginning with the units, by the figure in the tens' place of the multiplier, placing the first figure so obtained under the tens of the line above, the next figure under the hundreds, and so on.

Proceed in the same way with each succeeding figure of

the multiplier.

Then add up all the results thus obtained by the rule of Simple Addition.

Ex. Multiply 2307 by 358. By the Kule,

2307 358 18456 41535

6921

since 358 = 30 + 0.50 + 8, when we multiply by the 5, we in fact multiply by 50, and $2307 \times 50 = 115350$; again, when we multiply by the 3, we in fact multiply by 300, and $2307 \times 300 = 692100$; hence it is quite clear that we may multiply

product = \$25906 by the simple figures 5 and 3, if we only take care to place the first figure in the second line under the tens' place of the first line, and the first figure of the third line under the bundreds' place.

Fx. 2. Find the product of 758 and 609.

758
609
6822
4548
461622

The barboard volume and the place of the second line under the hundreds' place, and not under the tens' place of the line above, for 609 = 600 + 9.

Note 1. If the MULTIPLIER or MULTIPLICAND, or both, end with cyphers, we may omit them in the working; taking care to place on the right hand of the product as many cyphers as we have omitted from the end of the multiplier or multiplicand, or both. Thus, if 270 be multiplied by 507, and 2700 be multiplied by 50700, we have

270 270 In the first case, when we multiply 7 by 7, in fact we 507 50700 multiply 70 by 7, and 70×7 189 189 =490.135 135 In the second case, when 13689000 136890 we multiply 7 by 7, in fact

we multiply 70 by 700, and $70 \times 700 = 49000$.

Note 2. $2 \times 3 = 2 + 2 + 2 = 6$, and $3 \times 2 = 3 + 3 = 6$. $2 \times 3 = 3 \times 2$; and this is true of all numbers.

Note 3. If more than two factors have to be multiplied together, as $2 \times 4 \times 9$, it is termed CONTINUED MULTIPLICATION, and since $2 \times 4 = 8$, and $8 \times 9 = 72$, and $\cdot \cdot 2 \times 4 \times 9 = 72$, we shall of course obtain the same result, whether we multiply any number by 72, or by its factors 2, 4, and 9, by continued multiplication, and so of any other number.

 $35 \times 72 = 2520$, and $35 \times 2 \times 4 \times 9 = 70 \times 4 \times 9 = 280 \times 9 = 2520$.

19. Numbers which are produced by multiplying together two or more numbers respectively greater than unity, are called Composite Numbers. Thus $4 = 2 \times 2$, $36 = 6 \times 6$, or $= 2 \times 3 \times 2 \times 3$, and such like, are Composite Numbers.

Numbers which cannot be broken up into factors, as 3, 5, 7, 11, and such like, are PRIME NUMBERS.

Note 4. The truth of all results in Multiplication may be proved by using the multiplicand as multiplier, and the multiplier as multiplicand; if the product thus obtained be the same as the product found at first, the results are in all probability true.

ARITHMETIO.

]	Ex. X	∇.			
Multi	ipl y B y	(1) 463 18	(2) 678 27	(3 27 3		(4) 601 54	(5) 946 61	(6) 837 39
(7) 793 30	(8) 407 55	(9 86 8		10) 17 46	(11) 692 73	(12) 909 88	(13) 305 715	(14) 463 608
	(15 126 3		(16) 5613 54	3	9673 7		(18) 67628 64	
(19) 495 370	6	20) 390 80	(21) 417 739	(22) 278 900	9		(24) 3259 497	(25) 15900 3300
(26) 50738 9706		(27) 66370 00900	(28 476 51		6810 206	9 48	(30) 5094 7838	(31) 56888 6049
(32) 92035 8007		(33) 8400 789		(34 6780 8760	Ó O	(35 9008 9000	58	(36) 80108 7770

(37) Find the product of seven thousand and thirty-nine by four thousand seven hundred and nine; three thousand nine hundred and a fifty thousand; eighty-seven ahousand nine hundred by nine thousand and six; seven millions eight thousand and five by four hundred thousand seven hundred and three.

(38) Find the product of the sum and difference of four nundred and ninety-six, and three hundred and twelve.

(39) Multiply (1) 973 by 63, and also by its factors 3, 3, and 7, and (2) 33000 by 1560, and also by its factors 13, 5, 4, and 6.

(40) As in (39) do also, (15), (16), (17), (18).

		Ex. XVI		
	(1)	(2)	(3)	(4)
Multiply	78689	27 5832	729817	46481
Ву	547	476	6736	936
,	-		-	-

(5) 40930 779	(6) 9264397 9584	(7) 6707936 9878	(8) 6078908 6725	708670567 9780 6
_	(10) 6S3567 5 26S 9	(11) 27053679 3709		(12) 5S61 2 6289

- (13) Find the product of 3523725 and 2538.
 - (14) " 2778588 and 9867.
 - (15) " 79068025 and 1386.
 - (16) 44 79094451 and 764695.
- (17) Multiply five millions seventy-six thousand eight hundred and twelve by ninety-seven thousand six hundred and thirteen.
- (18) Multiply nine millions five hundred and seven thousand three hundred and forty by seven thousand and seven ty-one.
- (19) Required the product of twelve millions four hundred and eighty-one thousand six hundred and thirty, and afteen hundred and nine.

CIMPLE DIVISION.

20. Simple Division is a short method of repeated Subtraction; or, it is the method of finding now often one number called the Divisor is contained in another number called the Dividend. The number, which shows this, is called the QUOTIENT.

Thus, the dividend 12 divided by the divisor 4 gives the quotient 3; and for this reason, 4 + 4 + 4 = 12, and therefore if we subtract 4 from 12, and then a second 4 from the remainder 8, and then a third 4 from the remainder 4, noth-

ing remains.

If however some number be left, after the divisor has been taken as often as possible from the dividend, that number is called the REMAINDER; thus, Il divided by 4 gives a quotient 2, and a remainder 3; for after subtracting 4 from 11 once, there is a remainder 7; after subtracting 4 a second time trom the remainder 7, there is a remainder 3.

The wign +, called By, or Dividgo By, placed between

two numbers, signifies that the first is to be divided by the second.

Division is just the opposite of Multiplication. By the Multiplication Table, $3 \times 4 = 12$, and $12 \div 4 = 3$, or $12 \div 3 = 4$.

21. Rute for simple Division, when the Divisor is a number not larger than 12.

RULE. Place the divisor and dividend thus: divisor) dividend.

Take off from the left hand of the dividend the least number of figures which make a number not less than the divisor.

Find by the Multiplication Table how often the divisor is contained in this number; write the quotient under the units' figure of this number, and take notice of the remainder.

whether it be any number or 0.

On the right of the remainder (whether it be any number or 0), conceive in your mind to be placed the least number of the figures next following in the dividend which will, affixed to the remainder, make a number not less than the divisor. Proceed, as above, with this new dividend to find the next figure of the quotient; taking care to place after the first figure in the quotient a cypher for every figure just brought down from the dividend except the last.

Continue this process till all the figures in the dividend

have thus been brought down.

If there be a remainder at the end of the operation, write it as a remainder distinct from the quotient.

Ex. 1. Divide 756 by 3.

By the Rule,

3)756

Method of working. 3 in 7 goes 2 times and 1 over, write 2 under the 7; 3 in 15 goes 5 times, write 5 under the 5; 3 in 6 goes 2 times, write

2 under the 6.

Reason. In 756 the 7=700, the 550, = and the 6=6 Now 3 in 700 goes 200 times, and 100 over, therefore write 1 in the hundreds place, and carry the 100; then 3 in 100 + 50, on 150, goes 50 times, therefore write 5 in the tens' place; then 3 in 6 goes 2 times, therefore write 2 in the guits' place.

Ex. 2. Find the quotient of 21406 by 7.

Method of working. 7 in 2 goes no times, 7)21406 but 7 in 21 goes 3 times, write 3 under the 1; 3058

7 in 4 goes no times, 7 in 40 goes 5 times and 5 over; write 0 under the 4 and 5 under the 0; then 7 ip 56 goes eight times, write eight under the 6.

In 21406 the 21 is = 21000, the 4 = 400, and the Reason. 6 = 6.

... the 3 in the quotient = 3000, the 5 = 50, the 8 = 8. and the quotient is 3058.

Ex. 3. Into how many classes of eleven each can a population of eight hundred and ninety thousand three hundred and eighty-nine to be divided?

11)890389

80944 rem. 5. i. e. 80944 classes and 5 people over, or $890389 = 80944 \times 11 + 5$

11 in 8 will not go, 11 in 89 goes 8 and 1 over, write 8 under the 9; 11 in 10 will not go, 11 in 103 goes 9 and 4 over, write 0 under the 0, and 9 under the 3; 11 in 48 goes 4 and 4 over, write 4 under the 8; 11

Ex. 4. Distribute six hundred thousand four hundred and fifty-five apples in equal portions between 12 families.

12)600455

50037 rem. 11

. each family receives 50037 apples, and there are 11 apples over; or

500455 less 11 = 50037 × 12

in 49 goes 4 and 5 over, write 4 under the 9, and rem. 5.

12 in 60 goes 5: for the next dividend we have 045, ... we write two cyphers or 00 after the 5; 12 in 45 goes 3 and 9 over, .. write 3 after 0; then 12 in 95 goes 7 and 11 over. .. write / after 2, and rem. 11.

Ex. XVII.

Each of the given numbers is to so divided any sach f the different divisors.

- (1) 88, 93, 98, 103, 100, by 6, 9, and 5.
- 105, 110, 119, 128, 117, by 5, 11 and 10. (2)
- 130, 141, 153, 168, 147, by 6, 12, and 11. (3)
- 172 !95, 206, 257, 240, by 6, 8, and 12. (4)
- (5)462, 682, 840, 405, 555, by 4, 10, and 11,
- (6)600, 763, 842, 999, 717, by 11, 8 and 12.
- (7) 1210, 6876, 606g, 5000, by 9, 12, and 11,

- (8) 2760, 9604, 3267, 6548, by 8, 12, and 10.
- (9) 86246, 72635, S5490, 35298, by 12, 10, and 3
- (10) 76002, 90009, 53027, by 11, 8, and 12.
- (11) 5470698, 93700682, 2060198, by 8, 10, and 11.
- (12) 8360047, 6789643, 9889989, by 7, 9, and 12.
- (13) How many times can you subtract twelve from eight hundred thousand seven hundred and nine? What number besides 11 will exactly divide 218581?
- (14) (1) If the dividend be 84, the quotient 9, the remainder 3, what is the divisor? (2) If the divisor be 11, the remainder 7, the quotient 146, what is the dividend?
- (15) A woman bought 11 fowls at 36 cents each, and sold them so as to gain 198 cents; what did she sell each fowl for?
- (16) A boy, having a basket containing 214 plums, distributed them equally between his eight schoolfellows and himself; the number which remained over he gave to his schoolmaster; how many did the schoolmaster receive?
- (17) The sum of two numbers is 4563, and the less number is 9; find their quotient.
- (18) Find the difference between the product of 40687 and 503, and the quotient of 93710562 by 11.
- (19) A Bachelor, who died worth 5427 dollars, left 1500 dollars to charities, and the rest of his property between his housekeeper, manservant, and cook; the manservant was to have twice the cook s share, and the housekeeper was to have twice the manservant's share; what did each receive.
- (20) If the sum of 18 and 30 be divided by their difference, and the quotient be multiplied by the product of 16 and 27, what is the result?
- (21) Find the product of nine hundred and seven thousand and fifty seven by six millions and six, and find what number added to the result will make it exactly divisible by nine.
- (22) A basket contained 282 apples and oranges; there were 230 more apples than oranges. Find the number of oranges
- (23) How many penknives, worth 16 cents each, ought to be exchanged for 4 gross of penholders at 10 cents per dozen, and twenty-five score envelopes at 16 cents a hundred? No. 1 peops—20, 1 gross—12 dozens.

SIMPLE DIVISION.

22. Rule for Simple Division, when the Divisor is a number earger than 12.

RULE. Place the divisor and dividend thus:

divisor) dividend (

eaving a space for the quotient on the right of the dividend.

Take off from the left hand of the dividend the least number of figures which make a number not less than the divisor.

Find how many times the divisor is contained in this number; write the quotient as the left-hand figure of the whole quotient: multiply the divisor by this figure, and bring down the product under the number taken off from

the left of the dividend, and subtract.

On the right of the remainder (whether it be any number or 0) place the least number of figures next following in the dividend which will, affixed to the remainder, make a number not less than the divisor. Proceed as above with this new dividend to find the next figure of the quotient; taking care to place after the first figure in the quotient a cypher for every figure just brought down from the dividend except the last.

Continue this process till all the figures in the dividend

have thus been brought down.

If there be a remainder at the end of the operation, write it as a remainder distinct from the quotient.

Note. If any remainder be equal to or greater than the divisor, the last figure of the quotient must be changed for one greater.

Ex. 1. Divide 1368 by 57.

By the Rule,

57) 1368 (24 Method of Working. 136 is the least number taken from the left of the dividend, into which 57 will go; we then say 5 into 11 goes

228 2; write 2 as the first figure of the quotient on the right hand, write also 114 (product of

 67×2) under 136 and subtract; we obtain a remainder 22. Then place 8, the next figure in the dividend, to the right of the remainder; we thus obtain a new dividend 228; as before 5 into 22 goes 4; write the 4 to the right of the 2 in the quotient; and so proceed till all the figures in the dividend are brought down.

Reason. 1368 = 1360 + 8; ... the 1st dividend is really 1360; now $57 \times 20 = 1140$, ... the 1st number in the quotient is 20: and 1360 - 1140 = 220; ... the second dividend is 220 +

8 or 228, and as $57 \times 4 = 228$, ... the second figure in two quotient is 4, and the quotient is 20 + 4 or 24.

Note. Since $136\$ \div 57 = 24$ it follows that $136\$ \div 24 =$

57, and also that $57 \times 24 = 1368$.

Ex. 2. Find the quotient of 1039888 by 5048.

5043 1039888 (206 10398 is the *least* number, taker from the left of the dividend, into which 5048 will go; we then say 5 in 10 goes 2, and 5048 × 2 = 10096; write 2 as the left-hand figure of the quo-

tient, 10096 under 10398, and subtract; we obtain a remainder 302. Then we have to place the next two figures 88 of the dividend to the right of this remainder to form a number 30288 greater than the divisor, ... we must write 0 in the quotient after 2; then 5 in 30 goes 6 times, and 5048 × 6 = 30288, write 6 in the quotient after 0, 30288 under 30288, and subtract; there being no remainder, 206 is the quotient required.

Ex. 3. How many times does 318493585 contain 8607? 8607)318493585(37004

25821	
60283 60249	After obtaining 37 in the quotient, 3 figures of the divid-
34585 34428	end have to be brought down to get the next significant fig- ure in the quotient, write
157	two cyphers in the quotient.

\$607 is contained 37004 times in \$18493585, and there is a remainder 157; in other words $318493585 = 37004 \times 8607 + 157$, or 318493585 less $157 = 37004 \times 8607$.

23. When the divisor is a composite number, and made up of two factors, neither of which exceeds 12, the dividend may be divided by one of the factors in the way of Short Division, and then the result by the other factor. If there be a remainder after each of these divisions, the true remainder will be found by multiplying the second remainder by the first divisor, and adding to the product the first remainder.

Ex. 4. Divide 56732 by 45.

45

56732, i. e. 56732 units.

6303 rem. 5, i. e. 6303 nines and rem. 5 units,

1260 rem. 3, i.e. 1260 forty-fives, and rem. 3 mnes.

the true rem. $=9 \times 3$ units + 5 units = 27 + 5, or 32 units

Therefore the quotient arising from the division of 56732 by 45 is 1260, with a remainder 32 over.

Ex. XVIII.

ån vidu

- (1) 192 by 16; 720 by 18; 795 by 15; 1786 by 19.
- (2) 1035 by 23; 1073 by 37; 2730 by 42; 5432 by 56.
- (3) 4560 by 80; 3871 by 49; 7744 by 88; 6935 by 95.
- (4) 5375 by 25; 29526 by 37; 25665 by 29; 4590 by 45.
- (5) 69230 by 86; 37510 by 55; 10287 by 81; 23919 by 67; 25760 by 56; 538840 by 76.
- (6) 35626 by 94; 31339 by 77; 80840 by 86; 28782 by 39; 9009196416 by 96; 41765256 by 72.
- (7) 88832 by 256: 175252 by 308: 321776 by 104.
- (8) 653723 by 329 : 3577926 by 506 : 542100 by 834.
- (9) 8189181 by 909; 4049820 by 745; 342604 by 883,
- (10) 7848600 by 365 : 2339100 by 678 : 90625 by 727.
- (11) 27291888 by 478; 30387310 by 397; 3273068 by 703.
- (12) 37624792 by 843; 90273189 by 513; 53006751 by 609; 30073074 by 358; 630762540981 by 652.
- (13) 519387042 by 2731; 10101255 by 2185; 154725876 by 3076; 632798014 by 7243.
- (14) 2015029 by 1004; 131686100 by 6487; 395494875 by 6007; 50696184 by 1617.
- (15) 4519559744 by 5008; 16322853 by 9306; 23617103060 by 1579; 2106144185 by 2735.
- (16) 142997420 by 3782; 19554707200 by 6016; 2828882701578 by 38706.
- (17) What number multiplied by 79 will give the same product as 257 multiplied by 553?
- (18) How many pairs of stockings, at 66 cents a pair, should be given for 9 dozen pairs of gloves, at 110 cents a pair?
- (19) What number must be added to thirty millions nine hundred and eighty-four thousand and filty-one, that the sum may be exactly divisible by two hundred and eightyeight?
 - (20) If the sum of 274 and 108 be multiplied by the

difference, and the product be divided by 176, what will be the quotient?

- (21) A farmer bought 75 sheep at 4 dollars each; 94 sheep at 3 dollars each; and 106 sheep at 2 dollars each; at what price per head must be sell the sheep, so as to gain 147 dollars by his bargain?
- (22) A hatter sold 267 nate of '968 dollars, gaining thereby I dollar on each hat, what did each hat cost him?
- (23) If the sum of 103, 29, and 267 be divided by 19, and the quotient be multiplied by 57, and the product be dimin ished by 197, what will the remainder be?
- (24) 8 lambs are worth 16 dollars, and 15 sheep are worth 60 dollars; how many of such sheep ought to be given in exchange for 840 of such lambs?
- (25) The sum of the product of two numbers and 355 is eighty-seven thousand four hundred and three; one of the numbers is 216; find the other number.
- (26) What number must 416 be multiplied by to produce 154979552?
 - (27) What number subtracted 28 times from 479632 will leave 20 as a remainder?
 - (28) A farmer bought 29 bullocks for 1885 dollars, and after keeping them for 3 months, and spending on each 5 dollars per month, he sold all the bullocks for 2610 dollars; what was his gain on each bullock?
 - 24. If the Divisor terminate with a cypher or cyphers, the process of Division can be shortened by the following Rule.

RULE. Cut off the cypher or cpyhers from the divisor, and as many figures from the right-hand of the dividend, as there are cyphers to cut off at the right-hand end of the divisor; then proceed with the remaining figures according to the Rule, Art. 21 or Art. 22. as the case may be; and to the last remainder affix the figures cut off from the dividend for the true remainder.

Ex. 1 Divide 57 by 20.

2.0)5,7

57 = 50 + 7, sow 20 goes 2 in 50 with rem
10, ... when the 5 is divided by the 2, the rem
1 is really 1 ten, or 10, and the true rem. =
10 + 7 or 17

SIMPLE DIVISION.

Ex. 2. Divide 46431 by 500.

46431 = 46400 + 31, and 46400 divided 5.00)464,31 by 500 = 92 with rem. 400, ... when the 464 is divided by the 5, the rem. 4 is really 92 rem. 4.

400, and the true rem. 431.

Ex. 3. Divide 375340 by 5900

59,00)3753,40(63

354 .: quotient = 63, and rem. = 3640. 213 177 36

Ex. 4. Divide 563854 by 10, by 1000, and by 100000. We may write down the quotient and remainder for each ques tion at once.

1st quotient = 56385, and rem. = 4. Thus: 2nd 563, = 854.3rd 5. =63854

Ex. XIX.

- .1) Divide 34, 43, 56, 80, 135, 260, 1504, by 10, 20, and 30.
- (2) Divide 237, 840, 673, 291, 6019, 7820, 81229, 327800, by 40, 60, 70, 100, and 200,
- (3) Divide 7°048, 6870, 890061, by 240, 1000, 1500, and 1600; and 830678.03490 by 100000000.
 - (4) $806753245 \div 9067$.
 - $612709066 \div 70602$ (5)
 - (6) 60005836 ÷ 896.
 - (7) 70867509 9986.
 - (8) 8673456954 ÷ 868.
 - (9) $200006783 \div 93256$.
 - (10) Multiply 14609 by 719 and divide the product by 8067.
- (11) How many regiments of 1000 men, and also of 1200 men, can be formed out of one million one hundred thousand men?
- (12) Add together twenty-five millions seven hundred and sixty thousand and thirty-four, 75211379 and 4637862; subtract ten millions and seventy-five from the sum; divide the remainder by 100000.

SECTION IL

MONEY TABLES.

CANADIAN CURRENCY.

25 The silver coins are: a 5 cent piece.

a 10 a 20 a 25 a 50



(00 cents make one dollar, or \$1.

Note 1. The cent which is made of bronze, is one inch is meter, and 100 cents weigh one pound avoirdupois.

HALIFAX OR OLD CANADIAN CURRENCY.

2 Farthings make 1 Half-penny, or 1de 2 Half-pence 1 Penny ld.

12 Pence . . . 1 Shilling . . . 1s. 5 Shillings . . 1 Dollar . . . \$1. 4 Dollars 1 Pound£1.

Note 2. The farthing is written thus, 1d; and three farthings thus, ad.

ENGLISH OR STERLING CURRENCY.

2 Farthings make 1 Half-penny, or 3d. 7. 2 Half-pence 1 Penny ld.

12 Pence 1 Shilling 18. 20 Shillings 1 Pouna£1.

The sovereign, a gold coin = 20 shillings. The guinea, a gold coin not now in ase = 21 shillings.

No. 3. The sterling pound = \$4.86% Canadian currency.

UNITED STATES CURRENCY.

10 Mills make 1 Cent.

10 Cents 1 Dime. 10 Dimes 1 Dollar.

10 Dollars 1 Eagle.

WEIGHTS AND MEASURES.

TABLE OF TROY WEIGHT.

29 .	TROY	WEIG	нт із т	ısed	ir	weigh	ning	gold	, silv	ver, o	lia-
monds,	and	other	articles	of	a	costly	nat	ure;	and	also	ij
determ	ining	specific	c graviti	ies.							

24 Graiffs, grmake 1 Pennyweight	
20 Pennyweights 1 Ounce	l oz.
12 Ounce 1 Pound 1 lb.	or 1 th.

TABLE OF AVOIRDUPOIS WEIGHT.

30. Avoirdupois Weight is used in weighing all heavy sticles, which are coarse and drossy, or subject to waste, as butter, meat, and the like, and all objects of commerce, with the exception of medicines, gold, silver, and some precious stones.

16 Drams, drmake	1 Ounce	l oz.
16 Ounces	1 Pound	1 lb.
25 Pounds	1 Quarter	l gr.
4 Quarters, or 100 lbs	1 Hundredweight	1 cwt.
20 Hundredweights	1 Ton	l ton

Note. 1 lb. Avoirdupois weighs 7000 grs. Troy. TABLE OF APOTHECARIES' WEIGHT.

31. Apothecaries' Weight	r is used in mixing medicines
20 Grains, grmake	1 Scruple 1 sc. or 1 3
3 Scruples	1 Dram 1 dr. or 1 3
8 Drams	1 Ounce 1 oz. or 1 3
12 Ounces	1 Pound 1 lb. or 1 h

TABLE OF LINEAL MEASURE.

32. In this measure, which is used to measure distances lengths, breadths, heights, depths, and the like, of places o things:

12 Lines make 1 Inch	11
12 Inches 1 Foot	1 ft
3 Feet, or 36 in 1 Yard	1 ya
6 Feet1 Fathom	l fth.
53 Yards, meaning 5 yards and Rod, Pole, or Perch	1
a half yard or Perch	ı po.
40 Poles, or 220 yds 1 Furlong	1 fur.
8 Furlongs, or 1760 yds 1 Mile	l mi.
3 Miles l League	l lea

The following measurements may be added, as useful in tertain cases:

- 4 Inches make 1 Hand (used in measuring horses).

 22 Yards 1 Chain (used in measuring land.)

 100 Links 1 Chain
- A degree is equal to 60 geographical, or nearly 691 English miles.

TABLE OF CLOTH MEASURE.

33. In this measure, which is used by linen and woolles arapers:.

$2\frac{1}{4}$	Inches make	1	Nail	1	nı.
4	Nails	1	Quarter	1	qr.
4	Quarters	ŀ	Yard	l	yd.
5	Quarters	1	Ell (English).		•
6	Quarters	1	Ell (French).		

TABLE OF SQUARE MEASURE.

34. This measure is used to measure all kinds of surface or superficies, such as land, paving, flooring, in fact everything in which length and breadth are to be taken into account.

A SQUARE is a four-sided figure, whose sides are equal, each side being perpendicular to the adjacent sides. See figure below.

A square inch is a square, each of whose sides is an inch in length; a square yard is a square, each of whose sides is yard in length.

- Note. This table is formed from the table for lineal measure, by multiplying each lineal dimension by itself.

640 Acres = 1 Square Mile

The truth of the above table will appear from the following considerations.

Suppose AB and AC to be lineal yards placed perpendicularly to each other.



Then ABCD is a square yard. If AE, EF, FB, AG, GH, HC, each = 1 lineal foot, it appears from the figure that there are 9 squares in the square yard, and that each square is 1 square foot.

The same explanation holds good

of the other dimensions.

TABLE OF SOLID OR CUBIC MEASURE.

35. This measure is used to measure all kinds of solids, or figures which consist of three dimensions, length, breadth,

and depth or thickness.

A CUBE is a solid figure contained by six equal squares; for instance, a die is a cube. A cubic inch is a cube whose side is a square inch. A cubic yard is a cube whose side is a square yard.

40 Cubic Feet of Rough Timber or

50 Cubic Feet of Hewn Timber 1 Load.

42 Cubic Feet 1 Ton of Shipping.

128 Cubic Feet of Fire-wood 1 Cord.

16 Cubic Feet of Fire-wood ! Cord-foot.

The truth of the first part of above table will appear from sefollowing considerations.

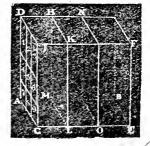
If AB, AC, and AD be per pendicular to each other, and each of them a lineal yard in length, then the figure DE is a cubic vard.

Suppose DH a lineal foot, and HKLM a plane drawn

parallel to side $D\hat{C}$.

By the table Art. 34, there are 9 square feet in side DC. There will therefore be 9 cubic feet in the solid figure DL.

Similarly, if another lineal



foot HN were taken, and a plane NO were drawn parallel to HL, there would be 9 cubic feet contained in the solid figure HO.

Similarly, there would be 9 cubic feet in the solid figure

NE.

Therefore, there are 27 cubic feet in the solid figure DE, or in 1 cubic yard.

Note. A pile of word 4 feet high, 4 feet wide, and 8 teet long, makes a cord.

MEASURES OF CAPACITY.

TABLE OF WINE MEASURE.

36. In this measure, by which wines and all liquids, with the exception of malt liquors and water, are measured

4 Gillsmake	I Pintl pt.
2 Pints	
4 Quarts	l Gallon l gal.
6 3 Gallons	
	1 Pipe1 pipe.
	1 Tun 1 tun.

TABLE OF ALE AND BEER MEASURE.

37. In this measure, by which all malt liquors and water are measured:

2 Pints	make 1	Quart	l	qt.
4 Quarts	1	Gallon	1	gal
9 Gallons	1	Firkin	1	fir.
18 Gallons	A	Kilder	kin .1	kil.
36 Gallons	l	Barrel	1	bar.
11 Barrels, or 54	Gallons 1	Hogshe	ead .1	hhd.
2 Hogsheads				
2 Butts				

TABLE OF DRY MEASURE.

38.	2 Pints make l Quart 1 qt.
	4 Quarts 1 Gallon 1 gal.
	? Gallons 1 Peck 1 pk.
	4 Pecks 1 Pashel 1 bu.
	36 Bushels ! Chaldron! ch

TABLES-MEASURES OF TIME

30	34	Pounds 7	nake	1 Bushel of Oats.
	48	Pounds		1 Bushel of B'kwheat, Barley or Timothy,
	5 0	Pounds		1 Bushel of Flax Seed.
	56	Pounds		1 Bushel of Rye or Indian Corn.
	60	Pounds		l Bushel of Wheat, Potatoes, Peas,
		\		Beans Onions or Red Clover Seed

Note 1. Grains are sold by the cental (100 lbs.), or by parts thereof.

MEASURES OF TIME.

TABLE OF TIME.

40.	1 Second is written thus 1".				
60	Seconds unake	1	Minute		
60	Minutes	l	Hourl hr.		
24	Hours	1	Day 1 day.		
			Week1 wk.		
4	Weeks, or 28 days	1	Lunar month mo.		
365	Days	1	Civil or common year.1 yr.		

Note 2. 60 minutes make 1 degree, or 60' make 1°.

A degree is the 350th part of the circumference of a circle.

A year is divided into 12 months, called Calendar Months, the number of days in each of which may be easily remembered by means of the following lines;

> Thirty days hath September, April, June a November: February has twenty-eight alone And all the rest have thirty-one: But leap-year coming once in four, February then has one day more.

Note 3. A civil or common year = 52 wks, 1 day.

A leap year = 366 days.

Every year which is divisible by 4 without a remainder is a LEAP OR BISSENTILE YEAR; except those years which complete a century (i. e. a hundred years), the numbers expressing which century, are not divisible by four; thus 1600 and 2000 are leap years, because 16 and 20 are exactly divisible by 4: but 1700, 1800 and 1900 are not leap years, because 17 18, and 19 are not exactly divisible by 4.

MISCELLANEOUS TABLE

4),	12 Units make	1 Dozen.
	12 Dozen	1 Gross.
	12 Gross	1 Great Grove
	20 Units	1 Score.
	24 Sheets of Paper.,	1 Quire.
	20 Quires	1 Ream.
	100 Pounds	1 Quintal.
	196 Pounds	
		1 Barrel of Pork or Beef.

Note. A sheet folded into two leaves is called a folio, into 4 leaves a quarto, into 8 leaves an octavo, into 16 leaves a 14 mo, into 18 leaves an 18 mo, &c.

REDUCTION.

- 42. When a number is expressed in one or more denominations, the method of finding its value in one or more other denominations is called REDUCTION. Thus, £1 is of the same value as 240d., and 7s. 1½d. is of the same value as 342 farthings, and conversely; the method or process by which we find this to be so, is REDUCTION.
- 43. First. To express a number of a higher denomination or of higher denominations in units of a lower denomination.

RULE. Multiply the number of the highest denomination in the proposed quantity by the number of units of the next lower denomination contained in one unit of the highest, and to the product add the number of that lower denomination, if there be any in the proposed quantity.

Repeat this process for each succeeding donomination, till

the required one is arrived at.

Ex. 1. How many cents in \$75.65 cents? By the Rule,

75.65 100 7500 + 65 = 7565 cents.

Reason. Since 100 cents make one dollar; \$75 = (75 × 100 cts.) = 7500 cts., ... \$75.65 = 7500 + 65 = 7505 cents.

- · · 375.65 = 7565 censa.

REDUCTION.

Ex. 2. Reduce £2 to farthings. By the Rule,

$oldsymbol{\pounds}_2$	Reason jor the Rute.
$\frac{20}{40}$ 8.	£1 = $20s$., £2 = $(2 \times 20)s$. = $40s$.
12	1s. = $12d$., $\therefore 40s$. = $(40 \times 12)d$. = $480d$.
480d.	$1d. = 4q., \therefore 480d. = (480 \times 4)q. = 1920q.$
1920a	$\therefore £2 = 40s. = 480d. = 1920q.$

Ex. XX.

- Juce

- (1) £709. 16s., 8d, to farthings.
- (2) 17 mls., 1 fur., 2 ft., 6 in. to inches.
- (3) 8 tons, 2 cwt., 3 qrs., 5 lbs. to drams.
- (4) 612 ac., 2 r., 271 yds. to square inches.
- (5) 10 mls. 5 fur., 5 po., 5 yds., 0 ft., 5 in., 5 ls. to lines
- (6) 5 ac., 3 per., 29 yds. to square inches.
- (7) 17 days to minutes.
- (8) 2 lbs., 11 oz., 20 grs. to grains.
- (9) 2 lea., 2 mls., 7 fur. to yards.
- (10) 23 cub. yds., 1000 in. to cubic inches.
- (11) 13 galls., 3 qts. to gills.
- (12) 220 bushels to quarts,
- (13) 3 yrs., 315 days to minutes.
- (14) 27 lbs., 5 oz., 16 dwts. to grains.
- (15) 47 lbs., 11 oz., 6 drs., 2 sc. to grains.
- (16) £200. 17s., 8½d. to half-pence.
- (17) 219 ac., 2 r., 16 per. to square yards
- (13) 218 yds., 2 qrs., 3 nls. to nails.
- (19) £2376. 19s., 81d. to farthings.
- (20) 216 cwt., 2 qrs., 17 lbs. to pounds.
- (21) 25° 36' to seconds.
- (22) 8 mls., 3 fur., 4 yds. to inches.
- (23) £312 17s., 61d. to farthings
- (24) 105 lbs. Troy to grains.

- (25) 26 English ells to vails.
- (26) 37 French ells to nails.
- (27) £567. 0s. 61d. to farthings
- (28) 287 lis., 6 oz. to scruples.
- (29) 3 pipes to gallons.
- (30) £200. 19s., 61d. to farthings.

44. Secondly. To express a number of lower denomination or denominations in units of a higher denomination.

RULE. Divide the given number by the number of units which connect that denomination with the next higher, and the remainder, if any, will be the number of surplus units of the lower denomination.

Carry on this process, till you arrive at the denomination

equired.

Fx. 1. How many tons, cwts., &c., are there in 27658 drams? By the Rule, $16 \begin{cases} 2 \\ 8 \end{cases} = \frac{27658}{13829} = 10 \text{ drs.} \qquad 16 \text{ drs.} = 1 \text{ oz.}, \cdots 27658 \div 16 = 1728 \\ \text{oz.} + 10 \text{ drs.} \qquad 27658 \div 16 = 1728 \\ \text{oz.} + 10 \text{ drs.} \qquad 16 \text{ oz.} = 1 \text{ lb.}, \cdots 1728 \text{ oz.} \div 16 = 108 \\ \text{lbs.} + 0 \text{ oz.} \qquad \text{lbs.} + 0 \text{ oz.} \qquad \text{lbs.} + 0 \text{ oz.} \qquad 100 \text{ lbs.} \div 25 = 4 \\ \text{oz.} + 10 \text{ drs.} \qquad 100 \text{ lbs.} \div 25 = 4 \\ \text{oz.} + 10 \text{ drs.} \qquad 100 \text{ lbs.} \div 25 = 4 \\ \text{oz.} + 10 \text{ drs.} \qquad 100 \text{ lbs.} \div 25 = 4 \\ \text{oz.} + 10 \text{ drs.} \qquad 100 \text{ lbs.} \div 25 = 4 \\ \text{oz.} + 10 \text{ drs.} \qquad 100 \text{ lbs.} \div 25 = 4 \\ \text{oz.} + 10 \text{ drs.} \qquad 100 \text{ lbs.} \div 25 = 4 \\ \text{oz.} + 10 \text{ drs.} \qquad 100 \text{ lbs.} \div 25 = 4 \\ \text{oz.} + 10 \text{ drs.} \qquad 100 \text{ lbs.} \div 25 = 4 \\ \text{oz.} + 10 \text{ drs.} \qquad 100 \text{ lbs.} \div 25 = 4 \\ \text{oz.} + 10 \text{ drs.} \qquad 100 \text{ lbs.} \div 25 = 4 \\ \text{oz.} + 10 \text{ drs.} \qquad 100 \text{ lbs.} \div 25 = 4 \\ \text{oz.} + 10 \text{ drs.} \qquad 100 \text{ lbs.} \div 25 = 4 \\ \text{oz.} + 10 \text{ drs.} \qquad 100 \text{ lbs.} \div 25 = 4 \\ \text{oz.} + 10 \text{ drs.} \qquad 100 \text{ lbs.} \div 25 = 4 \\ \text{oz.} + 10 \text{ drs.} \qquad 100 \text{ lbs.} \rightarrow 200 \text{ lbs.} \qquad 100 \text{ lbs.} \qquad 100 \text{ lbs.} \rightarrow 200 \text{ lbs.} \qquad 100 \text{ lbs.} \qquad 100 \text{ lbs.} \rightarrow 200 \text{ lbs.} \qquad 100 \text{ lbs.}$

.:. 27658 drams == 1 cwt., 0 qrs., 8 lbs., 0 oz., 10 drs.

Ex. 2. In 17392 cents, how many dollars and cents. By the Rule.

$$100 \begin{cases} 10 \middle| \frac{17392}{1739} & Reason for the Rule, \\ 10 \middle| \frac{1739-2}{\$173-92} & 100 \text{ cents } = \$1, \dots 17392 \text{ cts.} \div 100, \\ = \$173 + 92 \text{ cts.}, \dots 17392 \text{ cents} \end{cases}$$

Note. From the above example, we see that by cutting off the last 2 figures on the right of any number of cents gives the dollars and the figures so cut off will be the cents

Ex. XXI.

Reduce.

- (1) 123290 farthings to pounds.
- (2)13172 grs. to lbs. Troy.
- (3) 18191 pts. to gallons.
- How many leagues in 76787565 inches? (4)
- How many tor, &c., in 2007008 drams? (5)
- (6) How many acres in 93827 perches?
- In 167812 grs., how many lbs. Troy? (7)
- In 8756765637 lines, how many miles, &c.? (8)
- In 7678678956 drs., how many tons, &c.? (9)
- (10)In 121605 in., how many miles, &c.?
- (11)In 98006 grs., how many lbs. Troy, &c.?
- In 2022752 drs., how many tous, &c.? (12)
- How many lbs., ozs., drs., &c., in 702917 grs.? (13)
- How many years (365 ds.), &c., in 1727893 seconds (14)
- How many acres, &c., in 172425 vards? (15)
- How many yards in 13856832 cubic inches? (16)
- How many acres in 1244160000 sq. inches? (17)
- How many yards, &c., in 500 nails? (18)
- (19) In 131075 seconds, how many degrees, &c.?
- In 31557600 seconds, how many days, &c.? (20)
- (21)In 219612 pts., how many hogsheads of beer?
- In 300738 pts., how many hogshads of wine? (22)
- In 912715 lbs., how many bushels of wheat? (23)
- In 1000000 lbs. of oats, how many bushels? (24)
- In 7263 lbs. of timothy seed, how many bushels? (25)
- (26)In 30747 cents, how many dollars?
- (27) How many pounds, &c., in 973647 farthings?

COMPOUND ADDITION.

45. COMPOUND ADDITION is the method of collecting several numbers of the same kind, but containing different denominations of that kind, into one sum.

Arrange the numbers, so that those of the same denomination may be under each other in the same column

and draw a line below them.

Add 'he numbers of the lowest denominations together, and find by Reduction how many units of the next higher denomination are contained in this sum.

Write the remainder, if any, under the column just added.

and carry the quotient to the next column.

Proceed thus with all the columns.

Ex. 1. Add together \$21 97, \$28.76, \$38.39.

By the Rule, \$21.97 The sum of the right-hand column is 22; \$28.76 write 2 under that column, and carry 2 to the

\$38.39 next; the sum of the next column together with the 2 carried is 21; write 1 under that column

\$89.12 and carry 2 to the next, and so on; the same way as was done in the Simple Rules, and for the same reason.

Ex. 2. Find the sum of £6. 6s., £3. 13s. $0\frac{3}{4}d$., £33. 15s. $11\frac{1}{2}d$., and £43. 0s. $8\frac{1}{4}d$.

 $1q. + 2q. + 3q. = 6q. = \frac{1}{2}d.$ write down å, 1d., and carry 1d. 0 Then 1d. + 8d. + 11d. = 20d. = 1s. 8d.: 3. 03 13. write down 8d., and carry 1s. 15. 35.111 Then 1s. + 15s. + 13s. + 6s. = 35s. = £181 43 . 0. 15s.; write down 15s, and carry £1. Then £1 + £43 + £35 + £3 + \$6 = 81 £88 . 15. £88: write down £88.

Note. The method of proof in the Compound Rules is the same as in the Simple Rules.

Er. XXII.

Add together.

	i logether.		£	8.	á.	qrs.	Iba.	08.
(1)	\$26.79	(2)	6.	9.	8	(3) 2.	17.	12
. ,	. \$39.17	• •	8	10.	4	€.	24 .	13
	\$28.68		5	12.	3	1.	6.	8

	lbs. os. dwt.	gr.		lbs.	OZ.	dr.	SC.	gr.
(4)	35 . 3 . 4 .	12	(5)	17.	8.	2.	ı.	5
	27 . 8 . 14 .	22	• •	12.	10.	6.	0.	19
	41 . 9 . 17 .	10		6 .	6.	4 .	2.	18
	2 . 3 . 13 .	21		17.	11.	7.	2.	19

(6) \$ 286.97 6126.35 517.68 9612.07 71C.15	tons cwt. qrs. lbs. oz. 21 . 16 . 2 . 24 . 10 26 . 5 . 1 . 22 . 9 1 . 17 . 3 . 19 . 12 19 . 12 . 0 . 18 . 9 218 . 10 . 1 . 12 . 8
yds. qrs. nls. (6) 27 . 2 . 3 35 . 3 . 2 217 . 1 . 3 89 . 2 . 2 207 . 3 . 2	mls. fur. per. yds. ft. (9) 2 . 3 . 8 . 2 . 2 25 . 7 . 21 . 4 . 1 3 . 6 . 23 . 2 . 0 17 . 4 . 19 . 3 . 2 29 . 5 . 16 . 1 . 1
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	dys. hrs. min. sec. (11) 2 . 16 . 16 . 17 27 . 22 . 22 . 33 19 . 21 . 30 . 37 28 . 23 . 39 . 50 36 . 20 . 45 . 55
(12) \$2219.64 (13) 3812.75 913.25 837.19 687.29	ac. ro. per yds. ft. in. 5 . 0 . 7 . 13 . 2 . 5 7 . 3 . 9 . 22 . 8 . 107 9 . 1 . 16 . 29 . 2 . 96 19 . 2 . 22 . 27 . 6 . 108 0 . 3 . 7 . 28 . 3 . 12
3. 9.2.17,13	. 0 (35) \$5617.28

COMPOUND SUBTRACTION.

46. COMPOUND SUBTRACTION is the method of finding the difference between two numbers of the same kind, but containing different denominations of that kind.

RULE. Place the less number below the greater, so that the numbers of the same denomination may be under each other in the same column, and draw a line below them. Begin at the right hand, and subtract if possible each number of the lower line from that which stands above it,

and set the remainder underneath.

But when any number in the lower line is greater than the number above it, add to the upper one as many units of the same denomination as make one unit of the next higher denomination; subtract as before, and carry one to the n "" of the next higher denomination in the lower line,

Proceed thus throughout the columns.

Ex. 1. From £51. 0s. 8½d., take £47. 18s. 7¾d.

By the Rule,

£ d. d. 51 . 0 . 8½ 47 . 18 . 7½

Method of working. I cannot take 3q. from 2q., so I add 1d., or 4q., to the 2q., making it 6q.; then 3q. from 6q. leaves 3q.; write down the 3q.; in e der

£3. 2. 03 leaves 3q.; write down the 3q.; in e der to increase the lower number equally with the upper, I add ld. to the 7d., making it 8d.; then 8d. from 8d. leaves 0d.; write down 0d. I work the remaining columns in the same way, and find the required answer.

Ex. 2. From \$978.29 take \$678.93.

\$978.29 \$678.93 \$299.36

This example is worked in the way way as Simple Subtraction.

Ex. XXIII.

(1)	3 3 .	17 . 8 .	4

(9)	29 . 16 . 8½ 75 . 18 . 9½	cwt. qrs. lbs. oz. drs. lb 7 . 2 . 15 . 6 . 12 6 . 3 . 24 . 10 . 14
(11)	\$2967.78 (12) 193 . 1 1898.89 97 . 1	07 (13) \$325.68
(14)	ac. ro. per. yds. ft. in. 297 . 1 . 23 2 . 1 . 101 189 . 2 . 28 . 24 . 2 . 127	c. yds. c. ft. c. in. (15) 278 . 3 . 1127 198 . 8 . 1478
(TE)	mls. fur. per. yds. ft. in. i117 · 0 · 27 · 5 · 1 · 9 89 · 7 · 38 · 4 · 2 · 11	degs. min. sec. 29 . 38 . 22 . 49 . 59
(18)	tons. cwt. qrs. lbs. oz. drs. 293 . 16 . 1 . 21 . 6 . 15 287 . 19 . 2 . 22 . 11 . 14	(19) 1209 . 1 . 1 . 1
(20)	bu. pk. gal. qt. 268 . 2 . 1 . 1 197 . 3 . 1 . 3	bu. pk. gal. qt. 19672 · 0 · 1 · 1 18998 · 3 · 1 · 3

COMPOUND MULTIPLICATION.

47. COMPOUND MULTIPLICATION is the method of finding the amount of any proposed compound number, that is, of any number composed of different denominations, but all of the same kind, when it is repeated a given number of times.

RULE. Place the multiplier under the lowest denomina-

tion of the multiplicand.

Multiply the number of the lowest denomination by the multiplier, and find the number of units of the next denomination contained in this first product; if there be a remainder, write it down; for the second product, multiply the number of the next denomination in the multiplicand by the multiplier, and after adding to it the above-mentioned number of units, proceed with the result as with the first product.

Carry this operation through with all the different denom-

inations of the multiplicand.

6x. 1. Multiply £1. 14s. 92d. by 11.

3q. \times 11 = 33q. = 8\frac{1}{2}d.; write down \frac{1}{2}d.; then 9d. \times 11 + 8d. = 99d. + 8d. = 107d. =8s.

14. 9\frac{2}{1} \text{ 11d.}; write down 11d.; then 14s. \times 11 + 8s.

11 \(\text{ = 162s.} = \frac{1}{2}s.; \text{ write down \frac{1}{2}ths.} + 8s. = 162s. = \frac{1}{2}s.; \text{ write down \frac{1}{2}ths.} + 8s. = 162s. = \frac{1}{2}s.; \text{ write down \frac{1}{2}ths.} + 8s. = 162s. = \frac{1}{2}s.; \text{ write down \frac{1}{2}ths.} + 8s. = \frac{1}{2}s. = \frac{1}{2}s. \text{ write down \frac{1}{2}ths.} + \frac{1}{2}s. \text{ write down \frac

Ex. 2. Multiply \$27.78 by 9.

18) 73 . 17 . 82

11

\$27.78

In this example we do the same as in Simple Multiplication, observing to place the point separating the dollar and centrin its proper place.

Ex XXIV.

-11	12 · 9 · 6 (2) 17 · 5 · 6 · 2 (3)	lbs. os. dwt. prs 18 . 6 . 5 . 10 4
	yds. qrs. nls. mls. tar. per. yds. ft. 27 · 3 · 3 (5) 27 · 7 · 26 · 4 · 2	(6) \$237.19 ————7
(7)	wt. qrs. lbs. oz. drs. mls. fur. per. yds. ft. 16 . 0 . 17 . 0 . 15 (8) 6 . 4 . 6 . 2 . 1	in. . 9 (9) \$609.93
	wks. dys. hrs. min. 7 · 5 · 18 · 16 11 (11, 7 · 3 ·	per. yds. ft. in. 29 . 20 . 1 108 12
(12)	£ s. d. lbs. os. drs. sc. 20 · 17 · 78 (13) 74 · 11 · 5 · 2	(14) bu. pk. qt.
(15)	dys, hrs. min. 4554 . 3 . 1 (17) 3	ys brs. min. sec. 65 · 5 · 48 · 57
	£ s. d. sc. ro. per.	

(19) 14 . 3 . 39

(20)

297.68

12

COMPOUND MULTIPLICATION. 59
bu. pk. gal. £ s. d. lbs. os. dwt. gr. 2782 . 2 . 1 (22) 70 . 0 . 111 (23) 18 . 3 . 14 . 5
\$\frac{24}{8}\$ \bigspace{\
mls. fur. per. yds. (27) 54 . 3 . 18 . 5
If the Multiplier be a composite number, ear of whose factors is less than 12, multiply by one of them, and the resulting product by another, and so on. The last product so obtained is the required product. Find the product of 2 cwt., 3 qr., 17 lbs. by 63.
The factors of 63 are 9 and 7. First, we multiply by 9 and the product we get by 7 which clearly is the same as multiplying 6 cwt., 3 qr., 17 lbs. by 63. Note. The same result is obtained, by taking the factor 7 first, and then the 9.
Ex. XXV.
(1) 56 . 2 . 9 (2) 27 . 6 . 9 (3) 19 . 11 . 4 28 (3) 4 . 4 . 4 (4) 28 (3) 19 . 11 . 4
lbs. dwt. grs. £ s. d. yds. qr. als. in (4) 21 . 13 . 17 (5) 17 . 11 . 8\frac{1}{4} (6) 27 . 1 . 3 . 2
cwt. qrs. lbs. oz. drs. 2 . 2 . 2 . 23 . 12 . 6 (8) 72 . 19 . 92 (9) \$209.18
c, yds, c, ft, c, in. lbs, oz. dwt. grs. (10) 17 . 2) . 57 (11) 3 . 8 . 15 . 13 (12) 42 . 10 . 94 84 49 88

ibs. os. drs.

74 . 11 . 5 . 2

(13) 5 . 17 . 39 . 20 120 84 lbs. oz. dwt, grs. 13 . 7 . 48 (15) 6 . 2 . 3 . 17 (16)5382 275

ac. ro. per. yds. ft. in. mls, fur. per. yds. ft. in 20 . 2 . 17 . 15 . 3 . 3 (18) 2.6.2.3.0.5 (17)64 375

bu. pk. gal. 2 . 6 . 81 (20)\$237.15 (21) 10 . 2 . 1 500 900 800

When the Multiplier is not a Composite number and larger than 12, the easiest method will be to solit the number into factors and parts:

Thus, $29 = 4 \times 7 + 1$; $19 = 6 \times 3 + 1$; $39 = 12 \times 3 + 3$.

Ex. 1. Multiply £2579. 0s. 0½ 1 by 2331.

2331 = 2000 + 300 + 30 + 1.

dys, hrs. min. sec.

 $=1000 \times 2 + 100 \times 3 + 10 \times 3 + 1$.

 $=10 \times 10 \times 10 \times 2 + 10 \times 10 \times 3 + 1 \times 3 + 1$

0 . 02 for 1 10 0 . 7½ for 10 25790 . 10 3 for 10×10 , or 100**25**7900 . 6 . 10 6 for 100×10 , or 1000. **2579003** .

) for 1000×2 , or 2000. 5158006 . 5.

ada 773700 . 18 . 9 for £257900. 6s. 3d. × 3, or tor 300. . 101 for £25790. 0s. 71d. × 3, or for 30. add 77370 . 1

0 . 0\frac{3}{4} for 1. add2579 . 5. $8\frac{1}{2}$ for 2000 + 300 + 30 + 1, or 2331. 6011656 .

Ex. XXVI.

lbs. os. ars. sc. grs. (6) 15 . 2 . 3 . 2 . 7 712

- (7) If a man gets \$2.25 a day, how much will that be in 209 days?
- (8) When wheat is selling for \$1.27 a bushel, how many dollars will a farmer get for a load of 52 bushels of wheat?
- (9) A butcher had an ox weighing 1625 lbs., live weight, at 6 cents a pound how much will he have to pay altogether?
- (10) A boiler-builder bought 29 boiler plates, each weighing 1 qr., 17 lbs., 8 oz., what was the weight of the whole of them?
- (11) If the Government of Ontario sells one hundred thousand acres of wild land for forty cents an acre, how many dollars will it obtain for the whole?

COMPOUND DIVISION.

48. COMPOUND DIVISION is the method of dividing a compound number, that is, a number composed of several denominations, but all of the same kind, into as many equal parts as the divisor contains units; and also of finding how often one compound number is contained in another of the same kind.

When the Divisor is a number either larger, or not larger than 12.

RULE. Place the numbers as in Simple Division; then find how often the divisor is contained in the highest denomination of the divinend; put this number down in the quotient; multiply as in Simple Division and subtract.

If there be a remainder, reduce that remainder to the next

inferior denomination, adding to it the number of that de remination in the dividend, and repeat the division.

Carry on this process through the whole dividend.

When the Divisor is less than 12.

Ex. 1. Divide £676. 19s. 9\frac{1}{2}d. by 11.

 $\begin{array}{lll} \frac{\pounds}{6166} & \frac{\$}{19} & \frac{d}{9\frac{1}{2}} & \pounds 676 \div 11 \text{ gives } \pounds 61 \text{ as a quotient} \\ \frac{\$}{61} & \frac{10}{10} & \frac{10\frac{1}{2}}{10} \text{ rem. } 8q. \div 11 \text{ gives } 10s. \text{ as a quotient and} \\ 9s. \text{ over; } 9s. + 9d. = 117d., 117d. \div 11 \text{ gives } 10d. \text{ as a quotient} \\ \text{and } 7d. \text{ over; } 7d. + 2q. = 30q., 30q. \div 11 \text{ gives } 2 \text{ as a quotient} \\ \text{and rem. } 8q. \end{array}$

When the Divisor is greater than 12 and not a Composite number, the work may stand thus:

Ex. 2. Divide £297. 4s. 8d. by 73.

By the Rule, \pounds . d.

73) 297 . 4 . 8 (£4

5

20 [add the 4s.]

73) 104 (1s. 73

 $\overline{31}$ 12 [add the 8d.]

73) 380 (5d.

365

15 15 We first subtract £4 taken 73 times, i.e. £292 from £297. 4s. 8d., there remains £5. 4s. 8d.

Now £5. 4s. 8d. = 104s. 8d., from this we subtract 1s. taken 73 times, i.e. 73s. from 104s., there remains 31s., ... there is 1s in quotient.

31s. 8d. = 380d., from this we subtract 5d. taken 73 times, i.e. 365d., there remains 15d. over ...£4. 1s. 5d. goes 73 times in

£297. 48. 8d., and 15d. over.

.. the Quotient is £4. 1s. 5d. and 15d. over.

When the Divisor is a Composite number greater than 12, we may divide as in Ex. 1, successively by each factor, and the last quotient so obtained will be the required quotient.

Ex. 3. Divide 975 mls., 3 fur., 24 per. by 56. Since $56 = 8 \times 7$, the work may stand thus:

8 | 975 . 3 . 24 7 | 121 . 7 . 18 17 . 3 . 14

Note. The same result would be obtained by dividing first by 7 and then by 8.

Ex. XXVIL

- (1) £278. 15s. 8d. ÷5.
- (2) 237 lbs., 5 oz., 6 dwt. ÷ 8
- (3) 217 mls., 5 fur., 16 per., 2 yds. ÷ %.
- (5) 865 lbs., 9 oz., 2 sc., 10 grs. ÷ 6.
- (6) £2078. 17s. 1¼d. ÷11.
- (7) 67 tens, 13 cwt., 1 qr., 17 lbs. ÷ 27.
- (8) 976 ac., 2 ro., 19 per., 25 yds. ÷ 56.
- (9) 612 cwt., 17 lbs., 2 drs. ÷ 705.
- (10) 8627 mls., 6 fur., 2 yds. ÷ 1247.
- (11) 612 bu., 2 pks., 1 gal. 2 qts. 96.
- (12) £2851. 16s. 43d. ÷54.
- (13) 247 lbs., 10 oz., 7 drs., 1 sc. ÷ 57.
- (14) 200 mls., 3 fur., 6 per. ÷ 211.
- (15) 416 ac., 3 ro., 19 per., 7 yds. ÷ 318.
- (16) 614 tons, 2 cwt., 3 qrs. ÷ 564.
- (17) 917 c. yds., 9 c. ft., 100 c. in. + 163.
 - \(\)\) 926 lbs., 5 oz., 3 drs., 2 sc. ÷ 212.
- 19) 3068 lbs., 8 dwt. ÷ 634.
- 20) £1914. 10s. 5d. ÷ 758.
- 211 £215. 12s. 6\d. \d. \d. 317.
- 22) 125 yrs., 127 dys., 16 hrs., 47 min. ÷ 397.
- 23° \$2267.84 ÷ 267.
- ? 4) \$5693.75 ÷ 425.
- (.25) If a person earned \$600 a year, how much is that a lay? How much per day, omitting the Sundays?
 - Note. A year = 365 days.
- (26) A farm of 57 acres is let for \$265.05, for a year; how such is that for an acre?
- (27) A farmer sold 57 bushels of wheat for \$65.55; how nucb did he get for one bushel?
- 123) The annual rent of a house is \$132; how much must be out aside every week so as to have the whole rent ready it he end of the year?

When the divisor and dividend are both compound numbers of the same kind.

RULE. Reduce both numbers to the same denomination. Divide as in Simple Division. The Quotient will be the answer required. Ex. 1. How often is 3s. 7d. contained in £8. 15s. 7d. ?

38.	7d. £8. 15s.	7d.
12	20	Reason for the Rule.
43	175	3s. 7d. = 43d., £8. 15s. 7d. = 2107d.;
	12	43d. subtracted 49 times from 2107d.
	2107	leaves no remainder.
	43)2107(49	

 $\frac{172}{387}$

... 49 times is the answer.

Ex. 2. I employ twice as many men as women, the wages of the former are 3s.6d. each, and of the latter 1s.10d. each per day. The weekly wages amount to £23. 17s. How many men, and how many women do I employ?

• £23. 17s. \div 6 = £3. 19s. 6d. =954d. = am's of daily wager Uaily wages of 2 men and 1 woman = 3s.6d. \times 2 + 1s. 10d. = 8s.10d. = 106d.

106)954(\$

954 ... there are 18 men and 9 women.

Ex. XXVIII.

Divide.

- (1) £684. 7s. 6d. by £76. 0s. 10d.
- (2) £171. 1s. 10½d. by £57. 0s. 7½d.
- (3) 9 lbs., 9 oz., 3 dwt., 12 grs. by 5 dwt. 9 grs.
- (4) 4 mls., 1 fur., 2 yds. by 1 ml., 3 fur., 2 ft.
- (5) 6 cwt. 2 grs. by 1 gr., 3 oz.
- (6) 12 lbs., 6 oz., 2 sc., by 1 lb., 6 oz., 2 sc., 10 grz.
- (7) 3 yds., 1 qr., 2 nls. by 1 qr., 2 nls.
- (S) 1 dy., 1 hr., 12 min. by 1 hr. 3 min.
- (9) 5 sq. per., 7 yds., 108 in. by 2 yds. 1 ft.
- (10) \$141.05 by \$2.17.
- (11) \$221 by \$2.21.

To reduce old Canadian to the Decimal Currency.

RULE. Multiply the pounds by 4, the product is dollars.

Multiply the shillings by 20, the product is cents. Reduce the pence to farthings and add the given farthings,

If my; then multiply by 5 and divide by 12, the quotient b cents.

The sum of these results is the answer required.

How many dollars and cents in £72. 19s. 91d.? £1 = \$4, ... £72 = \$72 \times 4 = \$288.00

 $1s. = 20 \text{ cts.} \dots 19s. = 19 \times 20 \text{ cts.} =$

91d. = 38q. $\therefore 38q$. $\times 5 \div 12 = 190 \div 12 =$ 1512 \$291,9518

Therefore the required answer is \$291.951\$.

Ex. XXIX.

How many dollars and cents in

- · (1) £25. 68. 3dL(2) £57. 198. 3d.
 - (3) £207. 17s. 8d. (4) £153, 18s, 5d.
 - (5) £217. 17s. 0d.(6)£319. 158. $7\frac{1}{2}d$.
 - (7) £612. 19s. 111d. £63. 9s. 9\$d. (8)

 - (9) £912. 12a. 6d. (10)£711. 58. 5\d.
 - £47. 7s. 9d. (11) £1117. 0s. 71d (12)
 - (13) £2017. 6s. £75. 9s. 81d. 8d.(14)
 - (15) £37. 18s. $7\frac{1}{2}d$. (16)£87. 13s. 9d.

50. To reduce dollars and cents to Halifax or old Canadian Currency.

RULE. Divide the dollars by 4, the quotient is pounds. If there is any remainder bring it to cents and add the given cents if any; then divide by 20, the quotient is shillings.

If any cents are left, multiply them by 3 and divide by 5; the quotient is pence. By arranging these several quotients properly, the required answer is obtained.

How many pounds, shillings and pence in \$1279.121? $$3 + 12\frac{1}{2}$ cts. = 300 cts. + 12\frac{1}{2} cts. = 4 | 1279. 121

 $312\frac{1}{2}$ cts.; $312\frac{1}{2}$ cts. $\div 20 = 158$. and £319 and \$3 over. 12½ cts. over; 12½ cts. $\times 3 \div 5 = 7½d$.

Therefore the answer is £319. 15s. 72d. The above is evidently correct; because \$4 = £1, 20 cts. = 12d., 5 cts. = 3d.

Ex. XXX

t low	many pounds,	shilling	gs and p	es in		
(1)	\$217.25	(2)	\$327.		(3)	£17.35
(4)	\$\$4.50	(5)	\$75.9		(v)	\$125.371
(7)	\$867.87}	(8)	\$1162.4		(9)	$$1393.62\frac{1}{2}$
(10)	\$1937.20	(11)	\$2220.21		(12)	\$3785.48

Ex. XXXI.

MISCELLANEOUS EXAMPLES.

PAPER I.

- (1) The population of the counties on the riverSt. Law rence in 1861 was as follows: Leeds, thirty-five thousan's seven hundred; Grenville, twenty-four thousand on nundred and ninety-one; Dundas, eighteen thousand seven nundred and seventy-seven; Stormont, eighteen thousand one hundred and twenty-nine; Glengarry twenty-one thousand one hundred and eighty-seven. Find the total population of these five counties.
- (2) By the .nsus of 1848, the population of Montreal was fift. Live thousand one hundred and forty-six; of Toronto, twenty-three thousand five hundred and three; of Hamilton, nine thousand eight hundred and eighty-nine; of Uttawa, six thousand two hundred and seventy-five; of Kingston, eight thousand three hundred and sixty-nine; of London, four thousand five hundred and eighty-four. Find the whole population of those cities.
- (3) Add, one hundred thousand, two hundred and twenty-nine thousand seven hundred and thirteen, fifty-eight thousand seven hundred and five, six hundred and twelve thousand five hundred and seventeen, nine hundred and ninety-nine thousand nine hundred and ninety-nine thousand nine hundred and ninety-nine, seven hundred and sixty-eight thousand three hundred and nine, fifty thousand and fif
- (4) Add, five thousand and five, seven thousand and eight een, seventeen thousand nine hundred and uffeen, twenty-eight thousand seven hundred and nineteen, nine thousand and twelve eight hundred and seven thousand five hundred and twelve hundred and seventeen thousand and seventeen, ninety-three thousand five hundred and two, twenty-three thousand five hundred and two, twenty-three thousand six hundred and seven

- (5) How many miles in 178006 inches?
- (6) In 1848 the value of the imports into Canada was \$3375180.20; in 1861, the value of the imports was \$43054836; the population at the former date was 1493332, at the latter 2506755. Find 1st., the value of the imports for each person in 1848 and in 1861, and 2nd., the difference between these values.

PAPER II.

- (1) What is the price of 818 bushels of wheat at 8s. 10½d. per bushel?
- (2) A farmer sold 67 bushels of wheat at \$1.62 a bushel bought a suit of clothes for \$18, 82 yards cotton at 13½ cents a yard, a stove for \$16. How much was left of the price of the wheat?
- (3) If a Government was to divide 72812 acres equally among 397 discharged soldiers, how much would each receive?
- (4) A farmer brought 160 bushels of wheat to mill when wheat was worth \$1.60 per bushel, and in exchange got 27 barrels of flour. How much was he charged for the flour per barrel?
- (5) A merchant has a piece of cloth containing 42½ yards, worth 6:, 6½d. a yard. How many dresses of 8½ yards each can be made out of it, and what will each cost?
- (6) A farmer sold in the Toronto market 618 barrels of flour for £1. 13s. 9d. per barrel; and bought 84 yards of cotton at 17 cents a yard, 5 lbs. tea at 3s. 9d. a lb., 2 tons of coal at £1. 15s. per ton, 8 sheep at £2. 21s. 9d. each, 15 head of cattle at £12. 19s. 9d. each. How much can he deposit in a bank allowing that he takes \$50 home with him?

PAPER III.

- (1) In one year there were coined in the British mint 203761 pounds of gold, value £9520732. 14s. 6d. Required the value of each pound?
- (2) Three persons bought a ship for \$63000; the first taking one share, the second three, and the third five. How much to they severally pay?
- (2. If a contribution of £50±. 13s. 6d. is made up in equal thares by 26 men, how much roust each give?
 - (4) What is the 29th part 10 ac., 2 ro., 7 per., 2 yds?

(5) Divide 300 tons, 15 cwt., 3 qrs., equally among 34) men. How much will each get?

(6) Soldiers marching in quick time, make 110 steps in a minute, each step 2 ft. 6 in. long. In what time would a company of soldiers march 20 miles in quick time, allowing half an hour for rest?

PAPER IV.

(1) Add together £6. 17s. 6d., \$30.27, £3. 19s *** ±d. \$75.83; giving your answer in decimal currency.

(2) Three boys went out together to fish, the first caught eight, the second as many and three more, the third as many as his two comrades all but one. How many did each of the last two boys catch?

(3) Three boys, Thomas, William, and Alexander, had between them 6 cents; Thomas had one, William two, and Alexander three; they bought fifty-four marbles with their

money. How many ought each boy to get?

(4) Four men went out one night to fish, borrowing both boat and nets. A man was to have 4 shares of the catch as often as the owner of the net was to have one; but, a man was to have only two shares as often as the owner of the boat had one. The catch was four barrels of herrings. What was each party's share in dozens; each barrel containing 38 dozens of herrings?

(5) It is found by observation that in each square inch of the human skin there are about 1000 pores; and the surface of the body of a middle sized man contains about 2304 square inches, or 16 square feet. Required, the number of pores in the surface of such a body, 999 being supposed to be con-

tained in each square inch?

(6) The sum of two numbers is 84889; the difference between them is SS9. What are the numbers?

PAPER V.

- (1) Find the product of 72678397 and 86073?
- (2) The quotient is 73697; the remainder 3687; the divisor 11689. Find the dividend?
- (3) The minuend is twenty-seven thousand eight hundred and twelve; the difference, fifteen thousand nine hundred and eight. Find the subtrahend?
- (4) There are seven addends all equal; their sum is eighty-nine thousand two hundred and sixty-four. Find one of them?

- (5) In the census of 1861, Rutland contained twenty-two thousand nine hundred and eighty-three inhabitants; Northamptonshire, ninety-six thousand eight hundred and one; Huntingdonshire, sixty-four thousand one hundred and eighty-three; Leicestershire, ninety-one thousand three hundred and eight; Nottinghamshire, one hundred and ninety thousand and sixty. What was the sum of the population of the above tive counties in 1861?
- (6) During the Crimean war, out of the French army there were killed in action or missing ten thousand two hundred and forty; drowned in a wreck, seven hundred and four: died of various diseases before the battle of Alma, eight thousand and eighty-four; died of disease before Sebastopol, four thousand three hundred and twelve; died in hospitals, &c., seventy-two thousand two hundred and forty-seven How many were lost altogether?

PAPER VI.

- (1) In 1861 the population of Edinburgh was 160302; of Glasgow, 168795 more than that of Edinburgh; of Aberdeen 71973; of Inverness, 24527 more than that of Aberdeen. What was the total population of all these places in 1861?
- (2) The paid up capital of each of the following Barks doing business in Ontario, is: of the Bark of Montreal, \$6000000; Bark of British North America, \$4866666; of Quebec Bark, \$1467750; of Bark of Toronto, \$800000; of Ontario Bark, \$1909640; of Royal Canadian Bark, \$590382 of Merchants' Bark, \$862033. Find the total amount of the paid up capital of the above named Barks?
- (3) The amount of revenue, from the named sources during 1866, was as follows: Customs, \$7328146.68; Excise, \$1888576.76; Postage, \$621936.42; Public-works, \$417474; Education, \$66554; Common School Fund, \$122142.77. Find the whole revenue from these sources?
- (4) A person has \$975. He buys a team for \$375, a wagon for \$82, a plough for \$16, a stove \$16, a reaping machine for \$153, 12 sheep for \$8 each, 2 cows \$25 each, 3 pigs \$6 a piece, pays his servantman 3 months' wages at \$20 a month, and the rest he lays out in flour at \$1.75 per 100 pounds. How many pounds of flour will he have?
 - (5) Among 635 men divide equally 86895 acres.
 - (6) How many inches in 10 mls., 3 per., 4 you!

SECTION III

CKEATEST COMMON MEASURE

51. A MEASURE! any given number is a number which will divide the given number exactly, i. e. without a remain

Thus, 2 is a measure of 6, because 2 is contained 3 times

exactly in 6.

52. A MULTIPLE of any given number is a number which contains it an exact number of times. Thus, 6 is a multiple

53. A COMMON MEASURE of two or more given numbers is a number which will divide each of the given numbers exactly. Thus, 3 is a common measure of 18, 27, and 36.

The GREATEST COMMON MEASURE (G. C. M.) of two or more given numbers, is the greatest number which will divide each of the given numbers exactly. Thus, 9 is the greatest com mon measure of 18, 27, and 36.

54. To find the greatest common measure of two numbers

RULE. Divide the greater number by the less.

If there be a remainder, divide the first divisor by it.

If there be still a remainder, divide the second divisor by this remainder, and so on; always dividing the last preced ing divisor by the last remainder, till nothing remains.

The last divisor will be the greatest common measure re-

wired.

Ex. Find the c. c. M. of 144 and 240.

By the Rule, 44)240(1

144

96) 144 (1 bringing down last divisor 144 tor a dividend

48 \ 96 (2 . . 48 : G. C. M. required.

Ex. XXXII.

Find the G. C. M. of

(1)	8 and 18.	(2)	6 and 15.	(3)	4 and 22.
(4)	16 and 28,	(5)	20 and 32.	(6)	24 and 39.
(7)	26 and 44.	(8)	3 0 and 42 .	(9)	36 and 56.
10)	46 and 116.	(11)	58 and 174.	(12)	315 and 378.
	200 1 200				

(12) S56 and 128. (14) 180 and 210. (15) 310 and 630.

(16) 1216 and 424. (17) 127 and 445. (18) 6408 and 7264 (19) 3042 and 3094. (20) 7040 and 7392.

(19) 3692 and 3094. (20) 7040 and 7392. (21) 1441 and 1572. (22) 46436 and 23025. (23) 21168 and 204624. (24) 97482 and 29579. (25) 828597 and 738140. (26) 326337 and 737800.

LEAST COMMOR MULTIPLE.

55. A COMMON MULTIPLE of two or more given numbers is a number which will contain each of the given numbers an exact number of times. Thus, 144 is a common multiple of 3, 9, 18, and 24.

The LEAST COMMON MULTIPLE (L. c. M.) of two more given numbers is the least number which will contain each of the given numbers an exact number of times. Thus, is the least common multiple of 3, 9, 18, and 24.

56. When the least common multiple of several numbers is required, the most convenient practical method is that given by the following Rule.

RULE. Arrange the numbers in a line from left to right, with a comma placed between every two.

Divide those numbers which have a common measure by

that common measure, and place the quotients so obtained and the undivided numbers in a line beneath, separated as before.

Proceed in the same way with the second line, and so on with those which follow, until a row of numbers is obtained in which there are no two numbers which have any common measure greater than unity.

Then the continued product of all the divisors and the sumbers in the last line will be the least common multiple

required.

Note. It will in general be found advantageous to begin

with the lowest prime number 2 as a divisor, and to repeat this as often as can be done; and then to proceed with the prime numbers 3, 5, &c., in the same way.

Ex. 1. Find the L. C. M. of 10, 12, and 16.

by the Rule,

2 10, 12, 16
$$10=2\times5$$
 12= $2\times2\times3$, $16=2\times2\times2\times2$
2 5, 6, 8 2×5 for 10.
5, 3, 4 $2\times5\times2\times3$ for 10 and 12.

 $2\times5\times2\times3\times2\times2$ for 10, 12, and 16.

 \therefore L C M. = 2 × 2 × 5 × 3 × 4 = 240.

Note. The process of finding the L. C. M. may often be shortened by striking out in the same line every number which exactly measures any other number in that line.

Ex. 2. Find the L. C. M. of 9, 14, 16, 18, 24, 36, and 38.

19,14,16,18,24,36,38 8, 12, 18, 19 6. 9, 19 **3.** 9. 19

Every multiple of 36 must be a multiple of 9 and of 18; ... strike out 9 and 18: for the · same reason strike out 3 in the 4th line.

8, 9, and 12.

(8) 6, 33, 24, and 32. 7, 8, 9, 10, and 12.

24, 56, and 84.

2, 5, 45, 15 and 25.

15, 20, 24, 21, and 33

(4) 20, 28, and 36.

 $2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 19 = 1915$

Ex. XXXIII.

(2)

(6)

(10)

(12)

(14)

Fund the L. C. M. of

- 2, 4, and 10. (1)
- 12, 16, and 18. (3)
- 16, 24. and 30. (5)
- (7) 15, 25, and 105.
- 7, 21, 6, 14, and 25. (9)
- 24, 28, 36, 22, and 16. (11)
- 9, 4, 8, 15, and 27. (13)

 - - (15) 4, 5, 7, 8, 15, 21, and 30.
 - 2, 7, 9, 13, 15, 52, and 63. (16)
 - (17)3, 7, 11, 77, and 198.
 - (18) 100, 56, 35, 125, and 150.
 - (19)22, 55, 19, 15, 95, and 133.
 - (20) 48, 64, 27, 33, 110 and 165

SECTION IV.

FRACTIONS.

57. Let unity be represented by the line AB, which we

will consider to be one yard in length.

Suppose AB to be divided into 3 equal parts AD, 1 E, EB; then one of such parts AD A D E B F G C is a foot or one-third part of the variable in the content of the content

If another equal portion BF of a second yard BC, divided in the same manner as the first, be added, then AF, or four

feet, is denoted thus \{\frac{1}{3}\}; and so on.

Such expressions, representing any number of the equal parts of a unit, i. e. of a quantity which is denoted by 1, are called Broken Numbers or Fractions.

- 58. A Fraction denotes one or more of the equal parts of a unit; it is expressed by two numbers placed one above the other with a line between them; the lower number is called the Denominator (Dept.), and shews into how many equal parts the unit is divided; the upper is called the Numerator (Num.), and shews how many of such are taken to form the fraction.
- 59. A Fraction also represents the quotient of the number by the den'.

Thus $\frac{2}{3} = 2 \div 3$; for we obtain the same result, whether

- we divide one unit, AB or 1 yard, into three equal parts AD, DE, EB, each = 1 ft. or 12 in., and take two of such parts AE represented by $\frac{2}{3}$), = 12 in. \times 2 = 24 in., or divide 2 units, AC or 2 yards, into three equal parts, AE, EF, FC, each = 2 ft. or 24 in., and take one of such parts AE; which is equal to $\frac{1}{3}$ rd part of AC or 2 units, or = $2\div 3$. Hence $\frac{2}{3}$ and $2\div 3$ have the same meaning.
- 60. When fractions are denoted in the manner above explained, they are called VULGAR FRACTIONS.

Fractions, whose den". are composed of 10, or of 16 multiplied by itself any number of times, are called DECI-MAL FRACTIONS, OF DECIMALS.

VULGAR FRACTIONS.

- 62. In treating of the subject of Vulgar Fractions, it is sual to make the following distinctions:
- (1) A PROPER FRACTION is one whose num'. is less than the den'.; thus 3, \$, 7, are proper fractions.
- (2) An IMPROPER FRACTION is one whose num', is equal to or greater than the den' .: thus, &, &, & are improper fractions.
- (3) A SIMPLE FRACTION is one whose num'. and den'. are simple integer numbers; thus, 1, 3 are simple fractions.
- (4) A MIXED NUMBER is composed of a whole number and a fraction; thus $5\frac{1}{8}$, $7\frac{3}{4}$ are mixed numbers, representing respectively 5 units, together with 1th of a unit; and 7 units, together with \$ths of a unit.
- (5) A COMPOUND FRACTION is a fraction of a fraction; thus 1 of 3, 5 of 7 of , are compound fractions.
- (6) A COMPLEX PRACTION is one which is either a fraction of a mixed number in one or both terms of the fraction: thus, $\frac{3}{2}$, $\frac{2\frac{1}{2}}{3}$, $\frac{3}{4\frac{2}{8}}$, $\frac{2\frac{1}{7}}{5\frac{1}{8}}$, $\frac{2}{8}$ of $\frac{1}{2}$ are complex fractions.

- 63. It is clear from what has been said, that every whole number or integer may be considered as a fraction whose den'. is 1; thus, 5 = 5, for the unit is divided into 1 part comprising the whole unit and 5 of such parts, that is 5 nnits, are taken.
 - 64. To multiply a fraction by a whole number.

RULE. Multiply the numerator by the whole number. For in & and \$, the unit is divided into

5 equal parts, and twice as many parts are $\frac{1}{5} \times 2 = \frac{1}{5} = \frac{5}{5}$ taken in $\frac{2}{5}$ as are *aken in $\frac{2}{5}$.

Ex. XXXIV.

Multiply (1) ? and ? each separately by 2, 3, 5, 7, 9, and 12: and (2) 3 and 107 each separately by 6 8, 11, 106 and 157.

65. To divide a fraction by a whole number.

RULE. Multiply the denominator by the whole number.

 $\frac{2}{5} \div 2 = \frac{2}{5 \times 2} = \frac{2}{10}$ The value of each part in $\frac{2}{5}$ is twice as large as the value of each part in $\frac{2}{5}$ is twice as large as $\frac{2}{10}$, or $\frac{2}{5} \div 2 = \frac{2}{10}$.

Ex. XXXV.

Divide (1) $\frac{3}{4}$ and $\frac{7}{5}$ each separately by 2, 3, 5, 6, 9, and 12; and (2) $\frac{1}{2}$ and $\frac{7}{2}$ each separately by 3, 5, 11, 56, and 100.

66. If the numerator and denominator of a fraction be both multiplied, or both divided, by the same number, the value of the fraction will not be altered.

 $\frac{3}{4} = \frac{3 \times 2}{4 \times 2} = \frac{6}{8}$ Since $8 = 4 \times 2$, two of the parts in $\frac{9}{4}$ are equivalent to one of the parts in $\frac{3}{4}$; but since $6 = 3 \times 2$, there are twice as many parts taken in $\frac{9}{4}$ as there are in $\frac{3}{4}$, therefore $\frac{3}{4} = \frac{9}{8}$. In figure, Art. 57, AE represents either $\frac{1}{4}$ rd or $\frac{9}{4}$ ths of AC.

67. Hence it follows that a whole number may be converted into a vulgar fraction with any required denr., by multiplying the number by the required denr. for the numr. of the fraction, and placing the required denr. underneath.

For $5 = \frac{5}{1}$, and to convert it into a fraction with a den, 6

or 17, we have $5 = \frac{5}{1} = \frac{5 \times 6}{1 \times 6} = \frac{30}{6}$; also $5 = \frac{5}{1} = \frac{5 \times 17}{1 \times 17} = \frac{85}{17}$

Ex. XXXVI.

Reduce (1) 3, 5, 8, 15, to fractions with den. 2, 9, and 13; and (2) 9, 12, 17, 37, to fractions with den. 8, 10, and 57.

 To represent on improper fraction as a whole or mixed number,

RULE. Divide the numerator by the denominator.

If there be no remainder, the quotient will be a whole number.

If there be a remainder, put down the quotient as the integral part, and the remainder as the num'. of the fractional part, and the given den'. as the den'. of the fractional part.

Ex. Reduce $\frac{24}{4}$ and $\frac{24}{5}$ to whole or mixed numbers.

By the Rule, $\frac{24}{4} = 6$. For $\frac{24}{4} = \frac{4 \times 6}{4 \times 1} = \frac{6}{1}$ (Art. 66) = 6. $\frac{24}{5} = 4\frac{4}{5}$. For $\frac{24}{5} = \frac{20+4}{5} = \frac{20}{5} + \frac{4}{5} = 4 + \frac{4}{5} = 4\frac{4}{5}$.

Ex. XXXVII.

Express the following improper fractions as mixed or whole numbers:

To reduce a mixed number to an improper fraction.

RULE. Multiply the whole number or integer by the denominator of the fraction, and to the product add the numerator of the fractional part.

The result will be the required num'., and the den'. of the

fractional part the required den'.

Ex. Convert 33 into an improper fraction. By the Rule,

$$3\frac{3}{4} = \frac{3 \times 4 + 3}{4} = \frac{12 + 3}{4} = \frac{15}{4}.$$
For $3\frac{3}{4} = \frac{3}{1} + \frac{3}{4} = \frac{3 \times 4}{1 \times 4} + \frac{3}{4} = \frac{12}{4} + \frac{3}{4} = \frac{12 + 3}{4} = \frac{15}{4}.$

Ex. XXXVIII.

Reduce the following mixed numbers to improper fractions:

(10)
$$900\frac{3}{15}$$
, (11) $5\frac{2}{880}$, (12) $53\frac{2}{3}$, (13) $21\frac{2}{1860}$, (14) $148\frac{2}{3}$, (15) $13\frac{1}{3}\frac{2}{8}$, (16) $25\frac{2}{3}\frac{2}{3}$, (17) $197\frac{2}{3}\frac{2}{3}$

To reduce a compound fraction to its equivalent simple fraction.

RULE. Multiply the several numerators together for the numerator of the simple fraction, and the several denominators togeth ir for its denominator.

Ex. 1. Convert & of & into a simple fraction.

By the Kule,

$$\frac{2}{3}$$
 of $\frac{5}{6} = \frac{2 \times 5}{3 \times 6} = \frac{10}{18}$

For
$$\frac{2}{3}$$
 of $\frac{5}{6}$ = twice $\frac{1}{3}$ of $\frac{5}{6}$ = twice $\frac{5}{6} \div 3$ = twice $\frac{5}{18}$ (Art. 6a)

$$=\frac{5\times2}{18}$$
 (Art. 64) $=\frac{10}{18}$.

Note 1. Before applying the above Rule, mixed numbers must be reduced to improper fractions.

Note 2. In reducing compound fractions to simple ones, we may strike out from any num. and any den. such factors as are common to both; for this is in fact simply dividing the num. and den. of a fraction by the same number. 'Art. 66.)

Fix. 2. Reduce & of 21 of 11 to a simple fraction.

$$\frac{3}{5} \ ^{16} 2_{12} \ \text{of} \ 1_{15} = \frac{3}{5} \ \text{of} \ \frac{25}{12} \ \text{of} \ \frac{16}{15} = \frac{3 \times (5 \times 5) \times (4 \times 4)}{5 \times (3 \times 4) \times (3 \times 5)}$$

$$=\frac{3\times5\times5\times5\times4}{5\times5\times4}\cdot3\times5=\frac{4}{3}$$
 dividing num and den. by 3, 5, 5, 4.

factors commun to both.

Ex. XXXIX.

Reduce the following compound fractions to simple ones

(1)
$$\frac{2}{4}$$
 of $\frac{4}{5}$. (2) $\frac{4}{5}$ $\frac{6}{19}$. (3) $\frac{3}{7}$ or $\frac{3}{19}$. (4) $\frac{3}{19}$ of $\frac{3}{17}$. (5) $\frac{5}{8}$ of $\frac{3}{2}$. (6) $\frac{3}{8}$ of $\frac{1}{4}$.

71. A fraction is in its LOWEST TERMS, when its numerator and denominator are PRIME to each other.

To reduce a fraction to its lonnest terms

Rule. Divide the numerator and denominator by the greatest common measure.

Ex. Reduce 176 to its lowest terms.

(2)

By the Rule, find the G. C. M. of 176 and 484.

176) 484 (2 352

(1)

$$\begin{array}{c|c}
\hline
132 \\
132 \\
132 \\
\hline
44) 132 (3) \\
132
\end{array}$$
 For $\frac{176}{484} = \frac{44 \times 4}{44 \times 11} = \frac{4}{11}$ (Art. 66.)

44)
$$176$$
 (4 44) 484 (11 44) 44 ... fraction in its lowest terms = $\frac{4}{1}$

Ex. XL.

Reduce each of the following fractions to its lowest term

(3)

21.

3 g.

(4)

73. To reduce fractions to equivalent ones with a comme denominator.

Rule. Find the least common multiple of the denoming tors; this will be the common denominator.

Then divide the common multiple so found by the denominator of each fraction, and multiply each quotient s found into the numerator of the fraction which belongs t it for the new numerator of that fraction.

Note. If the given fractions be in their lowest terms, the above rules will reduce them to others having the least common denr.: if the least common denr. be required, the give fractions should be reduced to their lowest terms before the rule is applied.

Ex. 1. Reduce $\frac{1}{12}$, $\frac{17}{24}$, and $\frac{31}{38}$ to equivalent fractions wit a common denominator.

By the Rale, 12
$$\frac{12}{2}$$
, $\frac{24,36}{3}$. L. c. M. = $12 \times 2 \times 3 = 72$

the fractions become = $\frac{11 \times 6}{12 \times 6} = \frac{66}{72}$ (since $72 \div 12 = 6$), and $\frac{17 \times 3}{24 \times 3} = \frac{51}{72}$ (since $72 \div 24 = 3$),

and
$$\frac{31 \times 2}{36 \times 2} = \frac{62}{72}$$
 (since $7^{\circ} = 36 = 2$),

the required fractions are \$3, 51, and \$5.

Note. If the denra, have no common measure, the work Il be more quickly done, by multiplying each num. into all e den"., except its own, for a new num'. for each fraction, d all the denra, together for the common denr.

Ex. 2. Reduce 2, 3, and 5 to equivalent fractions with a mmon den'.

1.. c. M. of the den^m. = $3 \times 5 \times 7 = 105$.

fractus. =
$$\frac{2 \times 5 \times 7}{3 \times 5 \times 7}$$
, $\frac{3 \times 3 \times 7}{5 \times 3 \times 7}$, $\frac{5 \times 3 \times 5}{7 \times 3 \times 5}$; or $\frac{70}{105}$, $\frac{63}{105}$, $\frac{75}{105}$

Ex. XLI.

Reduce the fractions in each of the following sets to egriv ent fractions, naving the least common dent. :

- (1) $\frac{3}{4}$ and $\frac{5}{6}$. (2) $\frac{3}{4}$ and $\frac{2}{3}$. (3) $\frac{3}{4}$ and $\frac{7}{3}$.

- (4) $\frac{3}{7}$ and $\frac{5}{9}$. (5) $\frac{11}{16}$ and $\frac{21}{4}$. (6) $\frac{11}{12}$ and $\frac{27}{49}$.
- (7) $\frac{7}{10}$ and $\frac{188}{200}$. (8) $\frac{113}{280}$ and $\frac{527}{960}$. (9) $\frac{4}{5}$, $\frac{11}{12}$, and $\frac{4}{34}$.
- (10) $\frac{3}{13}$, $\frac{8}{21}$, and $\frac{5}{2}$. (11) $\frac{7}{13}$, $\frac{1}{21}$, and $\frac{23}{35}$. (12) $\frac{7}{9}$, $\frac{13}{11}$, $\frac{13}{15}$, and $\frac{9}{17}$. (13) $\frac{13}{14}$, $\frac{3}{35}$, $\frac{1}{15}$, and $\frac{46}{91}$.
- (14) $\frac{7}{12}$, $\frac{17}{30}$, $\frac{18}{18}$, $\frac{15}{20}$, and $\frac{7}{15}$. (15) $\frac{13}{26}$, $\frac{27}{32}$, $\frac{7}{12}$, and $\frac{15}{18}$.
- (16) $\frac{9}{14}$, $\frac{13}{18}$, $\frac{7}{29}$, $\frac{18}{35}$, $\frac{23}{42}$, and $\frac{63}{69}$. (17) 2, 4, 3, and 14.
- (17) $\frac{2}{3}$, $\frac{4}{5}$, $\frac{2}{3}$, and $\frac{1}{15}$. (18) $\frac{2}{5}$, $\frac{6}{5}$, $\frac{7}{5}$, and $\frac{9}{10}$. (20) $\frac{2}{3}$, $\frac{4}{5}$, $\frac{1}{2}$, and $\frac{9}{11}$.

74. Whenever a comparison has to be made between fracons, in respect of their magnitudes, they must be reduced to uivalent ones with a common den'.; because then we shall we the unit divided, in the case of each fraction so obined, into the same number of equal parts; and the reective num". will shew us how many of such parts are taken in each case, or which is the greatest fraction, which the next, and so on.

Ex. Which is the greatest, and which the least of the fractions $\frac{11 \times 4}{5 \times 9}$, $\frac{12 \times 3}{4 \times 10}$, $\frac{10 \times 5}{6 \times 8}$, $\frac{11 + 4}{5 + 9}$.

The fract^a in their lowest terms are $\frac{44}{45}$, $\frac{9}{10}$, $\frac{25}{24}$ and $\frac{15}{14}$

L. C. M. of the denr. =2520.

.. the fractions become $\frac{44 \times 56}{45 \times 56}$ or $\frac{2464}{2520}$, $\frac{9 \times 252}{10 \times 252}$ or $\frac{2263}{2520}$, $\frac{25 \times 105}{24 \times 105}$ or $\frac{2625}{2520}$, $\frac{15 \times 180}{14 \times 180}$ or $\frac{2700}{2520}$.

 $\therefore \frac{11+4}{5+9} \text{ is the greatest, and } \frac{12\times3}{4\times10} \text{ the least.}$

Ex. XLIL

Compare the values of

- (1) \(\frac{2}{3}\) and \(\frac{4}{5}\). (2) \(\frac{7}{9}\) and \(\frac{4}{12}\). (3) \(\frac{17}{24}\) and \(\frac{19}{26}\).
- (4) $\frac{7}{9}$, $\frac{5}{8}$, and $\frac{11}{14}$. (5) $\frac{15}{42}$, $\frac{22}{49}$, and $\frac{45}{83}$. (6) $\frac{53}{80}$, $\frac{63}{90}$, and $\frac{57}{84}$.
- (7) $\frac{3}{7}$ of $\frac{5}{9}$, $\frac{1}{2}$ of $\frac{3}{7}$, and $7\frac{3}{8}$. (8) $\frac{11}{15}$, $\frac{17}{20}$, $\frac{21}{25}$, and $\frac{29}{30}$.
- (9) $\frac{e}{11}$ of $\frac{1}{16}$ of $7\frac{1}{4}$, $\frac{41}{2}$ of $\frac{2}{3}$, $\frac{1}{5}$, of $7\frac{1}{2}$ of 11, and $\frac{2}{5}$ of $4\frac{1}{6}$ of $\frac{1}{5}$ of 14, $\frac{7}{1}$.
- (10) $\frac{684}{765}$ of $\frac{67}{171}$, $\frac{15}{17}$ of 64 of $\frac{11}{50}$ of 14 and 15 of 14 of 156 of $\frac{1}{2}$ of 12.

Which is the greater.

- (11) 5 of a yd. or 5 of a yd.
- 12) 1 of a yd. or 3 of a yd.
 - 13) 17 of 3 of 13 of 32 of a loaf, or 5 of 170 of 23 loaves?

ADDITION OF VULGAR FLACTIONS.

75. Rule. reduce the fractions to equivalent ones with the least common denominator.

Add all the new numerators together, and under their sum write the common denominator.

Ex. 1. Find the sum of \(\frac{1}{2}\), \(\frac{1}{2}\), and \(\frac{1}{2}\). By the Rule.

The L. O. M. of the denn. is 24.

fracton, become
$$\frac{1 \times 12}{2 \times 12}$$
 or $\frac{12}{24} \frac{1 \times 8}{3 \times 8}$ or $\frac{8}{24} \frac{5 \times 3}{8 \times 3}$ or $\frac{13}{24}$

... Their sum =
$$\frac{12+8+15}{24} = \frac{35}{24} = 1\frac{11}{24}$$
.

Reason for the Rule. In each of the equivalent fractions unity is divided into 24 equal parts, and 12, 8, and 15, of such parts are taken, therefore their sum must be 12 + 8 + 15, or 35 of such parts, and will be represented by the fraction $\frac{3}{2}$, or by $1\frac{1}{2}$.

Note 1. If the sum of the fractions be a fraction which is not in its lowest terms, reduce it to its lowest terms; and if the result be an improper fraction, then reduce it to a whole

or mixed number: thus $\frac{147}{105} = \frac{49}{35} = l_{\frac{14}{55}}$: the same remark applies to all results in Vulgar Fractions.

Note 2. Before applying the Rule, reduce all fractions to their lowest terms, improper fractions to whole or mixed numbers, and compound fractions to simple ones.

Note 3. If any of the given numbers be whole or mixed numbers; the whole numbers may be added together as in simple addition, and the fractional parts by the Rule given above.

Ex. 2. Find the sum of $3\frac{5}{2}$, $3\frac{1}{6}$, $2\frac{7}{16}$, and $\frac{3}{4}$ of $3\frac{2}{3}$. $\frac{3}{4}$ of $3\frac{2}{3} = \frac{3}{4}$ of $\frac{1}{3} = \frac{1}{4} = 2\frac{3}{4}$;

 $\frac{4}{4}$ of $\frac{3}{3} - \frac{4}{4}$ of $\frac{1}{3} - \frac{7}{4} - \frac{24}{6}$; ... sum of fractions = $3 + 3 + 2 + 2 + \frac{5}{12} + \frac{1}{6} + \frac{3}{16} + \frac{3}{4}$,

=10+
$$\frac{5\times4}{12\times4}$$
+ $\frac{1\times8}{6\times8}$ + $\frac{7\times3}{16\times3}$ + $\frac{3\times12}{4\times12}$ (since L. c. m of den^{re}. =48)

$$= 10 + \frac{20 + 8 + 21 + 36}{48} = 10 + \frac{85}{48} = 10 + 1\frac{37}{48} = 11\frac{37}{48}.$$

76. The sign () or {}, called BRACKET, enclosing numbers within it, and the sign called a VINCULUM, placed over two or more numbers, denotes that all the numbers within the bracket or under the vinculum are equally affected by anything outside the bracket or vinculum, thus (2 + 3) apples or 2 + 3 apples would mean 2 : les + 3 apples, or 5 apples.

whereas 2 + 3 apples would mean 2 units + 3 apples

Again
$$\frac{1}{2} + \frac{1}{3}$$
 of $(2 + \frac{1}{2}) = \frac{1}{2} + \frac{1}{3}$ of $\frac{5}{2} = \frac{1}{2} + \frac{5}{6} = \frac{7}{6} + \frac{7}{6} = \frac{7}{6} = \frac{1}{4} = \frac{1}{4}$.

$$(\frac{1}{2} + \frac{1}{3})$$
 of $(2 + \frac{1}{2}) = (\frac{7}{6} + \frac{2}{6})$ of $(\frac{1}{2} + \frac{1}{2}) = (\frac{5}{6} + \frac{2}{6})$ of $(\frac{1}{2} + \frac{1}{2})$ of $(\frac{1}{2} + \frac{1}{3})$ of $(\frac{1}{2} + \frac{1}{2})$ of $(\frac{1}{$

Ex. XLIIL

Find the sum of.

(1) \(\frac{1}{3}\) and \(\frac{2}{4}\). (2) \(\frac{3}{4}\) and \(\frac{3}{3}\). (3) 3 and \(\frac{1}{3}\).

(4) \$\frac{3}{4}\$ and \$\frac{5}{6}\$. (5) \$\frac{5}{12}\$ and \$\frac{7}{15}\$. (6) \$\frac{3}{4}\$ and \$\frac{7}{12}\$.

(7) $\frac{3}{5}$ and $\frac{3}{11}$. (8) $\frac{3}{5}$ and $\frac{1}{14}$. (9) $\frac{1}{30}$ and $\frac{2}{45}$.

(10) 11 and 11. (11) 72 and 8. (12) 11 of 21 and 6

(13) $\frac{3}{4}$, $\frac{4}{5}$, and $\frac{7}{12}$. (14) $2\frac{3}{5}$, $\frac{5}{5}$, and $3\frac{1}{12}$.

(15) 6_{1}^{3} , $\frac{1}{3}$ of 1_{7}^{3} , and 2_{7}^{3} . (16) $9_{\frac{1}{2}}$ of $2_{\frac{1}{3}}$, $\frac{1}{1_{\frac{3}{3}}}$, and $\frac{1}{1_{7}}$. (17) $\frac{2}{3}$, $\frac{2}{3}$, and $\frac{1}{3}$ of $(1 + 1_{\frac{1}{3}})$.

Find the value of,

(18) $\frac{1}{2} + \frac{2}{3} + \frac{7}{4} + \frac{1}{4}$. (19) $2\frac{1}{2} + 3\frac{1}{3} + 4\frac{1}{4} \div 5\frac{1}{6}$.

(20) $5\frac{7}{24} + 13\frac{5}{32} + \frac{49}{2} + 2\frac{23}{65}$. (21) $4\frac{5}{2} + \frac{7}{15} + 16\frac{5}{25} + 25\frac{1}{25}$.

(22) $3\frac{2}{5} + 16\frac{7}{5} + 7\frac{5}{12} + \frac{2}{5}$ of $3\frac{3}{5}$.

(23) $(2\frac{3}{4} + 3\frac{2}{3})$ of $2\frac{5}{11} + 3\frac{1}{5}$ of $(16\frac{5}{8} + 3\frac{1}{4}) + 1\frac{2}{3}$ of 11 of $2\frac{1}{22}$.

(24) A gentleman gave £2 $\frac{1}{3}$ to A, £ $\frac{1}{2}$ $\frac{3}{4}$ to B, £3 $\frac{1}{12}$ to C, £4 $\frac{1}{12}$ to D, and £ $\frac{2}{12}$ $\frac{3}{4}$ to E. How much did he give away?

(25) A man ate $\frac{3}{10}$ of a 4 lb. loaf on Mon., $\frac{5}{12}$ of a similar loaf on Tues., $\frac{7}{15}$ on Wed., $\frac{2}{20}$ on Thurs., $\frac{1}{27}$ on Frid., and on Sat. and Sun. as much as on Mon., Tues., and Wed. How many lbs. of bread did he eat during the week?

SUBTRACTION.

77. Rule. Reduce the fractions to equivalent ones having the least common denominator.

Take the difference of the new numerators, and place the common denominator underneath.

Ex. 1. Subtract & from &.

By the Rule,

The fractor become $\frac{1 \times 4}{2 \times 4}$ or $\frac{4}{8}$, and $\frac{5}{8}$

their difference $=\frac{5-4}{9}=\frac{1}{9}$.

Reason for the Rule. In each of the equivalent fractions, whity is divided into 8 equal parts, and there are 5 and 4 parts respectively taken, ... the difference must be 5—4, or 1 of such parts, which is represented by $\frac{1}{2}$.

Note 1. Before applying the Rule, reduce fractions to their lowest terms, improper fractions to whole or mixed numbers, and compound fractions to simple ones.

Note 2. If either of the given fractions be a whole or mixed number, it is most convenient to take separately the difference of the integral parts and that of the fractional parts, and then add the two results together, as in the following examples.

Ex. 3. Find the difference between 23 and 41.

§ is greater than 1, and cannot be taken from it,

. we write $4\frac{1}{4}$ thus $(3+1+\frac{1}{4})$, or $(3+\frac{5}{4})$ then diff. $=(3\frac{5}{4})-(2+\frac{5}{8})=(3-2)+(\frac{5}{4}-\frac{3}{8})=1+\frac{1}{4}-\frac{3}{8}$.

Ex. XLIV.

Find the diff. between

- (1) \(\frac{1}{4}\) and \(\frac{1}{5}\). (2) \(\frac{1}{2}\) and \(\frac{1}{8}\). (3) \(\frac{2}{4}\) and \(\frac{5}{12}\).
- (4) $\frac{13}{18}$ and $\frac{19}{24}$. (5) $3\frac{2}{3}$ and $2\frac{1}{6}$. (6) 7 and $2\frac{9}{10}$.
- (7) 1012 and 82. (8) 173 and 138. (9) 125 and 3.
- (10) 47 and 217. (11) 157 and 78. (12) 2018 and 888.
- (13) A boy ate \(\frac{3}{6} \) of a cake, how much less did he leave than he ate?
- (14) What number added (1) to $\frac{1}{2}$ will make $\frac{1}{2}$? and (2) to $\frac{1}{2}$ will make $\frac{1}{2}$?
- (15) I copied down by mistage §d. instead of \$d., what
- 78. Examples involving both Addition and Subtraction of Vulgar Fractions.

Ex. 1. Find the value of
$$5\frac{1}{4} - 2\frac{1}{2} + \frac{1}{8} + 2\frac{1}{4} - \frac{1}{16}$$
.
Value = $(5 - 2 + 2) + (\frac{1}{4} - \frac{1}{2} + \frac{1}{8} + \frac{1}{4} - \frac{1}{16})$.

$$= 5 + \frac{4 - 8 + 2 + 4 - 1}{16} = 5 + 1 = 5 + 1$$

Ex. 2. Find the value of $\frac{1}{9} + \frac{1}{3}$ of $(2 - \frac{1}{3}) - \frac{1}{3}$ of $2\frac{1}{3} + \frac{1}{3}$.

Value=
$$\frac{1}{8} + \frac{1}{8}$$
 of $\left(\frac{6-1}{3}\right) - \frac{1}{8}$ of $\frac{5}{2} + \frac{1}{2} - \frac{1}{4}$ of $\left(\frac{5}{8} - \frac{5}{8}\right)$
= $\frac{1}{3} + \frac{1}{3}$ of $\frac{5}{8} - \frac{1}{8}$ of $\frac{5}{2} + \frac{1}{2} - \frac{1}{4}$ of $\frac{2}{8} = \frac{5}{8} + \frac{5}{8} - \frac{5}{12} + \frac{1}{2} + \frac{1}{4}$
= $1 - \frac{5}{12} + \frac{1}{2} - \frac{1}{12} = 1 + \frac{1}{2} - \frac{1}{12} = 1 + \frac{1}{12} - \frac{1}{12} - \frac{1}{12}$
= $1 + \frac{6-6}{12} - \frac{1}{12} = \frac{6-6}{12} - \frac{1}{12} = \frac{1}{12}$

Ex. XLV.

Find the value of

- (1) $\frac{1}{6} \div 2\frac{1}{7} + 13\frac{3}{10} 3\frac{3}{70}$. (2) $\frac{1}{4} \frac{3}{8} \div \frac{4}{7} \frac{12}{8}$.
- (3) $12\frac{1}{17} \frac{21}{34} + 7\frac{1}{5}\frac{9}{17} \frac{1}{3}$ of $\frac{1}{17} + \frac{2}{5}$ of $3\frac{2}{3}$.
- (4) $(165 3\frac{1}{2})$ of $3\frac{1}{6} 165 + 3\frac{1}{2}$ of $3\frac{1}{6}$.
- (5) $6\frac{1}{4} + \frac{7}{12}$ of $\frac{9}{14}$ of $3\frac{1}{3} \frac{45}{80} 5\frac{3}{4}$.
- (6) $6\frac{1}{4} + \frac{7}{12}$ of $\frac{9}{14}$ of $(3\frac{1}{3} \frac{45}{60}) 5\frac{3}{4}$.
- (7) What number must be added to the sum of $\frac{1}{2}$, $\frac{1}{2}$, and $\frac{1}{2}$, to make $5\frac{3}{120}$?
- (8) A bought $\frac{3}{4}$ of a cheese, and sold $\frac{1}{3}$ of his purchase to B, $\frac{1}{3}$ of what then remained to C, $\frac{1}{3}$ of what then remained to D; what part of the cheese had B, C, and D, and what part had A, after the sales?

MULTIPLICATION.

79. Rule. Multiply all the numerators together for a new numerator, and all the denominators together for a new denominator.

Ex. 1. Multiply $\frac{2}{3}$ by $\frac{4}{7}$.

By the Rule, $\frac{2}{3}$ multiplied by $\frac{5}{7} = \frac{2 \times 6}{3 \times 7} = \frac{10}{12}$.

Reason for the Rule.

Rule, $\frac{2}{3}$ multiplied by 5, gives $\frac{2}{3}$ (Art 64.)

But $\frac{1}{3}$ must be 7 times

too large, since $\frac{5}{7}$ is one-seventh part of 5. Therefore $\frac{1}{3}$ must

be divided by 7, and $\frac{1}{3}$ $\frac{9}{3}$ $\frac{1}{3}$ $\frac{1}{3}$ (Art. 65.)

Note 1. The same reasoning will apply, whatever be the number of fractions which have to be multiplied together.

Note 2. Before applying the Rule, mixed numbers must be reduced to improper fractions.

Note 3. It has been si ewn that a fraction is reduced to its

'owest terms by dividing its num'. and den'. by their G. C. M., or in other words, by the product of those factors which are common to both; hence, in all cases of multiplication of fractions, it will be well to split up the num'n and den'n as much as possible into the factors which compose them; and then, after putting the several fractions under the form, of one fraction, the sign of X being placed between each of the factors in the num' and den' to cancel those factors which are common to both, before carrying into effect the final multiplication. Thus, in the following examples:

Ex. 1. Multiply
$$\frac{3}{4}$$
 and $\frac{4}{5}$ together.

Proof.
$$=\frac{3\times4}{4\times5}=\frac{3}{5}$$
, dividing num'. and den'. by 4.

Ex. 2 Multiply
$$\frac{8}{9}, \frac{16}{24}, \frac{27}{30}$$
, and $\frac{45}{60}$ together.

$$Prod^{t} = \frac{8 \times 16 \times 27 \times 45}{9 \times 24 \times 30 \times 60}$$

$$(2\times2\times2)\times(2\times2\times2\times2)\times(3\times3\times3)\times(3\times3\times5)$$

$$= \frac{1}{(3\times3)\times(2\times2\times2\times3)\times(2\times5\times3)\times(2\times2\times3\times5)}$$

Ex. 3. Multiplying $2\frac{1}{2}$, $3\frac{3}{8}$, $10\frac{1}{8}$, $20\frac{4}{5}$, and $5\frac{9}{78}$ together

$$\operatorname{Prod}^{t} = \frac{5}{2} \times \frac{27}{8} \times \frac{81}{8} \times \frac{184}{9} \times \frac{124}{23}$$
$$= \frac{5 \times (9 \times 3) \times (9 \times 9) \times (3 \times 23) \times (4 \times 31)}{2 \times (2 \times 4) \times 3 \times 9 \times 23}$$

$$=\frac{5\times3\times9\times9\times31}{2\times2}=\frac{37665}{4}=9416\frac{1}{4}.$$

Ex. 4. Simplify ($\frac{6}{7}$ of $1\frac{1}{4}$ of $\frac{14}{15} + 3\frac{1}{2}$ of $2\frac{10}{21} - 2\frac{2}{3} \times 3\frac{2}{7}$

Induce =
$$\left(\frac{6}{7} \text{ of } \frac{5}{4} \text{ of } \frac{14}{15} + \frac{7}{2} \text{ of } \frac{52}{21} - \frac{8}{3}\right) \times \frac{27}{7}$$

= $\left(\frac{3 \times 2 \times 5 \times 2 \times 7}{7 \times 2 \times 2 \times 3 \times 5} + \frac{7 \times 2 \times 26}{2 \times 3 \times 7} - \frac{8}{3}\right) \times \frac{27}{7}$
= $\left(1 + \frac{26}{3} - \frac{8}{3}\right) \times \frac{27}{7} = \frac{3 + 26 - 8}{4} \times \frac{27}{7} = \frac{21}{3} \times \frac{27}{7} = 27$

Ex. XLVI.

Find the value of

- (1) $\frac{1}{9} \times \frac{3}{4}$. (2) $\frac{7}{9} \times \frac{5}{8}$. (3) $\frac{4}{13} \times \frac{5}{8}$. (4) $\frac{2}{21} \times \frac{7}{8}$
- (5) $7\frac{1}{2} \times 3\frac{1}{3}$. (6) $\frac{3}{4}$ of $\frac{1}{6} \times 17\frac{1}{2}$. (7) $\frac{7}{12}$ of $1\frac{1}{7} \times 3\frac{3}{20} \times \frac{1}{3}$?
- (8) $\frac{5}{6} \times 3^{2}_{11} \times 19^{1}_{5} \times \frac{11}{56}$. (9) $\frac{7}{16}$ of 1^{1}_{10} of $1^{1}_{14} \times 2^{1}_{2} \times 2^{1}_{5}$.
- (10) $\frac{11}{17}$ of $3\frac{3}{4} \times 4\frac{4}{5}$ of $2\frac{1}{24} \times 13$.
- (11) $2\frac{11}{23}$ of $(4\frac{1}{6} + 3\frac{5}{14}) \times \frac{11}{6}$ of $2\frac{1}{16} \times 1\frac{1}{16}$.
- (12) $(3\frac{5}{6} 1\frac{7}{12} + 1\frac{4}{9} 2\frac{1}{7}\frac{1}{2}) \times 38\frac{1}{4}$ of $\frac{2}{7}$.
- (1d) $\frac{3}{4}$ of $(\frac{1}{8} + \frac{1}{5} \frac{4}{15} + \frac{1}{5}) \times \frac{2}{3}$ of $(2\frac{3}{16} + \frac{5}{5})$.
- (14) $\{(\frac{1}{2} + \frac{1}{8}) \text{ of } (1\frac{1}{8} + 2\frac{3}{4})\} \times \{(2\frac{1}{14} 1\frac{1}{2}) \text{ of } (3\frac{1}{16} \frac{3}{7})\}.$
- (15) $\left\{1\frac{3}{7} \text{ of } 26\frac{1}{2} \text{ ef } \left(1-\frac{2}{3}\right)\right\} \times \left\{2\frac{5}{9} \text{ of } \left(4\frac{1}{5}-3\frac{2}{3}\right) \text{ of } \frac{45}{106}\right\}.$

DIVISION.

80. Rule. Invert the divisor, i. e. take its numerator as a denominator and its denominator as a numerator, and proceed as in Multiplication.

Ex. 1. Divide ? by ?.

By the Rule, $\frac{3}{7} \div \frac{3}{3} = \frac{3}{7} \times \frac{3}{2} = \frac{7}{12}$.

Reason for the Rule. If \$ be divided by 2, the result is \$ \frac{3}{1}\$; Art. 65).

This quotient is only one-third part of the required quotient, since the divisor is one-third part of 2; hence $\frac{3}{14}$ must be multiplied by 3, in order to give the true quotient, and $\frac{3}{14} \times 3 = \frac{9}{14}$. (Art. 64.)

Note. Before applying this Rule, mixed numbers must be reduced to improper fractions, and compound fractions to simple ones

Ex. 2. Find the quotient of 33 by 42.

$$3_{\frac{3}{15}} \div 4_{\frac{1}{5}} = \frac{78}{25} \div \frac{22}{5} = \frac{78}{25} \times \frac{5}{22} = \frac{\cancel{2} \times \cancel{3} \cancel{9} \times \cancel{5}}{\cancel{5} \times \cancel{5} \times \cancel{2} \times \cancel{11}} = \frac{39}{55}.$$

Ex. XLVII.

Divide (1) 15 by 2

(2) ½ by ½. (3) ½ by ½

(4) 45 by 67.

- (5) 56 by 5\$.
- (6) 75 by 437. (8) \$ of 5½ by \$ of 9.
- (7) \(\frac{1}{8}\) of 20\(\frac{3}{4}\) by 10\(\frac{3}{8}\).
 (9) \((\frac{5}{8}\) of 7\(\frac{1}{4}\) \(\frac{5}{8}\)) by 1\(\frac{3}{6}\).

- What number multiplied by 216 will produce 63?
 - What must \ be divided by in order to produce 2?
- (13) What is the least fraction which must be added to the sum of 4 and 1 divided by their difference to make the result a whole number?

Note. COMPLEX FRACTIONS may by this Rule be re-

duced to simple ones.

(1)
$$\frac{1\frac{3}{4}}{2\frac{1}{2}} = \frac{7}{4} = 7 \div \frac{5}{4}$$
 (Art. 59) = $7 \times \frac{3}{8} = 7$

$$\frac{4\frac{1}{2}}{30} = \frac{\frac{9}{2}}{\frac{3}{4}} = \frac{9}{2} \div 20 = \frac{9}{2} \times \frac{1}{36} = \frac{3}{20}.$$

$$\frac{4\frac{1}{12} + 2\frac{3}{8}}{13\frac{5}{12} - 3\frac{3}{8}} = \frac{6 + \frac{1}{12} + \frac{2}{8}}{10 + \frac{5}{12} - \frac{1}{8}} = \frac{6 + \frac{1}{12} + \frac{5}{12}}{10 + \frac{5}{12} - \frac{4}{12}}$$

$$= \frac{6 + \frac{9}{12}}{10 + \frac{1}{12}} = \frac{\frac{9}{12}}{\frac{1}{12}} = \frac{8}{12} \times \frac{12}{12} \times \frac{8}{12} \times \frac{12}{12} = \frac{8}{12}$$

Ex. XLVIII.

(1)
$$\frac{6\frac{1}{2}}{3\frac{1}{9}}$$
, (2) $\frac{6}{2\frac{1}{4}}$. (3) $\frac{2\frac{1}{4}}{6}$ (4) $\frac{6\frac{9}{19}}{3\frac{2}{8}}$ (5) $\frac{5}{2\frac{5}{8}}$

Simplify, (2) 6 (3)
$$\frac{2\frac{1}{4}}{6}$$
 (4) $\frac{6\frac{1}{12}}{3\frac{1}{8}}$ (5) $\frac{5}{2\frac{1}{8}}$ (6) $\frac{7}{4\frac{1}{18}}$ (7) $\frac{1\frac{3}{4} \text{ of } 1\frac{1}{1}}{1\frac{2}{8} \text{ of } \frac{1}{1}}$ (8) $\frac{7}{4} + \frac{3}{7}$ (9) $\frac{5\frac{1}{2} + 6\frac{3}{7}}{6\frac{3}{7} - 5\frac{1}{2}}$ (10) $\frac{1}{2\frac{1}{4}} + \frac{1}{3\frac{1}{4}} + \frac{1}{4\frac{1}{4}}$

(11)
$$\left\{\frac{3\frac{1}{3}}{7} + \frac{2}{10\frac{1}{2}} - \frac{5}{18} \text{ of } \frac{4}{7}\right\} \times 1\frac{3}{2}$$
. (12) $\left(\frac{5\frac{5}{7}}{31\frac{5}{8}} \text{ of } \frac{9}{14}\right) \div \left(\frac{3\frac{2}{3}}{3\frac{2}{3}} \text{ of } 15\right)$.

$$\frac{13)}{2^{\frac{2}{5}}-1^{\frac{2}{5}}} \circ^{\frac{5}{6}} \frac{2^{\frac{1}{5}} \times 8^{\frac{1}{3}}}{4^{\frac{1}{5}} \div (\frac{1}{5} - \frac{1}{9})}. \qquad (14) \quad \frac{13}{2^{\frac{2}{6}}+\frac{1}{4}} + \frac{1^{\frac{1}{3}}}{3^{\frac{1}{5}}} - 1^{\frac{3}{16}}.$$

81. To find the value of a fraction in terms of the same or lower denomination.

RULE. Divide (if possible) the numerator by the denominator; if there be a remainder, reduce it to the next lower name, and divide the product by the denominator; repeat the latter operation as often as necessary.

Find the value of 3 of £15.

By the Rule, \hat{r} of £15 = £ $\frac{2\times15}{7}$ = £ $\frac{30}{7}$ =£4 \hat{r} ; £ \hat{r} = $\frac{2\times20}{7}$ s. = $\frac{40}{7}$ s. =5 \hat{r} s. \hat{r}

$$\frac{3}{7}s. = \frac{5 \times 12}{7}d. := \frac{60}{7}d. = 8 \frac{1}{7}d.; \quad \frac{1}{7}d. = \frac{4 \times 4}{7}q. = \frac{16}{7}q. = 2\frac{3}{7}q.$$

$$\therefore \frac{2}{7} \text{ of } £15 = £4. 58. 6\frac{1}{7}d. \frac{2}{7}q.$$

Ex. XLIX.

Find the respective values of,

- (1) \(\frac{2}{5}\) of \$1. (2) \(\frac{3}{5}\) of a ml. (3) \(\frac{5}{7}\) of a cwt.
- (4) $\frac{9}{30}$ of 2 tons. 3 cwt. (5) $\frac{3}{16}$ of 3 mls., 2 fur.
- (6) \$\frac{4}{5}\$ of 3 ac., 2 per., 3 yds. (7) \$\frac{5}{6}\$ of 5 lbs., 13 dwts.
- (8) 7 of 68 yds. 2 nls. (9) 3 of £26. 8s. 11d.
- (10) $\frac{6}{7}$ of 128 lbs., 2 sc. (11) $\frac{7}{8}$ of $\frac{3}{6}$ of $10\frac{2}{3}$ hrs.
- (12) 7% of a lb. Avoird. (13) % of % of \$42.
- (14) $\frac{3}{10}$ of a day. (15) $\frac{9}{16}$ of 24 cords of wood.

82. To reduce a given quantity to the fraction of another quantity of the same kind.

NULE. Reduce both to the same name; and take the result of the former for the numerator, and of the latter for the denominator, of the required fraction.

Reduce 7s. 5d. to the fraction of £1.

Method of working,

7s. 5d. = 89d.
£1. = 240d.

the fraction is $\frac{89}{340}$. $\frac{89}{240}$ of £1; ... 7s. 5d chief 89d. is $\frac{89}{240}$ of £1.

Ex. L

Reduce,

- (1) 3s. 4d. to the fr. of £1.
- (2) 2 ro. 13 per. to the fr. of 3 acres.
- (3) 3 wks., 16 min. to the fr. of half-an-hous.
- (4) 1 lb., 1 oz., 3 dwt., to the fr. of 2 lbs.
- (5) 1 lb., 5 oz. to the fr. of 2 lbs. 1 sc.
- (6) 8 ac., 3 ro. to the fr. of 2 ac., 32 per.
- (7) 2 sq. yds.. 2 ft., 120 in., to fr. of 3 per. 134 yds., 1 ft /2 11
- (8) £1. 18s. to the fr. of £7.
- (9) 2 bu., 1 pk., to the fr. of 4 bu. 1 gal.
- (10) \$2.09 to the fr. of \$56.43.
- 11) 2 yds., 2 ft. to the fr. of 13 per 3 yas., 6 in.

- (12) 1 lb. Troy to the fr. of 1 lb. Avoirdupois.
- (13) What fraction of 7 bu. is 3 qts.?
- (14) What fraction of 4 mls., 2 fur. is 11 yds.?
- (15) What fraction of 5 ac., 1 per. is 1 yd., 4 in.?
- 83. To reduce a fraction of one given quantity to a fraction of another.

RULE. Express by (82) the first quantity as a fraction of the second; and the fraction required will then be found by reducing the resulting compound fraction to a simple one.

Ex. 1. Reduce ? lb. to the fraction of a cwt

Method of working,

1 lh. = $\frac{1}{160}$ of cwt.; ... $\frac{2}{7}$ lb. = $\frac{2}{7} \times \frac{1}{160}$ of a cwt. = $\frac{3}{500}$ of cwt.

Ex. 2. $2\frac{1}{4}$ of \$5.25 to the fraction of 15 cents.

\$5.25 is $_{1}^{85}$ of 15 cts.; ... 2_{4} of $_{1}^{85}$ of 15 cts. $=\frac{31}{4}$ of 15 cts.

Ex. LL.

Reduce,

- f of \$14 to the fr. of f of \$16.
- (2) \$ of 2 ac., 2 ro. to the fr. of \$ of 3 ac., 2 per.
- (3) 21 of 3 lbs., 6 dwt. to the fr. of 11 of 6 lbs., 12 gra.
- (4) 12% of 3s. 6d. to the fr. of £1. .
- (5) 31 of 10 cwt., 2 grs., to the fr. of 1 ton.
- (6) 3\frac{1}{2} of 2 ac., 3 ro. to the fr. of 2 ro., 2\frac{1}{2} per.
- (7) § lb. Troy to the fr. of a lb. Av.
- (8) 1_{3} of £2. 4s. 71d, to the fr. of 5s.
- (9) 3 of 23 mls. to the fr. of 1 of 7 mls.
- (10) 6½ of 3 cords to the fr. of 5 cord ft.
- (11) 81 of 6 lbs., 2 sc. to the fr. of a lb.
- (12) of 3 of \$21 to the fr. of \$7.
- (13) $_{18}^{\circ}$ of 8 yds., 2 nls. to the fr. of $2\frac{1}{3}$ ells (English).
- (14) 27 of 10 hrs. to the fr. of 1 day.
- 84. Miscellaneous Examples in Vulgar Fractions worked out.
- Ex. 1. At the 'call over' at a certain school, § of the children on the register answered to their names; the rest, 18 in number, were absent. How many children were there as the register's

the no. were present, . . h of no. were absent. By the question, & of no. = 18.

... no. = $18 \times 6 = 108$.

Ex. 2. A poor woman lost through a hole in her pocket of her money; only 3s. 03. l. was left. How much money ad she at first. and how much did she lose?

After losing it of her money, it of it was left,

 \therefore J_{τ} of her money = 3s. $0\frac{3}{4}d$ of her money = 38. $0\frac{3}{4}$, $t = 7 = 5\frac{1}{4}d$ her money = $5\frac{1}{4}d$. $\times 11 = 48.9\frac{3}{2}d$.

19s. 3d. She lorg in of 4s. 9\$d.= - = 1s. 9d.

Ex. 3. A. B. C. D run a race over 1 mile. First A and B race, when A wins by 20 yds.; then C and D race, when C wins by 60 yds.; then A and C race, which will win, and by how much, supposing that if B and D had run against each other. B would have won by 40 yds.?

While A runs 1760 yds., B runs 1740 yds.; while C runs 1760 yds., D runs 1700 yds., or while D runs 1 yd., C runs $\frac{1769}{68}$ yds.; while B runs 1760 yds, D would have run 1720 yds., or while B runs 1 yd., D would have run $\frac{1720}{1760}$ yds.

While A runs 1760 yds., B runs 1740 yds.

". D runs (1740 $\times \frac{172}{6}$) yds. C runs $(1740 \times \frac{172}{176} \times \frac{176}{176})$, or $1760 \frac{8}{17}$ yds.

... C will win by 3 yds.

Ex. 4. Divide 153. 6d. between A and B, so that B's share may be less than A's share by 2 of A's share.

To represent A's share fix on some number which is ex-

ectly divisible by 5; let 5 represent A's share.

Then B's share = $5 - \frac{2}{3}$ of 5, or 5 - 2, or 3. 1. 15s. 6d. has to be divided into 5 + 3, or 8 shares, of which A is to have 5, and B3;

... value of each share $=\frac{15s. \ 6d.}{8} = is. \ 11\frac{1}{4}d.$

... A's share = 1s. $11\frac{1}{4}d$. $\times 5 = 9s$. $8\frac{1}{4}d$., B's = 1s. $11\frac{1}{4}d$. $\times 3 = 1$ 5s. 93d.

Ex. 5. If 7 men or 11 boys can dig a field in 10 days, in "! at time will 11 men and 7 boys dig at eld of half the size? 7 men = 11 boys, . . . 1 man = 1 boy;

121 + 49... Il men and 7 boys= $(11 \times \frac{1}{7} + 7)$, or $\frac{1}{7}$, or $\frac{1}{7}$ boys By the question,

11 boys can dig the great field in 10 days. , 1 boy.....(10 × 11) days: $10 \times 11 \times 7$... 7 boys..... 170 days;

...... the less field in $\frac{10 \times 11 \times 7}{170 \times 2}$ days = $2\frac{9}{54}$ days.

Ex. 6. Divide 1860 cords of wood between A, B, and C, so that for every 5 cords given to A, B may receive 4 cords. and for every 3 cords given to B, C may receive 1 cord.

The L. C. M. of 5, 4, and 3 is 60; ... if 60 shares be given to A, B will have to of 60 shares, or 48 shares, and C will have

1 of 48 shares, or 16 shares;

... A, B, and C together have (60 + 48 + 16), or 124 shares;

... A has $\frac{1}{124}$ of 1860 cerds = (15 × 60), or 900 cerds.

B has $\frac{2}{124}$ of 1860 cords = (12 × 60), or 720 cords.

C has $\frac{124}{124}$ of 1860 cords = (4 × 60), or 240 cords.

Ex. 7. A can do a piece of work in 5 days, B can do it in o days, and C can do it in 7 days; in what time will A. B. and C, all working at it, finish the work? Find also in what time A and B working together, A and C together, and B and C together, could respectively finish it.

In one day....A....does $\frac{1}{5}$ part of the work, ... B ... $\frac{1}{R}$...

.. no. of days in which A + B + C would finish the work

 $\frac{\text{whole work}}{\text{part done in one day}} = \frac{1}{107} = \frac{210}{107} = 1\frac{30}{107} = 1\frac{30}{107}$

Again, in one day $A + B \operatorname{do}\left(\frac{1}{5} + \frac{1}{6}\right)$, or $\frac{11}{30}$ of the work,

... A + R would linish the work in $\frac{l}{11}$, or $\frac{30}{11}$, or $2\frac{s}{11}$ days

In like manner, it may ℓ shewn that A and C would finish the work in $2\frac{1}{4}$ days: and B and C in $3\frac{3}{18}$ days.

Ex. [4]

- (1) $\frac{4}{5}$ ths of a farm belongs to A, $\frac{4}{5}$ rest to B; A sells $\frac{3}{5}$ ths of his share to C, and $\frac{1}{12}$ th of it to B; what portions of the farm do A, B, and C, respectively hold after the sales $\frac{1}{5}$
- (2) (1) Among how many boys can 9 oranges be divided so that each boy may have $\frac{3}{5}$ of an orange? (2) From the sum of $4\frac{1}{2}$ and $3\frac{9}{10}$ take their difference.
- (3) Divide $\frac{2}{3}$ into two parts, so that one of them is greater than the other by $\frac{3}{4}$.
- (4) (1) What number must be multiplied by $1\frac{1}{5}$ of $2\frac{2}{5}$ to give $3\frac{3}{5}$? (2) What number must be added to $\frac{1}{5}$ of $2\frac{1}{7}$ to give $3\frac{2}{5}$?
- (5) A gives to $B \frac{1}{5}$ of his money, to $C \frac{1}{2}$ of what remains, and to $D \frac{1}{3}$ of what then remains; compare the sums which A and D will now have.
- (6) Miss Taylor, after spending 3rd of the money in her purse, and then 3ths of the remainder, has still left \$4.20; how much had she in her purse at first?
- (7) $_{3}^{7}$ of a fishing smack being worth \$90, find the value of $_{3}^{1}$ rd of it.
- (8) A person after paying an income-tax of 5 cents in the dollar, has a net income of \$855; find his gross income?
- (9) If, when the income-tax was 6 cents in the dollar, a person paid \$54; how much less will he now pay, the tax being reduced 4 cents in the \$?
- (10) If † of a rabbit be worth \(\frac{2}{3}s. \), and \(\frac{2}{5} \) of a rabbit be worth \(\frac{1}{30} \) of a pig; what is the value of 100 pigs?
- (11) If, in practising, 7 riflemen shoot 26 rounds in 1 hr., 31 min.; how many rounds will 37 riflemen shoot in 44 hrs. at the same rate?
- (12) A sum of money is divided into 4 parts, which are to each other as the numbers 1, 2, 3, 4; and a person, wno receives § of each share, obtains altogether \$12.60; find the sum of the several shares?
- (13) If 15 cows or 28 sheep can graze a field of 5 ac. in 41 days, how many days ought a similar field of 18 ac. to serve 33 cows and 20 sheep?

- (14) Divide \$94.50 between A and B; (1) giving A half as much again as B; (2) giving A's share less half A's share to B.
- (15) A bankrupt owes to one creditor 500 dollars, to each of two others \$250, to each of three others \$75: his property is worth \$625. How much can he pay in the dollar, and how much will the first creditor receive?
- (16) A mine is worth \$10000; a person for $\frac{1}{15}$ of his share receives \$750. What part of the mine did he possess?
- (17) A school is composed of three divisions; there are $\frac{1}{2}$ this of the whole number of boys in the first, $\frac{1}{2}$ th in the second, and the rest, 80 in number, in the third; how many boys are there altogether?
- (18) A can do a piece of work in 10 days, which B could do in 12; in what time would they do it together?
- (19) A father left to the elder of his two sons $\frac{13}{25}$ of his estate, and $\frac{13}{25}$ of the remainder to the younger, and the residue to the widow; find their respective shares, it being found that the elder son received \$1690 more than the younger.
- (20) Divide 85 ac. 2 ro. of land between A, B, and C, so that B's share $=\frac{e_1}{11}$ of A's share, and that Cs share shall be 9 ac. more than the united shares of A and B.
- (21) A fine of \$14.40 had to be raised among a number of boys; one-third paid 18 cents each, as many more 30 cents each, and the remainder 42 cents each. How many boys were there?
- (22) A cistern has 3 p.pes in it, by one of which it could be filled in 3 minutes, and by the other two it could be emptied in 6 and 7 minutes respectively; in what time will it be filled, if they are all opened together?
- (23) A and B together can do spiece of work in 30 days, B by himself can do it in 70 days; (1) in what time could A do it by himself? (2) how much more of the work does A do than B, when they work together?
- (24) A and B can do a piece of work in 62 days, A and C in 52 days, and A, B, and C in 32 days. In how many days can A do it alone?
- (25) There are 4 casks of different sizes. The 1st is filled with liquid the rest are empty. The 2nd cask is filled from the 1st, and 4ths of the original liquid in the 1st remains. The 3rd is then filled from the 2nd, and 4th of the liquid in

the 2nd remains. The figuid in the third is then poured into the 4th, and fills ${}_{10}^{\circ}$ ths of it. Had the 3rd and 4th casks been filled from the contents of the 1st, 15 gallons would still have remained in the 1st. Find the size of each cask?

(26) A in 2 days can do as much work as B can do in 3 days; together they take 12 days to do a certain work. In what time would A alone have done it?

DECIMALS

85. Figures in the units' place of any number express their simple values, while those to the left of the units' place increase in value tenfold at each step from the units' place; therefore, according to the same notation, as we proceed from the anits' place to the right every successive figure would decrease in value tenfold. We can thus represent whole numbers or integers and certain fractions under a uni form notation by means of figures in the units' place and on each side of it; for instance, in the number 5673 241, the figures on the left of the dot represent integers, while those on the right of the dot denote fractions. The number written at length would stand thus:

$$5 \times 1000 + 6 \times 100 + 7 \times 10 + 3 + \frac{2}{10} + \frac{4}{100} + \frac{1}{1000}$$

The dot is termed the decimal point, and all figures to the ight of it are called Decimals, or Decimal Fractions, because they are fractions with either 10, 100 or 10 × 10, 1000

\r	10 ×	(10	$\times 10$), &c	as	the	in e eir re Tal	espe	ectiv	re de	non	iina	tors.	
	7	6	5	4	3	2		9	3	4	5	6	7	
&c.	Millions.	Hundreds of Thousands.	Tens of Thousands.	Thousands.	Hundreds.	Tens.	Units.	Tenths.	thundredths.	Thousandths.	Ten Thousandths.	Hundred Thousandths.	Millionths.	to.

86. 10, called the first Power of 10, is written thus, 10¹. 10 × 10, or 100, called the second Power of 10, is written

thus, 102.

 $10 \times 10 \times 10$, or 1000, called the *third* Power of 10, is written thus, 10^3 , and so on; similarly of other numbers: thus the fifth power of 4 is $4 \times 4 \times 4 \times 4$, and is written thus, 4^5 .

The small figures 1, 2, 3, &c., at the right of the number, a

little above the line, are called INDICES.

87.
$$306 = \frac{3}{10} + \frac{0}{100} + \frac{6}{1000} = \frac{3 \times 100}{10 \times 100} + \frac{0 \times 10}{100 \times 10} + \frac{6}{1000}$$

$$= \frac{300}{1000} + \frac{0}{1000} + \frac{6}{1000} = \frac{306}{1600}.$$
Again,
$$0306 = \frac{0}{10} + \frac{3}{100} + \frac{0}{1000} + \frac{6}{10000} = \frac{0 \times 1000}{10 \times 100} + \frac{3 \times 100}{100 \times 100} + \frac{9 \times 10}{10000} + \frac{6}{10000} = \frac{0 + 300 + 0 + 6}{10000} = \frac{306}{10000} + \frac{306}{10000} = \frac{80306}{1000}.$$
Again,
$$80.306 = 80 + \frac{306}{1000} = \frac{80000 + 306}{1000} = \frac{80306}{1000}.$$

Hence to convert decimals to vulgar fractions: from the above examples we deduce the following:

88. Rule. Write the figures which compose the decimal as numerator, and for denominator 1, followed by as many cyphers as there are figures after the decimal point.

Ex. LIII.

Express as vulgar fractions,

- (1) '3; '13; '19; '301; '270; '5653.
- (2) '504; '73201; '791003; '03; '0045.
- (3) '300; 18:741; 2:1; '000001; 5:0007.
- (4) 347.02007; 500.005; 5.60746805; 0000500
- (5) 29·0050; 20·607; 5·00038.
- 89. Any fraction, having 10, or any power of 10, for its aenominator, as \$\frac{0.0036}{0.0036}\$, may be expressed thus, 80.0036.

For $\frac{80 \cdot 803 \cdot 6}{100 \cdot 6030} = 80 + \frac{1}{100 \cdot 600} + \frac{1}{100 \cdot 600} = 80 + \frac{1}{100} + \frac{1}{100$

90. $241 = \frac{241}{1000}$, $0241 = \frac{241}{10000}$, $2410 = \frac{2410}{10000} = \frac{241}{10000} = \frac{241}{10000}$

We see that '241, '0241, and '2410 are respectively equivaient to fractions which have the same numerator, and the first and third of which have also the same denominator, while the denominator of the second is greater. Hence '241

equal to 2410, but 0241 is less than either.

The value of a decimal is therefore not affected by affixing syphers to the right of it; but its value is decreased by prefixing cyphers: which effect is exactly opposite to that which is produced by affixing and prefixing cyphers to integers.

91. A decimal is multiplied by 10, if the decimal point be removed one place towards the right hand; by 100, if two places; by 1000, if three places; and so on: and conversely, a decimal is divided by 10, if the point be removed one place to the left hand; by 100, if two places; by 1000, if three places; and so on.

Thus, $5.6 \times 10 = \frac{5}{10} \times 10 = 56$; $5.6 \times 1000 = \frac{5}{10} \times 1000 = 500$, $5.6 \div 10 = \frac{5}{10} \times \frac{1}{10} = \frac{5}{100} \times \frac{1}{10} = \frac{5}{100} = \frac{5}{100} \times \frac{1}{1000} = \frac{5}{1000} = \frac{5}{1000} \times \frac{1}{1000} = \frac{5}{1000} \times \frac{$

Ex. LIV.

- (1) 10; 10; 10; 10; 100; 1000; 1000.

- (4) Seven-tenths: thirty thousandths.
- (5) Three hundred and three thousandths; one ten thousandth.
- (6) Four, and five hundred and four millionths; seventy ten millionths.

Express in words the meaning of,

- (7) ·6; ·17; ·07 (8) ·007; ·700; 6·3^04.
- (9) 35·00205; 400·34000.
- (10) Multiply 3, 13, 013, 54 0003, $7420 \cdot 1$, each separately by 10, 100, 10000, and by ten millions.
- (11) Divide 5:362, :3, 70:0107, and 5000, each separately by 10, 100, and by 1000000.
 - (12) What is the quotient of 2.03 by a million?

ADDITION OF DECIMALS.

92. RULE. Place the numbers under each other, units under units, tens under tens, &c., tenths under tenths, &c.; so that the decimals be all under each other. Add as in

whole numbers, and place the decimal point in the sum under the decimal point above.

Ex. Add together 2.3, .056, 37, and 3.60015.

By the Rule.

2.3 By fractions.

 $\begin{array}{ll} 37 \cdot & 2 \cdot 3 + \cdot 056 + 37 + 3 \cdot 60015 = \frac{73}{13} + \frac{5}{13} \cdot \frac{5}{13} + \frac{5}{13} \cdot \frac{5}{13} \cdot \frac{5}{13} \\ & = \frac{73}{13} \cdot \frac{5}{13} \cdot \frac{5}{13} \cdot \frac{5}{13} + \frac{5}{13} \cdot \frac{5}{13} \cdot \frac{5}{13} + \frac{5}{13} \cdot \frac$

 $\frac{42.95615}{1600000} = 42.95615 \text{ (Art. 89)}.$

Ex. LV.

Add (1) 1.035 (2) 24 (3)186.8 (4) 94.25 00643 185:3009 35.2779 -00827 · .98795 9000 187 96009 2.2146 3.098 9.201 57:3916 70006 830:05764 530.09 5.998347

Add together, and verify each result by fractions:

- (5) 12.5, 20.043, 7.63201, add 90561.
- (6) .0573, 15, 2.04, and 567.98075.
- (7) 505.0003, 13.98, 5853.097, and 960.
- (8) 6.00734, 54, 15.70087012, 8.00003, and 9.987789.
- (9) Find the sum of thirteen hundredths, seven and three ten-thousandths, four hundred and eight and five tenths, nine hundred and seventy-eight, and eight hundred and eight ten-thousandths.

SUBTRACTION OF DECIMALS.

93. RULE. Place the less number under the greater, units under units, tens under tens, &c., tenths under tenths, &c.: suppose cyphers to be supplied if necessary in the upper line to the right of the decimal

Then subtract as in whole numbers, and place the decimal

point in the remainder under the decimal point above.

Ex. Subtract 3 084 from 5.7.

By the Rule,

57 3081 57 - 3084 = \$7 - \$888 = \$788 - \$888 = \$818 = 2.616.

Ex. LVI.

- (1) From 5 345 (2) 26 and (3) 15 67 (4) 21 Take 3 087 15 9564 9 7003 19 9009
- (5) Find the difference between, verifying each result by fractions, (1) ·13 and 1·3; 2·07 and 207. (2) 76·3 and 7.63; 67·3 and 67·5803. (3) 501 and 428·90456; 53·24 and 5324. (4) 4·42 and ·00042; ·0000007 and ·007.
- (6) By how much does 23 exceed the difference between 2.3 and .23?
- (7) Find the difference (1) between one-tenth and five thousandths; (2) between twenty and nine thousandths and twenty-nine thousandths.
- (8) A person who has seven-tenths of a ship, sells eighty seven thousandths of it, how much has he left?
- (9) Find the least fraction, which added to the sum of 1.2, .12, .012, and 210, will make the result a whole number.
- (10) Find the value of (1) 31.25 3.059 + 235.6758 184.0003; (2) 215.263 (7.0004 .05) (45.08 + 80.3007).

MULTIPLICATION OF DECIMALS.

94. Rule. Multiply the numbers together as if they were whole numbers, and point off in the product as many decimal places as there are decimal places in both the multiplicand and the multiplier; if there are not figures enough, supply the deficiency by prefixing cyphers.

Ex. Find the product of (1) 7:35 by 23, (2) of 8:27 by

·0002.

By the Rule, (1) 7:35

 $\frac{23}{2205}$ By fractions, $7.35 \times 23 = \frac{188}{188} \times \frac{23}{188} = \frac{18888}{1888} = 1.6905$,

1.6905

 $\begin{array}{ccc} (2) & 8.27 \\ & 0002 \\ \hline & 001654 \end{array} & 8.27 \times 0002 = \frac{185}{185} \times \frac{2}{10000} = \frac{185}{100000} = 0016 \text{ fm} \\ \end{array}$

Multiply Ex. LVII.

(1) 3·25 (2) 6·035 (3) 40·004 (4) 680·35 (5) 20607 By 35 2·7 2·03 0049 20607 Multiply, and verify each result by fractions:

- (6) 60.71 by 11; 57.068 by 2.004; 5.36 by 700; 7.01509 by 50.805.
 - (7) 48.067 by .00037; 54.3047 by 9.00005; 2.568 by .00025.
- (8) Find the continued product (1) of 5.5, 055, 550, and 9055; (2) of 1.75, 6.2, 85, and 9004.
- (9) How many yds. of cloth are there in 7.35 pieces of cloth, each of which contains 37.85 yds.?
- (10) A man eats 95 of a loaf daily; how many loaves will he eat in the year 1866?

DIVISION OF DECIMALS.

95. First, When the number of decimal places in the dividend exceeds the number of decimal places in the divisor.

RULE. Divide as in whole numbers, and mark off in the quotient a number of decunal places equal to the excess of the number of decimal places in the dividend over the number of decimal places in the divisor; if there are not figures sufficient, prefix cyphers as in Multiplication.

Ex. 1. Divide (1) 2.1125 by 8.45, (2) .0021125 by 84.5.

By the Rule,

(1) 8:45)2:1125(25 By fractions, $\frac{1690}{4225} = 2 \cdot 1125 \div 8 \cdot 45 = \frac{211125}{11125} \div \frac{8}{10} \cdot \frac{8}{10} = \frac{2}{1112} \cdot \frac{8}{10} \times \frac{8}{10} = \frac{2}{1112} \cdot \frac{8}{10} \times \frac{8}{10} = \frac{2}{10} \cdot \frac{8}{10} \times \frac{8}{10} = \frac{8}{10} \cdot \frac{8}{10} \times \frac{8}{10} = \frac{8}{10} \cdot \frac{8}{10} \times \frac{8}{10} = \frac{8}{10} \times \frac{8$

4225 = 25.

No. of dee! places in quotient = 4-2=2, ... quotient = 25. (2) 84.5) Ω 21125 (25 By fractions,

 $\frac{1690}{4225}
\begin{array}{r}
0021125 \div 84 \cdot 5 = \frac{21125}{10010000} \div \frac{8}{10} \\
= \frac{21125}{1000000} \times \frac{8}{10} = \frac{21125}{1000000} \times \frac{8}{10} \times \frac{1}{1000000} \\
4225
= \frac{2}{10000000} \times \frac{8}{10000000} \times \frac{8}{1000000} = \frac{1}{10000000} = 0000025.$

No. of decl. places in quotient=7-1=6, ... quotient='000025.

96. Secondly. When the number of decimal places in the dividend is less than the number of decimal places in the divisor.

RULE. Affix cyphers to the dividend until the number of decimal places in the dividend equals the number of decimal places in the divisor; the quotient up to this point of the division will be a whole number.

If there be a remainder, and the division be carried on

further, the figures in the quotient after this point will be decimals.

Ex. 2. Divide 2112.5 by 845.

By the Rule,

845)2112:500(2500

1690	By fractions,
4225	$2112.5 \div .845 = \frac{2112.5}{10.00} \div \frac{845}{1000} = \frac{2113.5}{1000}$
4225	$\times \frac{1000}{545} = \frac{21125}{845} \times \frac{1000}{100} = 25 \times 100 = 2500$
00	

Ex. LVIII.

Divide and verify each result by fractions.

- (1) 33·372 by 2·7. (2) ·33372 by ·27. (3) ·33372 by 27.
- (4) 33372 by ·27.
- (5) 33372 by 00027.
- (6) 561 0833 by 323.
- (7) 5610833 by 323.
- (8) 56108·33 by **3**·23.
- (9) 5610.833 by 6000323
- (10) 552:5325 by 3:25, and also by :00325.
- (11) 2.419003 by 464.3, and also by .004643.
- (12) '000081 by 2.7, by '0027, and also by 27000.
- (13) 218051 081884 by 2:00099, and by 200099.
- (14) '121 by 11, by 1100, and also by '0011.
- (15) 393.72 by .000193, by 1.93, and also by 193000.
- (16) 590:4825 by :03275, and also by 327500.
- (17) 213.419596 by 1.00103, and also by 100103.
- (18) Divide the sum of twenty-four ten thousandths and twenty-four hundreths by twenty-four.
 - (19) Two ten thousandths by twenty-five hundreths.
- (20) If a man mow 1.75 ac. of grass in one day, how long will it take him to mow 21.875 ac.?
 - (21) How often is '75 min. contained in 64'125 min.!
- (22) The product of two numbers is seventy thousand two hundred and forty-two hundred millionths; one of the numbers is twenty-three thousandths; find the other number.
- Ex. 3. Divide 240:13 by 73:4 to three places of decimals. Before dividing, affix two cyphers to the dividend, so as to make the number of decimal places in the dividend exceed

the number of decimal places in the divisor by 3; if we divide up to this point, the quotient will contain 3 decimal places by Rule 1.

73·4) 240·1300 (**3·271 220** By fractions. 240·13 ÷ 73·4 = 2 + 8 + + 18 1993 1468 $= \frac{24018}{600} \times \frac{10}{731} = \frac{24018}{31} \times \frac{10}{100}$ $=\frac{24013}{734} \times \frac{100}{1000}$ 5250 (we multiply numr. and denr. by 10, to 5138 make den'. 1000, since the quotient is 1120 to contain three decimal places) 734 = 21 41 20 \times $^{-1}$ $^{-1}$ = 27 1 = 3 27 1 386

Ex. LIX.

Divide to three places of decimals, and verify each result by fractions,

(1) 1.9 by 3, by 03, and by 300.

(2) 4.937 by 159, by 1.59, and by 1590.

(3) 329744 by 53, by 0053, and by 5300.

\$7. Certain Vulgar Fractions can be expressed accurated as Decimals.

RULE. Reduce the fraction to its lowest terms; then place a dot after the numerator and affix cyphers for decimals; divide by the denominator, as in division of decimals, and the quotient will be the decimal required.

Fix. 1. Convert \$, 30, 300, each into a decimal.

4) 300 No. of dec! places in quotient = no. of dec! places in dividend - no. of dec! places in divisor = 2-0=2.

 $=3 \div 10 = .75 \div 10 = .075$; $=3 \div 100 = .75 \div 100 = .0075$.

Ex. 2. Reduce $\frac{\partial}{16}$ to a decimal.

16) 5 0000 (3125 $-\frac{48}{20}$ or thus, 16 $\left\{\frac{4}{4}\right| \frac{5 \cdot 00}{1 \cdot 2500}$ $\frac{16}{40}$ $\frac{32}{80}$ $\frac{32}{80}$ $\frac{5}{80}$ E. S. Convert $5\frac{4}{12}$ + '75 of $\frac{6}{5}$ of $7\frac{1}{2}$ into a decimal.

640
$$\begin{cases} 8 & \frac{5.006}{.625000} \\ 10 & \frac{-078125}{.0078125} \end{cases}$$
 75 of $\frac{6}{6}$ of $7\frac{1}{2} = .75$ of $\frac{1}{6}$ of $\frac{1}{6}$

... $5_{\frac{6}{440}} + .75$ of $\frac{6}{5}$ of $7\frac{1}{2} = 5.0078125 + 6.75 = 11.7578125$

Ex. LX.

Reduce to decimals,

- (1) $\frac{1}{4}$; $\frac{3}{5}$; $\frac{4}{4}$; $6\frac{1}{5}$; $\frac{3}{5}$; $\frac{5}{6}$; $\frac{5}{5}$; $\frac{3}{10}$. (2) $\frac{3}{10}$; $8\frac{15}{16}$; $\frac{19}{20}$; $\frac{3}{21}$; 71.
- $\frac{1}{3}$ (3) $\frac{47}{50}$; $4_{1}\frac{7}{25}$; $\frac{3}{500}$; $\frac{99}{625}$; 84_{1024} .
-) (4) § of 18; 38 of 24; 32 of 44 of 58.
- (5) $1\frac{3}{6} \frac{13}{16} + 3\frac{5}{40}$; $11\frac{1}{2} \div .75$ of $\frac{24}{25}$ of $6\frac{3}{4}$.
- · 98. To convert a vulgar fraction into a decimal, we have in fact, after reducing the fraction to its lowest terms. and affixing cyphers to the numr., to divide 10, or some multiple of 10 or of its powers, by the den.; now $10=2\times 5$, and these are the only factors into which 10 can be broken up; therefore, when the fraction is in its lowest terms, if the den'. be not composed solely of the factors 2 and 5, or one of them, or of powers of 2 and 5, or one of them, then the division of the num'. by the den'. will never terminate. Decimals of this kind are called indeterminate decimals, and they are also called CIRCULATING, REPEATING, or RE-CURRING DECIMALS, from the fact that when a decimal does not terminate, the same figures must come round again, or recur, or be repeated: for since we always affix a cypher to the dividend, whenever any former remainder recurs, the quotient will also recur.
- 99. Pure Circulating Decimals are those which recur from the beginning: thus, '333.., '2727.., are pure circulats, dech.

MIXED CIECULATIN DECIMALS are those which do not begin to recur, till after a certain number of figures: thus, 128888..., 0113636..., are mixed circulats. decla.

The circulating part is called the Period or Repetend. Pure and mixed cilculating decimals are generally written down only to the end of the first period, a dot being placed over the first and last figures of that period.

Thus ·3 represents the pure circulats. decl.	·333 .
·36	.3636
·639	.639639.
138 mixed	·1388
01136	0113636

100. Pure Circulating Decimals may be converted into their

equivalent Vulgar Fractions by the following Rule.

RULE. Make the period or repetend the numerator of the fraction, and for the denominator put down as many nines as there are figures in the period or repetend.

This fraction, reduced to its lowest terms, will be the frac-

tion required in its simplest form.

Ex. Reduce the following pure circulats. dech., '3, '27, 857142, to their respective equivalent vulgar fractions.

By the Rule,
$$\dot{3} = \frac{3}{9} = \frac{1}{3}$$
; $\dot{27} = \frac{27}{99} = \frac{3}{11}$.
 $\dot{857142} = \frac{857142}{999999} = \frac{142857 \times 6}{142857 \times 7} = \frac{6}{7}$

101. Mixed Circulating Decimals may be converted into their equivalent Vulgar Fractions by the following Rule.

RULE. Subtract the figures which do not circulate from the figures taken to the end of the first period, as if both

were whole numbers.

Make the result the num¹, and write down as many nines as there are figures in the circulating part, followed by as many zeros as there are figures in the non-circulating part, for the denominator.

Ex. Reduce the following mixed circulat decis. 14, 0138, 2418, to their respective equivalent vulgar fractions.

By the Rule,
$$1\dot{4} = \frac{14-1}{90} = \frac{13}{90}$$
; $013\dot{8} = \frac{138-13}{9000} = \frac{125}{9000}$
= $\frac{1}{72}$; $2\dot{4}1\dot{8} = \frac{2418-2}{9990} = \frac{2416}{9990} = \frac{1208}{4995}$.

102. In the Addition and Subtraction of circulating decimals, where the result is only required to be true to a certain number of decimal places, it will be sufficient to carry on the circulating part to two or three decimal places more than the number required; taking care that the last figure

retained be increased by 1, if the succeeding figure be 5, or greater than 5. In the Multiplication and Division, however, of circulating decimals, it is always preferable to reduce the circulating decimals to Vulgar Fractions, and having found the product or quotient as a Vulgar Fraction, then, if necessary, to reduce the result to a decimal.

Ex. LXL

Reduce to circulating decimals: (1) $\frac{2}{3}$; $\frac{1}{9}$; $\frac{6}{7}$; $\frac{7}{12}$; $\frac{11}{15}$,

(2) $6\frac{3}{81}$; $7\frac{6}{87}$; $100\frac{7}{4}$; $2\frac{1}{2}$. (3) $11\frac{67}{675}$; $23\frac{1}{1875}$.

Reduce to their equivalent vulgar fractions: (4) 2; 05; 18; 156; 027027; 285714. (5) 566; 743; 20235; 19:305; 20:02916. (6) 6:18153153; 15:692307692307.

Find the vame correct to six places of dec¹s. of (7) $4\cdot 3 + 16\cdot 45 + 75\cdot 7352$. (8) $3\cdot 23 + 26\cdot 796 + 7\cdot 413$. (9) $3\cdot 8564 - 2\cdot 0387$. (10) $52\cdot 86 - 8\cdot 37235$.

Find the value of (11) $7 \cdot 6 \times 5 \cdot 3$; $3 \cdot 5 \cdot 1 \times 73 \cdot 6$; $13 \times 2 \times 4$ (12) $6 \cdot 7 \div 2 \cdot 6$; $26 \cdot 27 \div 1 \cdot 92 \cdot 6$; $37 \cdot 1 \div 5$; $42 \cdot 0463 \div 1 \cdot 36$.

REDUCTION OF DECIMALS.

103. To reduce a decimal of any denomination to its proper value.

RULE. Multiply the given decimal by the number of units of the next lower denomination which make one of the given denomination, and point off for decimals as many figures in the product, beginning from the right hand, as there are figures in the given decimal.

The figures on the left of the decimal point will represent

the whole numbers in the next denomination.

Proceed in the same way with the decimal part for that denomination, and so on.

Ex. 1. Find the value of '4625 of £1.

Note. If the quantity, the value of whose decimal part is to be found, be a compound quantity, it must be reduced to one denomination before the rule is applied.

Ex. 2. Find the value of 7.405 of 15 mi., 5 fur., 31 po.

15 m., 6 fur., 31 vo. =
$$5031$$
7:405
25155
20124
35217
37254:555 po.
 $5\frac{1}{2}$
2:775
2:775
3:0525 yda.

36
3150
1575
1:8900 in. or = 116 3 14 3 1:36

Ex. 3. Find the value of '5416 of 41 cwt. 1st method.

cwt. lbs
$$4\frac{1}{2}$$
=450 541666 2d. method. $\frac{450}{27083300}$ 5416 of $4\frac{1}{2}$ = $\left(\frac{5416-541}{9000}\text{ of }\frac{9}{2}\right)$ cwt. $\frac{2166664}{16}$ = $\left(\frac{4875}{9000}\times\frac{9}{2}\right)$ cwt. = $\left(\frac{13}{24}\times\frac{9}{2}\times100\right)$ lbs.

11.995200 oz. =243 lbs., 12 oz.

... value = 243 lbs., 12 oz nearly. The 2nd method is the bet ter one in most cases.

Ex. LXIL

- Find the value of, (1) 75 of \$1. '875 of \$5, (3) '625 of \$1. (4) '625 of 1 cwt. '375 of a mi. (5)(6) 175 of a ton. (7) '46875 of £2, 10s.
- (8) ·0625 of 7s. 6d. (9) 3:175 of 1 lb. Troy.
- (10) 4.65 of 41 ac. (11) 10.04 of 2½ ro. (12)2.56 of 10s. 111d.
- (13) 5.00875 of 3 wks. 4 dys. (14) 16:504 days.

- 15) 3 05 of 5 lbs. 29. (16) 3 0085 of 54 la
- (17) 7.034 of 1 ac., 3 ro., 5 po.
- (18) 5.005 of 16 lbs., 1 oz., 6 grs. Troy.
- '19) 3 of \$2. (20) 54 of 16s. 6d. (21) 243 of a ton.
- \$\mathbb{\mathbb{E}}2\) 6.83 of £5. (23) 2.383 of 2\frac{1}{2} lbs. T'y. (24) 6.2 of ac. yd.
- (25) 18.72 of an ac. (26) 2.063 of 1000 guineas.
- (27) £ $\cdot 634375 + \cdot 025$ of $25s + 3 \cdot 16$ of 30s.
- 128) '6 of an ac. + '625 of a ro. + po.
- (29) 6.714285 of 1s. 9d. -.0833 of £7. 4s. +.251190476 of 6s. 8d.
- 104. To reduce a number or fraction of one or more denominations to the decimal of another denomination of the same kind.

RULE. Reduce the given number or fraction to a fraction of the proposed denomination; and then reduce this fraction to its equivalent decimal.

Ex. 1. Reduce \(\frac{2}{6} \) of £1 to the decimal of a guinea.

 $\frac{1}{8}$ of £1 = $\frac{1}{8}$ 8. $\frac{1}{8}$ 8. 1 guin*. = 21s., . . fraction req⁴. = $\frac{1}{8}$ 1. Now $8 \div 21 = 38095238...$. . . dec! req₄. = 380952.

Ex. 2. What decimal of £2 is 11s. $9\frac{3}{4}d$.?

11s. $9\frac{3}{4}d.=567q.$; £2 = 1920q.

: fract*, req*. = $\frac{5.67}{1.925} = \frac{1.89}{0.49}$, :.deg*. req*. = $189 \div 640 = 2953152$; ir thus,

(0.0) 11·8125 11·8125s. to the dec. of £2, by div. by 40 which = £·2953125.

Ex. LXIIL

Reduce.

- (1) 1 qr., 5 lbs. to the decl. of a cwt.
- (2) \$2.50 to the decl. of \$10.
- (3) 3 hrs., 30' to the decl. of a day.
- (4) 3 ro., 11 per. to the decl. of an acre
- (5) 61d. to the decl. of a shilling.
- (6) 31 in. to the decl. of 2 furlongs.
- (7) 2 oz., 13 dwt. to the decl. of a lb.
- (8) 4 lbs., 2 sc. to the decl. of an oz.

- (9) 2 sq. ft. 73 in. to the decl. of a sq. yd.
- (10) 1 lb. Troy to the decl. of a lb. Avoir.

(11) 10s. 9d. to the decl. of a £.

(12) 17s. 7d. to the dec! of a f.

(13) 2 wks., 61 dys. to the decl. of 4 dys. 3 hrs.

(14) 2 lbs., 14 oz. to the decl. of 18 lbs.

Ex. LXIV.

MISCELLANEOUS EXAMPLES.

PAPER I.

- (1) Define a unit; a number. Into what classes are numbers divided? Explain the difference between them. Define Notation and Numeration.
 - (2) Write down in words the following numbers: 70340; 125004321; 5607605213403;

and express by numbers eight hundred and ten thousand four hundred and one; sixty-four billions two millions six hundred and forty-six thousand and two.

(3) (1) Add together one million eighteen thousand two hundred and sixty-nine; twenty thousand nine hundred and seventy-nine; one hundred millions one thousand and fifty; fifty-four billions three thousand; four hundred millions and six; nine hundred and ninety-nine thousand nine hundred and ninety. (2) Subtract 300725 from 400001.

Explain clearly why you carry I when you borrow ten.

- (4) (1) Multiply 268936785 by 5689, and verify by division (2) Divide 27027027027 by 6974, and verify by multiplication.
- (5) The product is 99626417315464, the multiplier 72568; what is the multiplicand?
 - (6) In 12 mi., 2 fur., 6 per., how many inches? Shew that your result is correct.

PAPER IL

- (1) When is a number said to be a multiple of another number? What is a common multiple? What is the least common multiple of two or more numbers? Find L. C. M. of 27, 36, 42, 48.
- (2) Explain the meaning of the signs, +, -, =. When can questions in Addition be performed by Multiplication.

(3) A cask is required to be exactly filled by any one of the following measures: 1 pint, 2 pints, 3 pints, 5 pints, 3 pints, or 9 pints; find the smallest cask for the purpose.

(4) The forewheel of a waggon is 8 feet round, and the hind-wheel fourteen; how many feet will the waggon travel er before each wheel shall have made a number of com-

plete turns? How often will this happen in 1000 feet?

(5) The length and cost of building the undernamed Canadian Canals, were as follows: The Rideau Canal, 1264 miles, \$4380000; the St. Lavrence Canal, 404 miles, \$8550000; the Ottawa Canal, 104 miles, \$1500000; the Chambly and St. Curs Lock, 11½ miles, \$550000; the Welland Canal and feeder, 50½ miles, \$7000000; the Burlington and Desjardins Bridge cost \$560000. Find (1) the total length of the above canals, (2) their total cost, and (3) the average cost per mile, excluding the Furlington and Desjardins Bridge.

(6) Define a vulgar fraction? Distinguish between a vulgar and decimal fraction? Give an example of the dif-

ferent kinds of vulgar fractions?

PAPER III.

 $(1) Simplify (1) <math>2\frac{1}{4} (\frac{1}{6} + \frac{2}{3}) + \frac{4}{5} (\frac{2}{3} - \frac{1}{7}).$ $(2) 2\frac{1}{4} \{ (\frac{1}{6} + \frac{2}{3}) + \frac{4}{5} (\frac{2}{3} - \frac{1}{7}) \}.$

(2) A person who owns \(\frac{1}{2} \) of a steam-vessel, sells \(\frac{3}{2} \) of his share for \$15030; what is the remaining part of his share worth?

(3) Simplify (1) $\frac{7}{12}(3\frac{1}{4}-2\frac{1}{1}) - \frac{1}{2}(\frac{3}{8}-\frac{1}{11}.)$

$$(2) \frac{7}{12} \left\{ (8\frac{1}{4} - 2\frac{1}{2}) - \frac{1}{2} \left(\frac{8}{8} - \frac{1}{11} \right) \right\}$$

(4) A clerk copied '55 of £5 instead of 5.5 of £5, what was the amount of the error?

(5) It takes 87 yds. of earpet, 1.25 yd. wide, to cover a room, how many more yda w:: it take, if the width be 75 yd?

(6) A gave 5 of an orange to B, 3 of what remained

to C; how much of the orange had A left for himself?

PAPER IV.

(1) A drover sold $\frac{1}{3}$ of his flock to A, $\frac{1}{5}$ of the remainder to B, and the rest to C. How many had he at first, supposing C got 32?

(2) Add together 131. 563, and 145 by vulgar and dec

mal fractions, and shew that U. results coincide.

(3) The product of two decimals is 033372; $\epsilon_{a} \ni of$ them is 2.7; find the other.

(4) Add together £27. 6s. 9½d., \$17.22, £19. 5s. 8d., \$198.05, £3. 12s. 7d. The answer to be in decl. currency.

- (5) At a football match there were '875 as many on one side as on the other, and the players on both sides were equal in number to '625 of the lookers on; if there were 21 on the smaller side, how many were playing ou the other side, and how many were looking on?
 - (6) If in a cricket match one side scores '014 of $1\frac{1}{5}$ of $\frac{1}{5\frac{2}{5}}$

of $\frac{5}{7}$ of 4.5 of $\frac{3}{3} + \frac{1}{2}$ of $71\frac{3}{7}$ of the score made by the other side; which side wins?

PAPER V.

(1) Cowes B.6 of what B owes A, B gives C 5s to put the accounts between them all straight. What is B's debt to A?

(2) Out of a bag of silver, I take 50s. more than '5 of the whole sum which it contained; then 30s. more than '2 of what then remained; and then 20s. more than '25 of what then remained; after this 10s. remained. What did

the bag contain at first?

(3) A bath, containing 286 cub. yds. has two inlets A and B, which respectively supply 26 cub. yds. in $3\frac{1}{4}$ hrs., and $12\frac{1}{2}$ cub. yds. in $2\frac{1}{4}$ hrs.; and also an outlet C, which discharges 11:375 cub. yds. in $1\frac{3}{4}$ hrs., if the bath be empty, and A and C open for 12 hrs., and then B also open, in what time will 75 of it be filled?

Make out the following bills :

(4) 500 envelopes at 44 cents per 100, 3 boxes of elastic bands at 33 cents per box, ½ a gross of penholders at 19 cents per doz. 2½ reams of foolscap at 21 cents per quire, 4 dozen quill pens at 9 cents per doz., 13 note books at 27 cents each, and 250 official envelopes at 48 cents per 100.

(5) A loin of lamb (7½ lbs.) at 10 cents per lb., a haunce of mutton (19½ lbs.) at 8 cents per lb., a pork ham (18 lbs.) at 15 cents per lb., 5½ lbs. of suet at 10 cents per lb., and 9

chops at 4 cents each.

(6) 17 yds. calico at 19 cents per yd., 25½ yds. at 55 cents per yd., 3½ yards of flannel at 60 cents per yd., 14 pairs of stockings at 38 cents a pair, and 5 pairs of gloves at \$12 per doz.

SECTION V

RATIO AND PROPORTION.

105. Numbers are divided into two classes, ABSTRACT and CONCRETE. One, or the number one, when the unit does not refer to any particular object, is an abstract number. One, in the expression one pound, when the unit refers to a particular object, viz. "a pound," is a concrete number.

106. We may ascertain the relation which one abstract number bears to another abstract number or one concrete number to another concrete number of the same kind, by expressing the first number as a fraction of the second; thus the relations which 12 bears to 3, and 3 to 12 are expressed by

the fractions $\frac{12}{3}$ or $\frac{4}{1}$, and $\frac{3}{12}$ or $\frac{1}{4}$; also the relations which

12s. bears to 3d., or 144d. to 3d., and 3d. to 12s., or 3d. to 144d. are expressed by the fractions $\frac{144}{3}$ or $\frac{48}{1}$, and $\frac{3}{144}$

107. The relation of one number to another in respect of magnitude is called RATIO. The Ratio of one number to another may be expressed by the fraction which the first is of the second.

108. The Ratio of one number to another is often denoted by placing a colon between them. Thus the ratios of 12 to 3 and 3 to 12 are denoted by 12:3 and 3:12. Hence

it follows that $12:3 = \frac{12}{3}$, and $3:12 = \frac{3}{12}$.

109. The two numbers which form a Ratio are called its terms; the former term is called the ANTECEDENT, the latter the consequent. Since 3d. reduced to the fraction of 12s.

 $=\frac{3}{144}$, it is clear that when we have two concrete numbers of the same kind, but of different denominations, we must, in order to find their ratio, reduce them to one and the same denomination, and may then treat them as abstract numbers

110. When two Ratios are equal, in other words, when they can be expressed by the same fraction, they are said to form a Proportion, and the four numbers are called Pro-PORTIONALS. Thus the ratio of 8 to 9 is equal to that of 24

to 27, for 8: $9 = \frac{8}{9}$, and 24: $27 = \frac{24}{27} = \frac{8}{9}$ The Ratios being equal, Proportion exists among the numbers 8, 9, 24, 27;

and those numbers are Proportionals.

111. The existence of Proportion between the numbers 8, 9, 24, 27 is denoted thus, 8:9=24:27, or 8:9:24:27which is usually read thus, 8 is to 9 as 24 is to 27.

112. In any Proportion, as 8:9::24:27, the product of the 1st and 4th, i.e. the extreme terms = the product of the 2nd and 3rd, i.e. the mean terms;

$$\frac{8}{9} = \frac{24}{27}; \dots \frac{8}{9} \times 9 \times 27 = \frac{24}{27} \times 9 \times 27, \text{ or } 8 \times 27 = 24 \times 9.$$

If four numbers be proportionals when taken in a certain order, they will also be proportionals when taken in the contrary order. For instance, 8, 9, 24, 27 are proportionals;

$$\therefore \frac{8}{9} = \frac{24}{27}; \dots 1 \div \frac{8}{9} = 1 \div \frac{24}{27}; \text{ or } \frac{9}{8} = \frac{27}{24}, \text{ or } \frac{27}{24} = \frac{9}{8};$$
$$\therefore 27 : 24 :: 9 : 8.$$

114. If any three terms of a proportion be given, the renaining term may always be found.

For since in any Proportion

1st term × 4th term = 2nd term × 3rd term;

.. 1st term =
$$\frac{2\text{nd } \times 3\text{rd}}{4\text{th}}$$
, 2nd term = $\frac{1\text{st } \times 4\text{th}}{3\text{rd}}$,

3rd term = $\frac{1\text{st } \times 4\text{th}}{2\text{nd}}$, 4th term = $\frac{2\text{nd } \times 3\text{rd}}{1\text{st}}$.

Ex. 1. Find the 4th term in the propertion 2, 3, 18.

2:3::18:4th term; ... 4th term =
$$\frac{3 \times 18}{2}$$
 = 27.

Ex. 2. Find the 2nd term in the proportion 8, 32, and 24

8; 2nd term :: 32: 24; ... 2nd term =
$$\frac{8 \times 24}{32}$$
 = 6.

Ex. LXV.

Find the 4th term in each of the following proportions:

- (1) 4:9:12: (2) 32:9:24:
- (3) 4:6::10: (4) $\frac{1}{2}:\frac{1}{3}::\frac{1}{4}:$
- (5) *05: *8:: *79: (6) 3:10:: 4.5 } Find the 2nd term in each of the proportions:

(7) ϕ : :: $\frac{1}{2}$ ϕ : :: $\frac{1}{2}$ ϕ . (8) 1·2: :: 1·3: ·39.

Find the 1st term in each of the proportions:

(9) $: \frac{9}{14} : \frac{7}{13} : \frac{1}{3}$. (10) $: 4.22 : 17.6 : 23 \frac{3}{6}$.

RULE OF THREE.

115. The RULE OF THREE is a method by which we are enabled, from three numbers which are given, to find a fourth which shall bear the same ratio to the third as the second to the first; in other words, it is a Rule by which, when three terms of a proportion are given, we can determine the fourth.

116. Rule. Find out of the three quantities which are given, that which is of the same kind as the fourth or required quantity; or that which is distinguished from the other terms by the nature of the question: place this quantity as the third term of the proportion.

Now consider whether, from the nature of the question, the fourth term will be greater or less than the third; if greater, then put the larger of the other two quantities in the second term, and the smaller in the first term; but if less, put the larger in the first term and the smaller in the

second term.

Take care to reduce the first and second terms to one and the same denomination, and also to reduce the third so that it may be wholly in one denomination; remembering, however, that if the quantities involved be all of the same kind, it is unnecessary to reduce all the three terms to the same denomination, but only the first and second terms to one and the same denomination, and the third to a single denomination, which will not necessarily be the same as the former. Nhen the terms have been properly reduced, multiply the second and third together, and divide by the first, treating all three as abstract numbers. The quotient will be the answer to the question, in the denomination to which the third term was reduced.

If 19 bushels of potatoes cost \$15.20, how many bushels can be bought for \$83.20? Since 19 bush is of the same kind as the req. term, viz., bus., we make 19 bus. the 3.4 term; since \$83.20 can buy more bus, than \$15.20, we make \$83.26 the 2.4 term, and \$15.20 the la. term:

\$ c. \$ c. bus. 15.20:83.20::19:no. of bus. req4.

or 1520 cts. : 8320 cts. :: 19 bus. : of bus. reqa.

... no. of bus, req⁴. $=\frac{8320 \times 19}{1520} = 104$.

Ex. 2. A gentleman hired a servant for the year 1865 for £32. 13s. 11½d., the man left his service on the evening of the ast day of June: what amount of wages ought to be paid to him?

From Jan. 1 to June 30, both included, there are (31 + 28

+31 + 30 + 31 + 30) days = 181 days;

We place £32. 13s. 11½d., the given quantity of the req. kind, in the 3rd. term; wages for 181 days will be less than wages for 365 days, ... place 181 days in the 2rd. term, and 365 days in the 1rd. term.

days, days. £ s. d. .: 365: 181:: 32 13 11½: req⁴. am⁴. of wages.

or 365 days: 181 days :: 313907......in q.

... req⁴. am⁴. of wages = $\frac{31390 \times 181}{365} q$. =£16. 4s. 3½d.

Ex. 3. A bankrupt can pay 9s. $0\frac{1}{2}d$. in the £, and his assets amount to £1069. 3s. $6\frac{1}{2}d$.; find the amount of his debts.

For every asset of 9s. $0\frac{1}{2}d$. he owes £1, ... place £1 in the

3rd term.

9s. 0½d.: £1069. 3s. 6½d.:: £1: am'. of debts in £'s, or 217 half-pence: 513205 half-pence:: £1: am'. of debts in £'s;

... am'. of debts in £'s = $\frac{513205}{217}$ = 2365

Ex. 4. If '0625 of 1 lb. cost '458s.; what will '075 of a ton cost?

or $0625: 075 \times 20 \times 112: 458: \text{req}^4$. price in shillings

:. price = $\frac{100 \times 100 \times 100}{10625}$ s. = £61, 11s. 1.248d.

Ex. 5. A owned $^4_{17}$ ths of a ship, and sold $^4_{17}$ of $^2_{1}$ of his share for £12 $^4_{18}$; what was the value of $\frac{1\frac{1}{4}}{4\frac{1}{4}}$ of $^2_{1}$ ths of the versel?

 $^{8}_{17}$ of $^{8}_{3}$ of $^{4}_{17}:\frac{1^{\frac{1}{4}}}{4^{\frac{1}{4}}}$ of $^{8}_{8}::£12^{\frac{4}{4}}:req^{4}$. value in £'s,

or
$$\frac{2\times4}{11\times3\times17}$$
: $\frac{5}{4}\times\frac{4}{17}\times\frac{2}{5}$:: £\frac{400}{33}: req⁴. value in £'s;

... req⁴. value in £'s =
$$\frac{400 \times 2}{33 \times 17} \times \frac{11 \times 3 \times 17}{2 \times 4} = 100$$
.

Note 1. There are certain examples in which, at first sight, more than three terms appear to be given, but they, in certain cases, come under this Rule, as in the following instances:

Ex. 6. If the carriage of 5 cwt., 7 lbs., for 84 miles cost £3. 18s. 4d., what will it cost to have 21 cwt., 1 qr., 14 lbs. carried the same distance?

84 miles may be left out of consideration, the distance in

both cases being the same.

:.5 cwt., 7 1 :: .21 cwt., 1 qr., 14 lbs. :: £3.18s.4d. : req⁴. cost; whence, req⁴. cost = £16. 10s. 8\frac{3}{2}d. \frac{5}{2}q.

Ex. 7. If 12 men can reap a field in 4 days, in what time can the same work be performed by 32 men?

32 men require less than 4 days to perform the work;

∴ .32 : 12 :: 4 days : req⁴. time in days;
∴ req⁴. time =
$$\frac{12 \times 4}{32}$$
 days = $1\frac{1}{2}$ days.

Note 2. Examples such as the following are easily worked by Rule of Three.

Ex. 8. A gentleman after paying an income-tax of 7d. in the £, has £248. 10s. 8d.; what was his gross annual income! After paying inc. tax on £1, he had £1 less 7d., or 19s. 5d.

Ex. 9. A hare, pursued by a greyhound, was 130 yards before him at starting; whilst the hare ran 5 yards the dog ran? yards; how far had the hare gone when she was caught by the greybound?

Since the dog gains 2 yds. on every 5 yds. which the hare

runs, we require to find how many yards the hare must run see the dog to gain 130 yds.

•'. 2 yds.: 130 yds.:: 5 yds.: no. of yds. the hare must run;
•'. so. of yds. req*. = $\frac{130 \times 5}{2}$ = 325.

Ex. LXVI.

- (1) If 8 bushels of wheat cost \$16, what will 24 bushels sont at the same rate?
- (2) If 2 bushels of oats cost \$1.10, how much will 33 bushels cost?
- (3) If 9 bushels clover seed cost \$36, how much will 4 bus. 20 lbs. cost?
- (4) When oats are selling at 55 cents a bushel; how many bushels can be bought for \$21.25?
- (5) The price of a bushel of pease being 84 cents; how many bushels can be bought for \$17.20?
- (6) Find the value of a silver salver, weighing 21 lbs., 4 os. at 6s. 5d. an oz.
- (7) How much cheese at 16 cts. per lb. can be bought for \$462.36?
- (8) A bankrupt, who owes \$23856, can pay \$10496.64; what will be the dividend in the \$?
- (9) A pensioner received \$106.14 for the year 1864; find the amount of his daily pension.
- (10) I mile of road cost \$393.75; what will 20 mi., 5 fur., 22 yds. of the same kind of road cost?
- (11) What weight of sugar may be bought for \$449.28, when the cost of 6 cwt., 2 qrs. is \$133.12.
- (12) The taxes on a house rated at \$183.75 amount to \$32.15, the taxes on another house in the same village amount to \$286.66\frac{1}{2}; find the rateable value of the 2nd house.
- (13) A bankrupt's debts amount to \$10000, and ris property to \$3875, what will each of his creditors lose in the \$?
- (14) A ship was provisioned for a crew of 84 men for 5 months; how much longer would the provisions last, if a arew of only 60 men were taken on board?
 - (15) A merchant exchanged 1134 yds. of velvet for 5313

yds. of silk at 3s. $4\frac{1}{2}d$. a yd.; find the value of the velvet . yd.?

- (16) What are the effects of a bankrupt worth, whose debts amount to £3057. 12s., and who can pay 17s. 6d. in the £?
- (17) A man on the average walks over 10 ft., 8 in. in 4 steps, what number of steps will be take between two places, a distance of 1 mi., 1280 yds. apart?
- (18) If 31 ac., 2 ro, 9 po., 21 yds. of ground cost £3025 12s. $4\frac{1}{2}d$., what will be the price of 49 ac., 3 ro., 38 po., 23 yds. of ground of the same quality?
- (19) A bankrupt pays 59 cts. in the \$; what will be lost on a debt of \$13675?
- (20) How many minutes must a bey, who runs 6 mi. an hour, start before another boy, who runs $7\frac{1}{2}$ mi. an hour in order that they may be together at the end of 10 mi.?
- (21' Two boats start in a race, and one of them gains 5 ft. upon the other in every 55 yds.; how much will it have gained at the end of half a mile?
- (22) How many pairs of mits at 45 cts. a pair should be exchanged for 36 dozen pairs of stockings at 55 cts. a pair?
- (23) How many men would perform in 168 days a piece of work, which 108 men can do in 266 days?
- (24) If an incorporated village be rated at \$12571.87½ and a rate be granted of \$419.06½; how much is the rate in the \$? How much will be paid by a house rated at \$1734.37½.
- (25) A gentleman's income in 1863 was \$2500, out of which he saved \$994.37½; find his average daily expenditure.
- (26) If 100 men can finish a piece of work in 27 days, how many men will finish it in 20 days?
- (27) A special train on the Grand Trunk Railway, which travels at the uniform rate of 44 ft. in a second, leaves Belleville for Toronto, a distance of 109 miles, at 8 o'clock A. M.: at what time will the train reach Toronto.
- (28) A bankrupt owes to one creditor a certain sum, to each of two others \$1250, to each of three others \$816; his property is worth \$1718.75, and he can pay 22 cts. in the \$. How much will the first creditor lose?
 - (29) If, when wheat is 42s. a qr. (8 bus.), the 4 lb. loaf

costs $4\frac{1}{2}d$., what ought the 4 lb. loaf to cost when wheat is 70s. a qr.?

- (30) In what time ought 10 men to perform the same work, which 5 men and 5 boys can perform in 15 days, it being given that 3 men can verform the same amount of work as 5 boys?
- (31) Find a 4th proportional to 1 lb., 10 oz., 10 dwts.; 1 oz.; and £6. 3s. 9d.
- (32) How much might a person have spent in Jan., 1864, who wished to save in that year \$250 out of an income of \$2034.50?
- (33) A person, after paying an income-tax of 6d. in the £, has £877. 10s. left, find his original income.
- (34) Find (1) the income which pays £29. 3s. 4d. tax at the rate of 7d. in the £; (2) the income from which, after paying tax at the same rate, the remainder is £932.
- (35) A piece of gold at £3. 17s. $10\frac{1}{2}d$. per oz. is worth £150; what will be the worth of a piece of silver of equal weight at 54s. 6d. per lb.?
- (36) A certain piece of work was to be done by 25 men n 16 days; after 4 days 15 men go away; how long will it take the rest of the men to finish the work?
- (37) A person after paying for the 1st half of a year an income-tax of 1 ct. in the \$, and for the 2nd half one of 1½ cts. in the \$ on his income, bas \$1855 left; what was the income on which he paid?
- (38) If ? of a qr. of wheat cost 54s., what will be the price of ? of a bus.?
 - (39) If 13 of a cwt. cost £7 3s., what will 11 of a ton cost?
- (40) If $\frac{1}{102}$ of $\frac{2}{3}$ of $2\frac{1}{2}$ of 40 lbs. of beef cost $1\frac{2}{100}d$., how many lbs. can be bought for £1. 6s. 6d.?
- (41) A clock marks the true time on Sunday morning at 6 o'clock, and on Tuesday at noon it has gained 24 minutes, what will be the true time when it shews 1 o'clock on Saturday afternoon?
- (42) The hour and minute hands of a watch are together at 12 o'clock, when will they next be together?
- (43) If 5 lbs. of sugar cost 0703125 of \$4, what will 0625 cwt. of the same sugar cost?
 - (44) A certain piece of work can be done in 18 days by

4 men, 7 women, or 9 boys; how long will the same work occupy 5 men, 4 women, and 2 boys?

- (45) If after selling \$ths of an estate, I sell \$ of \$ of the remainder for 1\$ of \$ of £600\$, what is the value of \$rds of t?
- (46) What will be the value of a gold cup weighing 2.683 lbs.; when l oz. of it is worth £4.09?
- (47) 4 men and 5 boys earn \$22.12 in 7 days, and 3 men and 8 boys earn \$28.98 in 9 days; in what time will 12 men and 12 boys earn \$186.48?
- (45) A can do a piece of work in 5 hours, B in 9 hours, and C in 15 nours. How long will it take C to finish the work, after A has worked at it for 40 minutes, and B for $1\frac{1}{2}$ hours?
- (49) If a garrison of 1500 men have provisions for 13 mo., how long will their provisions last, if at the end of 2 mo. they be reinforced by 700 men?
- (50) Two men start at 8.30 A.M, one from Toronto and the other from Whitby, a distance of 30 miles, and they approa h each other at the rates of 4½ and 3 miles an hour; at what time will they meet, and at what distance from a place, which is 2 miles nearer to forento than Whitby?
- (51) Two trains respectively 210 feet and 180 feet in length are going in opposite directions, the first at the rate of 24 miles per hour, and the other at the rate of 27 miles per hour; and how long they will take to pass each other?

DOUBLE RULE OF THREE.

- 117. The DOUBLE RULE OF THREE is a shorter method of working out such questions as would require two or more applications of the Rule of Three
- 118. For the sake of convenience, we may divide each question in the Double Rule of Three into two parts, the supposition and the demand; the supposition being the part which expresses the conditions of the question, and the demand the part which mentions the thing demanded or sought. In the question, "If the carriage of 15 cwt. for 17 miles cost \$21, what would the carriage of 21 cwt. for 16 miles cost?" the words "if the carriage of 15 cwt. for 17 miles cost \$21," form the supposition; and the words "what would the carriage of 21 cwt. for 16 miles cost!" form the demand

Adopting this distinction, we may give the following Rule for working out examples in the Double Rule of Three.

119. Rule. Take from the supposition that quantity which corresponds to the quantity sought in the demand; and write it down as a third term. Then take one of the other quantities in the supposition and the corresponding quantity in the demand, and consider them with reference to the third term only (regarding each other quantity in the supposition and its corresponding quantity in the demand as being equal to each other); when the two quantities are so considered, if from the nature of the case, the fourth term would be greater than the third, then, as in the Rule of Three, put the larger of the two quantities in the second term, and the smaller in the first term; but if less, put the smaller in the second term, and the larger in the first term.

Again, take another of the quantities given in the supposition, and the corresponding quantity in the demand; and retaining the same third term, proceed in the same way to make one of those quantities a first term and the other a

second term.

If there be other quantities in the supposition and demand,

proceed in like manner with them.

In each of these statings reduce the first and second terms to the same denomination. Let the common third term be also reduced to a single denomination if it be not already in that state. The terms may then be treated as abstract numbers.

Multiply all the first terms together for a final first term, and all the second terms together for a final second term, and retain the former third term. In this final stating multiply the second and third terms together and divide the product by the first. The quetient will be the answer to the question in the denomination to which the third term was reduced.

Ex. 1. If 5 men earn £18, 15s, in 12 weeks, how much will 16 men earn in 20 weeks?

By the Rule,

5 men : 16 men 12 wks. : 20 wks. ::£18 15x 16 men will earn more money than 5 men in a given sime; in 20 wks. more money will be earned than in 12 wks. by 2 John no. of men.

... 5 x 12 : 16 x 20 :: 3758 : no. of shillings req 4.;

: no. of shillings reqd. = $\frac{16 \times 20 \times 375}{5 \times 42}$ = 2000s. =£100.

Ex. 2. If 16 horses eat 56 bus. of corn in 32 days, in how many days will 8 horses eat 84 bus.?

:: 32 days A given no. of bus. will last 8 horses more days than 16 8 horses: 16 horses) 56 bus. : 84 bus. horses; 84 bus. will last a ... no. days req⁴. = $\frac{16 \times 34 \times 32}{8 \times 56}$ = $\frac{16 \times 94 \times 32}{96 \times 96}$ no. of horses more days than 56 bus.

Ex. 3. If 15 pumps, working 8 hours a day, can raise 1260 tons of water in 7 days; how many pumps, working 12 hours a day, will be required to raise 7560 tons of water in 14 days?

Fewer pumps works. 12 hrs. 12 hrs. : 8 hrs. 1260 tons: 7560 tons : 15 pump a day are reqd. to raise a 14 days: 7 days given no. of days than if they worked 8 hrs a day; ... no. of pumps reqd. $= \frac{8 \times 7560 \times 7 \times 15}{12 \times 1260 \times 14} = 30.$ more pumps are reqd. to raise 7560 tons than to raise 1260 tons in a given no. of

days, works. a given no. of hrs. each day; fewer pumps are req. works. for 14 days a given no. of hrs. each day, to raise a given weight of water, than if they worked only for 7 days.

Ex. 4. If 25 men can perform a piece of work in 16 days working 12 hours a day, in what time will 20 men perform a similar piece of work 4 times as large, when they work only 8 hours a day?

Call the 1st piece of work 1, then the 2nd piece will = 4.

20 men : 25 men 1 : 4 8 hrs. : 12 hrs. : 16 days. $= \frac{25 \times 4 \times 12 \times 16}{20 \times 8} = 120.$

Ex. 5. A contractor engages to make a road 51 mi. long in 160 days; but after employing 135 men upon it for 100 days, he finds that only 3 mi., 700 yards are completed; how many extra men must he employ in order to complete his contract 1

 $5\frac{1}{2}$ mi. -3 mi., 700 yds. =9680 yds. -5980 yds. =3700 yd. .. no. of men reqd.

3700 × 100 × 135 men_ 3700 × 100 × 135 5980 × 60

. . 140 men must be employed, or 6 additional men.

Ex. LXVII.

- (1) If 10 sacks of oats supply 12 horses for 4 weeks, how long will 15 sacks supply 9 horses?
- (2) If 42 men finish a work in 36 days, how many will finish twice as great a work in 27 days?
- (3) If 60 men in 36 days finish a work, in how many lays will 135 men finish four times as great a work?
- (4) If 104 tons carried 34 miles cost \$87.36, what will 102 tons carried 122 miles cost?
- (5) If a man with a capital of \$100000 gain \$2500 in 3 months, what sum will he gain with a capital of \$1500000 in 7 months?
- (6) If 21 cwt. be carried 40 miles for \$2.80, now far ought 7 cwt. to be carried for \$4.06?
- (7) If 7 horses be kept 20 days for \$70, what will it cost to keep 45 horses for 9 days?
- (8) If 140 norses eat 560 bus, of oats in 16 days, how many torses may be kept for 24 days on 1200 bus, of oats?
- (9) If with a capital of \$5000 a person gains by trade \$250 in 16 months, in how many months will be gain \$625 with a capital of \$2000?
- (10) It a regiment of 1878 soldiers consume /02 qrs. of wheat in 336 days, how many qrs. will an army of 22536 men consume in 112 days?
- (11) If 6 horses can plough $17\frac{1}{2}$ acres in 4 days, how much land can 24 horses plough in $2\frac{1}{2}$ days:
- (12) If £240 he paid for bread for 49 persons for 20 mo., when wheat is 48s. a qr.; how long will £234 find bread for 91 persons, when wheat is £2. 16s. a qr.?
- (13) If 100.8 lbs. of dour support 20 men for 3 days, how many men will 46.305 cwt. support for 7.35 weeks?
- (14) If 26 men can reap a field of 85 ac. in 12 days, how nany men will reap another similar held one-half the size of the 1st field in one-seventh part of the time?
- (15) 3 men can do a piece of work in 6 days, if they work 10 hours a day; how long will it take 16 men to do twice the amount of work, when they are working at it 9 hours a day?
- (16) If the wages of 25 men amount to £76, 13s, 4d, in 16 days, how many men must work 24 days to seceive

- £103. 10s., the daily wages of each of the latter being one half that of each of those of the tormer?
- (17) If 6664 men, on half rations, consume 357 qrs. of wheat in 57 days, how many qrs. of wheat will 798 men, or full rations, consume in 119 days?
- (18) If the 16 cts. loaf weighs 3.35 lbs., when wheat is \$1.14 a bus., what ought to be the price of wheat per bus., when 47.5 lbs, of bread cost \$3.20.?
- (19) If when wheat is \$14.40 a qr., the 12 cts. loaf weighs 4lbs., what should be the price of wheat per qr., when 25 lbs. or bread cost 37½ cts.?
- (20) It 4 men, each working 8 hrs. a day, take 11 days to pave a road 220 yds. long, and 35 ft. broad; how many days will 6 men, each working 12 hrs. a day, take to pave a road 175 yds. long, and 36 ft. broad?
- (21) It 100 horses consume a stack of hay 20 ft. long, 11 ft., 3 in. broad, and 31 ft., 6 in. high, in 9 days, how long will a stack 18 ft. long, 5 ft. broad, and 14 ft. high supply 80 horses?
- (22) It 3 men can dig a ditch 105 yds. long, 4 ft. deep, and 5 ft. wide in 10 days, how long will it take 5 men to dig a ditch 175 yds. long, 4½ ft. deep, and 6 ft. wide?
- (23) If the 3 cts. loaf weighs 1 lb. 11 oz. 12 drs. when wheat is \$1.80 per bu., what ought the 12 cts. loaf to weigh when wheat is \$4.26 per bus.?
- (24) It 5 horses require as much corn as 8 ponies, and 15 prs. last 12 ponies for 64 days, how many horses may be kept 48 days for £41. 5s. when corn is 22s, a qr.?
- (25) A contractor agrees to execute a certain piece of work in a certain time. He employs 55 men, who work 9 hrs. daily. When \$\frac{1}{2}\$ths of the time is expired, he finds that only \$\frac{1}{2}\$ths of the work is done. How many men must be employ during the remaining part of the time, working 11 hrs. daily, in order that he may fulfil his contract?
- (26) If 5 pumps, each having a length of stroke of 3 feet, working 15 hours a day for 5 days, empty the water out of a mine; what must be the length of stroke of each of 15 pumps which, working 10 hours a day for 12 days, would empty the same mine, the strokes of the former set of pumps being per formed 4 times as fast as those of the latter?

PRACTICE.

120. An Aliquot part of a number is such a part as, when taken a certain number of times, will exactly make up that number.

Thus, 4 is an aliquot part of 12; 6s. of 18s.

TABLES OF ALIQUOT PARTS.

Industry Va AL	dejour laters.
Parts of a cut. (100 1)s	Parts of a cut. (112 lbs.)
50 lbs. or 2 qrs. = $\frac{1}{2}$ cwt. 25 lbs. or 1 qr. = $\frac{1}{4}$ " 20 lbs. = $\frac{1}{5}$ " 10 lbs. = $\frac{1}{2^{1}0}$ " 5 lbs. = $\frac{1}{2^{1}0}$ " Note. The parts of a \$ the same as of the cwt. (100 lbs).	56 lbs. or 2 qrs. = ½ cwt. 28 lbs. or 1 qr. = ½ 16 lbs. = ½ 14 lbs. = ½ 7 lbs. = ½ 4 lbs. = ½ 2 lbs. = ½
Parts of a £1.	Parts of a shilling.
$\begin{array}{rcl} 10s. & = & \frac{1}{2} \pounds 1. \\ 6s. 8d. & = & \frac{1}{3} \text{ "} \\ 5s. & = & \frac{1}{4} \text{ "} \\ 4s. & = & \frac{1}{6} \text{ "} \\ 2s. 6d. & = & \frac{1}{6} \text{ "} \\ 2s. & = & \frac{1}{10} \text{ "} \\ 1s. 8d. & = & \frac{1}{15} \text{ "} \\ 1s. 3d. & = & \frac{1}{15} \text{ "} \\ 1s. & = & \frac{1}{15} \text{ "} \\ 1s. & = & \frac{1}{15} \text{ "} \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

Note. In working examples in Practice, the above tables will often have to be varied; the knowledge, which the scholar now has, will render him expert in taking such aliquot parts as he may require in any particular example.

121. Practice is a short method of finding the value of any number of articles by means of Aliquot Parts, when the value of a unit of any denomination is given. Practice may be divided into Simple and Compound.

SIMPLE PRACTICE.

122. In this case the given number is expressed in the same denomination as the unit whose value is given: as, for instance, 27 bushels at \$1.30 per hashed

The Rule for Simple Practice will be easily shewn by the following examples.

Ex. 1. Find the value of 1296 things at 16s. 101d. each. The method of working such an example is the following: If the cost of the things be £1 each:

then the total cost = £1296. .. cost at £. 10s. 0d. each = $\frac{1}{2}$ of the above sum. ... = 648. 5s. 0d.each = $\frac{1}{2}$ the cost at 10s. each .. = 324. 1s. 3d. each = $\frac{1}{4}$ the cost at 5s. each. .. = 81. 0s. 71d. each = $\frac{7}{2}$ the cost at 1s. 3d. each = 40 . 10 . 0

... by adding up the vertical columns, cost at 16s. 101d. each =£1093.10.0

The operation is usually written thus:

1296 . 0.0 = cost at £l each. $10s. = \frac{1}{2}$ of £1. $5s_{\bullet} = \frac{1}{5}$ of $10s_{\bullet}$ $648 \cdot 0 \cdot 0 = \text{cost at } 10s. \text{ each.}$ 18. $3d. = \frac{1}{4}$ of 5s. 324 : 0 . 0 = cost at 5s. each. $7\frac{1}{2}d. = \frac{1}{6}$ of 1s. 3d. 81. $0.0 = \cos t$ at 1s. 3d. each. 40.10.0 = cost at $7\frac{1}{2}d$, each. £1093 . 10 . 0 = cost at 168. $10\frac{1}{2}d$. each

Note. The student must use his own judgment in select ing the most convenient 'aliquot' parts; taking care tha the sum of those taken make up the given price of the unit.

Ex. 2. Find the value of 825 bushels of wheat at \$1.24 per bus.

If 1 bus. cost \$1, cost of 825 bus. = \$825 at \$1 each.

\$\$25.00 = value at \$1 each.165.00 = value at 20 cts. each. 20 cts. = $\frac{1}{5}$ of \$1. $10 \text{ cts.} = \frac{1}{2} \text{ of } 20 \text{ cts.}$ 82.50 = value at 10 cts. each.\$1072.50 = value at \$1.30 each.

Ex. LXVIII.

Find the value of.

- (1) 75 at \$2.25.
- (3) 910 at \$1.75.
- (5) 1075 at \$3.25. (7) 397 at £1. 1s.
- (9) 1324 at \$3.75.
- (11) 973 at 16s. 81d.

- (2)105 at \$1.50.
- (4) 876 at \$2.20.
- (6) 1278 at \$1.874.
- (8)250 at £2. 8s.
- (10)
 - 2678 at £2. 7s. 6d.
- (12)236 at £7. 5s. 114d

(13) 9978 at £8. 13s. 8½d. (14) 15'39 at £9. 17s. 9¾d

(15) 27835 at \$9.62½. (16) 37832 at \$18.90.

(17) A bankrupt whose debts amount to \$250215 pays 29 cts. in the dollar; what are his effects worth?

(18) A gentleman's gross income is \$12815, his rates and

taxes amount to 25 cts. in the \$, find his net income.

(19) What will be the loss on a debt of £4970, if a divi-

dend of 8s. $10\frac{1}{2}d$. in the £ be paid? (20) What will be the total cost of $83\frac{1}{2}$ yds. of calico @

1112d. per yd., of $57\frac{3}{4}$ yds. of flannel @ 1s. 10d. a yd., and of 118 yds. of ribbon @ $9\frac{5}{4}d$. a vd.?

COMPOUND PRACTICE.

123. In this case the given number is not whony expressed in the same denomination as the unit whose value is given; as for instance, 1 cwt. 2 qrs., 14 lbs. at \$10.24 per cwt.

The Rule for Compound Practice will be easily shewn from the following examples.

Ex. 1. Find the value of 60 cwt., 3 qrs., 5 lbs. of sugar @ \$8.50 per cwt

The method of working such an example is the following

The value of 1 cwt. of sugar being \$8.50;

**Nature of 60 cwt. =
$$(\$5.50 \times 60)$$
 = $\$510.00$

2 qrs. = $\frac{1}{2}$ (value of 1 cwt.)

= $\frac{1}{2}$ ($\$5.50$) = $\$4.25$

1 qr. = $\frac{1}{2}$ (value of 2 qrs.)

= $\frac{1}{2}$ ($\$4.25$) = $\$2.12\frac{1}{2}$

5 lbs. = $\frac{1}{5}$ (value of 1 qr.)

= $\frac{1}{5}$ ($\$2.12\frac{1}{2}$) = $\$0.42\frac{1}{2}$

'neretore adding up the vertical columns, value of 60 cwt. 3 qrs., 5 lbs. -\$516.80

The oper tion is usually written thus:

\$516.80 = value of 60 cwt., 3 ars., 5 lbs.

Ex. 2 Find the value of 319 cwt., 3 qrs., 16 lbs., at £8 12s. 6d. per cwt.

2 qrs. =
$$\frac{1}{2}$$
 cwt.

2 . 12 . 6 = value of 1 cwt.

10

26 . 5 . 0 = value of 10 cwt.

4

105 . 0 . 0 = value of 40 cwt.

8

840 . 0 . 0 = value of 320 cwt.

2 . 12 . 6 = value of 1 cwt.

8

840 . 0 . 0 = value of 320 cwt.

1 qr. = $\frac{1}{2}$ of 2 qrs.
1 qrs. = $\frac{1}{2}$ of 1 qr.
2 lbs. = $\frac{1}{7}$ of 14 lbs.

9 . 0 . 13 . 1 $\frac{1}{2}$ = value of 1 qr.
1 dbs. = $\frac{1}{2}$ of 1 qr.
2 lbs. = $\frac{1}{7}$ of 14 lbs.

6 . 0 . 1 $\frac{1}{4}$ = value of 2 lbs.

£839 . 14 . 4 $\frac{1}{2}$ = value of 319 cwt.

Ex. LX.

3 qrs., 16 lbs.

Find the value of

- (1) 55 bus., 25 lbs. wheat @ \$1.20 per bushes.
- (2) 16 cwt. 2 grs., 20 lbs. of sugar @ 10 cts. per lb.
- (3) 96 ac., 2 ro., 10 per. at \$15.50 per ac.
- (4) 2 lbs., 8 oz., 13 dwt. at 7s. 1d. per oz.
- (5) 15 yds., 2 ft., 7 in. at 12s. 6d. per yd.
- (6) 28 sq. yds., 7 ft., 110 in. at £1. 7s. per sq. ft.
- (7) 11 mls., 3 fur., 55 yds., at \$11000 per mile.
- (8) What is the value of 5 tubs of butter, each of 2 of them containing 57½ lbs., and each of the rest 73½ lbs., at 525 per cwt.?
 - (9) What will 3460 ft. of timber cost at \$5 per 100 ft.?
 - (10) What will 24650 bricks cost at \$4 per 1000?
 - (11) What will 46590 ft. lumber cost at \$10.25 per 1000 ft.? Find the amount of each of the following bills:
- (12) 17 \S yds. calico at 19 \S cts. a yd., 35 \S yds. tiannel at 55 \S cts. a yd., 96 \S yds. sheeting at 70 \S cts. a yd., 104 \S yds. of Holland at 32 \S cts. a yd., 12 \S yds. of ribbon at 17 \S cts. a yd.

(13) 251 lbs. of beef at 121 ets. a lb., 1911 veal at 11 cts

a ib., 35 $\frac{7}{6}$ lbs. of pork at S_2^1 cases a lb., $17\frac{1}{2}$ lbs. lamb at $6\frac{1}{2}$ cts a lb.

(14) 17 $\frac{3}{5}$ lbs. crushed sugar at $12\frac{1}{2}$ cts. a lb., $18\frac{3}{4}$ lbs. cheese at 17 $\frac{1}{2}$ cts. a lb., $5\frac{5}{15}$ lbs. of tea at 75 cts. a lb., $10\frac{5}{7}$ lbs. coffee at 40 cts. a lb., $7\frac{3}{4}$ lbs. honey at 25 cts. a lb.

Note 1. The scholar should bring the last three questions

in the form of a bill, to the master.

INTEREST.

124. INTEREST (Int.) is the same of money paid for the loan or use of some other sum of money, lent for a certain time at a fixed rate; generally at so much for each \$100 for one year.

The money lent is called THE PRINCIPAL.

The int. of \$100 for a year is called THE RATE PER CENT.

The principal + the interest is called the AMOUNT.

Interest is divided into Simple and Compound When inverest is reckoned only on the principal or sum lent, it is SIMPLE INTEREST.

When the interest at the end of the first period, instead of being paid by the borrower, is retained by him and added as principal to the former principal, interest being calculated on the new principal for the next period, and this interest again, instead of being paid, is retained and added on to the last principal for a new principal, and so on; it is COMPOUNL INTEREST.

SIMPLE INTEREST.

125. To find the interest of a given sum of money at a given rate per cent. for a year.

RULE. Multiply the principal by the rate per cent., and

divide the product by 100.

Note 2. The int. for any given number of years will be found by multiplying the int. for 1 year, by the number of years; and the int. for any part of a year may be found from the int. for 1 year, by Practice, or by the Rule of Three.

Note 3. If the interest has to be calculated from one given day to another, as for instance from the 30th of Jan. to the 7th of Feb., the 30th of Jan. must be left out in the calculation, and the 7th of Feb. must be taken into account, for the borrower will not have had the use of the money for one tay till the 31st of Jan.

Note 4. If the amount be required, the int. has first to be

found for the given time, and the principal has then to be added to it.

Ex. 1. Find the simple int. of \$250 for one year, at 9 per cent. per annum.

By the Rule.

or by the Rule of Three.

\$250 9 \$100 : \$250 :: \$9 : Int. req4.

\$22.50 . Int. = \$22.50

... Int. req^d. =
$$\frac{250 \times 9}{100}$$
 = \$22.50.

Ex. 2. Find the amount of £1376. 11s. 3d. at 43 per cent from Apr. 6 to Aug. 30.

$$^*1376 \cdot 11 \cdot 3$$
 3
 $4) \underline{4129 \cdot 13 \cdot 9}$
 $\underline{£1032 \cdot 8 \cdot 5}$

1032 .

C65 38 . 13 . 51

20

3. 7·73 12

.•. Int for 1 yr. = £65 7s. 8.8125d.

d. 8.8125 since 51d. = 5.25d.

No. of days from Apr. 6 to Aug. 30 = 24 + 31 + 30 + 31 + 30= 146:

.:. 365 days: 146 days:: £65. 7s. 8.8125d : int. req4. or 5:2:: £65. 7s. 8.8125d.: int. req.

... int. req⁴.= $\frac{2}{5}$ of £65. 7s. 8.8125d.=£26. 3s. 1.125d.; $Am^{4} = £1376$, 11s. 3d. + £26, 3s. 1·125d. =£1402, 14s. 4·125d. Note. Since £1376. 11s. 3d = £1376.5625, and $4\frac{3}{2} = 4.75$,

we might have found the int. thus: int. $\Rightarrow \pounds \left(\frac{1376.5625}{2} \times 4.75 \right)$

=£65.38671875.

E_{x} . LXX.

Find the Simple Int. and also the Amt. of

- \$217.25 for 1 year at 8 per cent. per anna. (1)
- \$217.25 for 2 yrs. at 8 per cent...... (2)
- (3) \$527.37\frac{1}{2} for 3 yrs. at 7.....
- \$93.50 for 2 yrs. at 6..... (4)
- \$75.75 for 2½ yrs at 7..... (5)£62. 18s. 91d. for 31 yrs. at 8..... (6)

COMPOUND INTEREST.

- (7) \$1075.75 for 41 yrs. at 8 per cent. per ann.
- (8) \$684 for 5 yrs. 8 mo., at 8
 - (9) £7500 from May 5 to Oct. 26, at 3\(\frac{1}{2}\).......
- (10) £4865. 11s. 5d. from Jan. 1 to Aug. 28, 1868, at 53.
- (11) In what time will \$672 at 8 per cent. simp. int. amount to \$994.56?
- (12) At what rate per cent., simp. int., will the int. on \$816 amount to \$346.80 in 5 yrs. ?

(13) What sum of money will amount to £138. 2s. 6d., in 15 mo, at 5 per cent, per annm., simp. int. ?

- (14) If £1 = 10 florins = 100 cents = 1000 mills, find the simp. int. on £578. 3 fl. 1 c. 21 m. for 21 yrs. at 21 per cent
- (15) At what rate per cent., simp. int., will \$2293.75 louble itself in 25 yrs. ?

COMPOUND INTEREST.

126. To find the Compound Interest of a given sum of noney at a given rate per cent. for any number of years.

RULE. At the end of each year add the interest of that vear found by (Art. 116), to the principal at the beginning of it; this will be the principal for the next year; proceed in the same way as far as may be required by the question. Add together the interests so arising in the several years, and the result will be the compound interest for the given period.

Ex. 1. Find the Comp. Int. and Amt. of \$600 for 3 yrs. at 8 per cent. per ann.

\$600 8 \$43.00 Int. for 1st yr. . \$648 Print. for 2nd yr. 8 Int. for 2nd yr. \$51.84 Print. for 3rd yr. . . \$699.84 \$55.9872 Int. for 3rd yr.

.:.Compd int. = \$55.9872 + \$61.84 + \$48 = \$155.8272. Am¹. \$600 + \$155.8272 = \$755.8272.

Ex. 2. Find, working with decimals, the comp. int. and int. of £690 for 2 yrs. at 41 per cent. per ann.

ARITHMET 10.

1.36q. ...am^t. = £753. 9s. 11\frac{1}{4}d. nearly, and Int. = £753. 9s. 11\frac{1}{4}d. nearly - £690 = £63. 9s. 11\frac{1}{4}d. nearly.

Note 1. It is customary, if the comp⁴ int. be required for any number of entire yrs. and a part of a yr. (for instance for 5\frac{3}{4} yrs.) to find the comp⁴ int. for the 6th yr., and then take \frac{3}{2}ths of the last int. for the \frac{3}{4}ths of the 6th yr.

Note 2 If the int. be payable half-yearly or quarterly, it is clear that the comp⁴ int. of a given sum for a given time will be greater as the length of each given period is less; the simp, int. will not be affected by the length of each period.

Ex. LXXI.

Find the Compound Int. and Arat of

LILL	a the Compound the and III. of
(1)	\$800 for 2 yrs. at 7 per cent. per annum.
(2)	\$742 for 3 yrs. at 8
(3)	\$560 for 5 yrs. at 10
(4)	\$308 for 1½ yrs. at 6paid quarterly.
	\$610 for 2 yrs. at 8 paid half-yearly.
(6)	\$1000 for 3 yrs. at 7 paid half-yearly

(7) Find the difference between the Amounts at simp and comp. int. of (1) £880 for 2 ys. at $3\frac{1}{2}$ per cent. (2) £1431. 5s. for three yrs. at 4 per cent.

PRESENT WORTH AND DISCOUNT.

127. A owes B \$500, which is to be paid at the end of 9 months from the present time; it is clear that, if the debt be paid at once (int. being reckoned, we will suppose, at 8 per cent. per annum), B ought to receive a less sum of money than \$500; in fact such a sum of money as will, being now put out at 8 per cent. int., amounts to \$500 at the end of 9 months. The sum which B ought to receive now is called the Present Worth of the \$500, due 9 months hence, and the sum to be deducted from the \$500, in consequence of immediate payment, which is in fact the int. of the Present Worth, is called the Discount of the \$500 paid 9 months before it is due: hence.

PRESENT WORTH is the actual worth at the present time of a sum of money due some time hence, at a given rate of interest.

DISCOURT of a sum of money is the interest of the I resent Worth of that sum, calculated from the present time to the time when the sum would be properly payable.

... Disc' = given sum less its P. Worth, and P. Worth =

given sum lece its Disc'.

PRESENT WORTH.

128. RULE. Find the interest of \$100 for the given time at the given rate per cent., and state thus:

\$100 + its interest for the given time at the given rate per

cent. : given sum :: \$100 : present worth required.

Ex. 1. Find the present worth of \$676, due 6 markly hence, at 8 per cent. per annum.

By the Rule,

Int. on \$100 for 6 mo. at 8 per cent. = \$4. .: \$164 : \$676 :: \$100 : P. Worth req4.

hence P. Worth req⁴. = $$\frac{670 \times 100}{104} = 650 .

Reason \$100 is the P. Worth of \$104, due 6 mo. hence, we have the above statement by the Rule of Three.

Ex. 2. Find the present worth of £275. 6s. 8d. due & months hence at 4 per cept.

Int. of £100 for 15 mo. at 4 per cent. $=\frac{15}{12}$ of £4 = £5.

.. £105 : £275\frac{1}{3} :: £100 : P. Worth req⁴. .. P. Worth req⁴. = £\frac{275\frac{1}{3} \times 100}{105} = £262. 4s. 5\frac{1}{4}d. nearly.

DISCOUNT.

129. RULE. Find the interest of \$100 for the given time at the given rate per cent., and state thus:

\$100. + its interest for the given time at the given rate per cent. : given sum :: interest of \$100 for the given time at the given rate per cent. : discount required.

Ex. 1. Find the discount of \$250.75 due 17 months hence at 8 per cent per annum, simple interest.

By the Rule,

nt. of \$100 for 17 mo. at 8 per cent.
$$=\frac{17}{12}$$
 $= 38 = 114 .

$$\therefore$$
 \$111\frac{1}{3}: \$250\frac{3}{4}:: \$11\frac{1}{3}: \text{disc}^4. \text{ req}^4.

$$\therefore \text{disc}^4. \text{ req}^4. = \$ \frac{250_4^3 \times 11_3^4}{111_3^4} = \$ 25.40_2^2 \$.$$

Reason. $\$11\frac{1}{3}$ is the interest on \$100 or the discount on $\$111\frac{1}{3}$ for 17 mo. at 8 per cent., ... we have the above statement by the Rule of Three.

- 130. In the discharge of a tradesman's bill before it has become due, it is usual to deduct interest instead of discount; thus, if B contracts with A a debt of \$100, A giving 12 months' credit, it is usual, if the interest of money be reckoned at 8 per cent. per annum, and the bill be discharged at once, for A to throw off \$8, or for A to receive \$92 instead of \$100; but if A were to put out the \$92 at 8 per cent. interest for 12 months it will not amount to \$100; therefore such a proceeding is to the advantage of B: the sum of money which in strictness ought to have been deducted, was not \$8, the interest on the whole debt, but \$7.36, the interest on the present worth of the debt, i. e. the discount.
- 13. Benkers and Merchants in discounting bills calculate interest, instead of discount, on the sum drawn for in the bill, from the time of their discounting it to the time when it becomes due, adding THREE DAYS OF GRACE, which days are usually allowed after the time a bill is NOMINALLY due, be-

fore it is LEGALLY due. When a bill is payable on demand, the days of grace are not allowed.

If a bill, without the days of grace, should appear to be due on the 31st of any month which contains less than 31 days, the last day of that month, and not the first day of the next, is considered as the day on which the bill is due. Thus a bill drawn on the 31st of Oct. at 4 months, would be really due, adding in the days of grace, on the 3rd of March. Bills which fall due on a Sunday, are paid on the previous Saturday

Ex. A bill of £1000 is drawn on Feb. 16th, 1864, at 7 months' date: it is discounted on the 8th day of July at 5 per cent. What does the banker gain by the transaction?

The bill is legally due on Sept. 19; from July 8 to Sept.

19 are 73 days.

(1) \$216

(2) \$968

(3) \$1236

nun:?

profit.

Find the present worth of

Int. of £1000 for 73 days == £10. Disc. = x_1^4 18₁₂₁₈., banker's gain =£10 -£9. 18₁₂₀₁₈. = 1_{12018}^{69} .

Ex. LXXIL

due 1 yr. hence at 8 per ct. per ann. simp. in

.....3 yr...... 7

(4) \$225.25	9 mo 10	• • • • • • • • • • • • • • • • • • • •
(5) \$1057.50	$2\frac{1}{2}$ yrs 7	
(6) £161. 13s. 5\frac{1}{4}d.	$7\frac{1}{7}$ yrs $3\frac{1}{2}$	
(7) £193. 178. 4\frac{1}{4}d.	19 mo 5	
(8) £458. 8s. 91d.	31 days 5	
Find the Discount		
(9) \$217 due 3	yrs. hence at 8 per ct	. per ann. simp. irt
(10) $$22100 \dots 1$	11mg 7	
(10) \$22100 13	y 13	• • • • • • • • • • • • • • • • • • • •
, , ,	mo 10	
(11) \$20006	•	·•···
(11) \$2000 6 (12) \$1750 9	mo 10	•••••••

cartile liscount or £549 for 32 days at 5 per cent. per an-

(15) A bifl or £450 drawn March 3, at 9 mo. date, is dis counted by a banker on Oct. 22 at 5 per cent. Find his

(16) From a bill of £3. 11s. 8d. due 18 mo, hence, a tradesman deducts 5s.; which is the rate per cent. at which the true discount is calculated?

STOCKS.

132. If the 6 per cent. "Dominion of Canada" stock be quoted in the money market at $105\frac{1}{2}$, the meaning is, that for $\$105\frac{1}{2}$ of money a man can purchase \$100 of such stock, for which he will receive a document which will entitle him to half-yearly payments of Interest or Dividends, as they are called, from the Government of the country, at the rate of 6 per cent. per annum on the stock held by him, until the Government choose to pay off the debt.

Similarly, if shares in any trading company, which were originally fixed at any given amount, say \$100 each, be advertised in the share-market at 86, the meaning is, that for \$86 of money one share can be obtained, and the holder of such share will receive a dividend at the end of each half-year upon the \$100 share according to the state of the finan-

ces of the company.

STOCK may therefore be defined to be the capital of trading companies; or to be the money borrowed by our or any other Government, at so much per cent., to defray the expenses of the nation.

The a nount of debt owing by the Government is called the NATIONAL DEBT, or the FUNDS. The Government reserves to itself the option of paying off the principal or debt at any future time, pledging itself however to pay the interest on it regularly at fixed periods in the mean time.

From a variety of causes the price of stock is continually varying. A fundholder can at any time sell his stock, and so convert it into money, and it will depend upon the price at which he disposes of it as compared with the price at which he bought it, whether he will gain or lose by the transaction.

Note 1. Purchases or sales of stock are made through Brokers, who generally charge \$\frac{1}{2}\text{t}, or \$12\frac{1}{2}\$ cts. per cent. upon the stock bought or sold: so that, when stock is bought by any party, every \$100 stock costs that party \$\frac{1}{2}\text{m ore than the mark-t-price of the stock: and when stock is sold, the seller g.tn \$\frac{1}{2}\text{ less for every \$100 stock sold than the market-price.}

Taus, the actual cost of \$100 stock in the 3 per cents at

 $84\frac{1}{3}$, is $5(94\frac{1}{3} + \frac{1}{3})$, or $594\frac{1}{3}$. The actual sum received for \$100 stock in the 3 per cents. at $94\frac{1}{8}$, is \$($94\frac{1}{8} - \frac{1}{8}$), or \$94.

Unless the brokerage is mentioned, it need not be noticed

in working examples in stocks.

Note. When \$100 stock costs \$100 in money, the stock is said to be at par; when \$100 stock cost more than \$100 in money, the stock is said to be at a premium; when \$100 stock costs less than \$100 money, the stock is said to be at a discount.

All Examples in Stocks depend on the principles of Proportion, and may therefore be worked by the Rule of Three.

Ex. 1. What sum of money will purchase \$2600 6 per cent. stock at 93?

\$100 stock (st) costs \$93 in money;
\$100 st.: \$2600 st.: \$93 : req⁴. sum;

$$\therefore \text{ req}^4. \text{ sum} = \frac{2600 \times 93}{100} = $2418.$$

Ex. 2. Find the cost of £2353 3 per cent. Consols at 90g brokerage being | per cent.

∴ £100 st. : £2353 st. :: £20½ : reqd. cost;

 $\therefore \text{ req^4. cost} = \pounds \frac{2358 \times 90\frac{1}{2}}{100} = \pounds 2129. \ 9s. \ 3\frac{1}{2}d. \ \frac{2}{3}q.$

Ex. 3. A person who has \$10000 Bank-stock, sells out when it is at 35 per cent. premium; what amount of money does he receive, brokerage being } per cent.?

\$100 st. sells for
$$\xi \left(135 - \frac{1}{8}\right)$$
, or \$134\frac{7}{8} money.

∴\$100 st.:\$10000 st.::\$134g : reqd. am'. of money;

 $\therefore \text{ req}^{d}. \text{ am}^{t}. = \$ \frac{10000 \times 134\frac{7}{8}}{100} = \$ 13487.50.$

Ex. 4. What incomes will \$5500 at 7 per cent. stock, and \$5500 invested in the 7 per cent. stock at 1023, respectively produce?

1st, since every \$100 stock gives \$7 int.; ... income from \$5500 of 7 per cent. stock = \$ $\frac{5500 \times 7}{100}$ = \$385.

2nd, since \$100 stock, which gives \$7 int., costs \$1022; .. every \$102% give \$7 int.;

.:.\$1023: \$5500 :: \$7 reqd. income;

•• req4. income =
$$\$ \frac{5500 \times 7}{102 \frac{2}{8}} = \$375$$
.

Ex. 5. One person buys £500 Consols at 90g and sells out at 93; another invests £500 in Consols at 90g and sells out at 93; what sum of money does each gain?

lst man gains $\pounds(93-90\frac{1}{3})$, or $\pounds2\frac{2}{3}$, on every £100 stock; ... his whole gain $=\pounds(2\frac{2}{3}\times 5)=£13$. 6s. 8d.

2d man gains £2 $\frac{1}{3}$ on every £100 stock, i. e. on every £90 $\frac{1}{3}$ of his money which he invests:

Ex. 6. A person invested some money in the 3 per cent. Consols when they were at 90, and some money when they were at 80; find the rate of interest he obtained in each case, and the advantage per cent of the second purchase over the first.

£90:£100::£3: rate per cent. in 1st case, £80:£100::£3: rate per cent. in 2d case,

... rate per cent. in 1st case = £
$$\frac{100 \times 3}{90}$$
 = £3. 6s. 8d.;

$$2nd = 4 \left(\frac{100 \times 3}{80} \right) = £3. 15s;$$

... advantage = £3. 15s. -£3. 6s. 8d. = 8s. 4d.

Ex. 7. A person invests £1037. 10s. in the 3 per cents. at 83; the funds rise 1 per cent; he then transfers his capital to the 4 per cents at 96: find the alteration in his income. £83: £1037. 10s. :: £100: quantity of 3 per cent. st.:

... quantity of 3 per cent st. bought = £
$$\frac{1037\frac{1}{2} \times 100}{80}$$
 = £1250.

The funds have risen 1 per cent. therefore to transfer £1250 stock from the funds at 84 to the funds at 96,

£96: £84:: £1250 stock; quantity of 4 per cent. stock, (since the higher the price of the stock the less will be the arount purchased);

. quantity of 4 per cent. stock = £
$$\frac{1250 \times 84}{96}$$
 =£1093.15s.

Ist Income =
$$\pounds \frac{1250 \times 3}{100} = \pounds 37.$$
 10s.
2nd Income = $\pounds \frac{1093 \frac{3}{4} \times 4}{100} = \pounds 43.$ 15s.;

... alteration in income = £43. 15s. £37. 10s. = £6. 5s.

Ex. LXXIII.

(1) Find amount of Bank of Montreal stock purchased by investing \$527.25 at 126½, the stock yielding 8 per cent., per annum interest?

(2) Bank of Toronto stock being at 1021, how much can

be purchased for \$800?

(3) Find the value of \$1536 Royal Canadian Bank stock

at 98.

(4) Royal Canadian bank stock being at 1 per cent. discount, I invest \$525.50; find my income therefrom; the

Bank's dividends being 7 per cent. per annum.

(5) Montreal Bank stock being at 125\(\frac{3}{5}\), and paying yearly dividends of 7\(\frac{1}{2}\) per cent.; how much money must be in vested in order to secure an annual income of \$900, allowing \(\frac{1}{2}\) per cent. for brokerage?

(6) Upper Canada Bank bills are at 65; how much

money could a person obtain for \$2140 of such Bank bills?

(7) If a man invest £666. 8s. 4d. in the 3 per cents. at 90½, (1) what half-yearly interest will he obtain after deducting an inc. tax of 4d. in the £? (2) What rate per cent will he get for the money invested?

(8) What rate per cent. per annum does a person receive for his money, who invests in Bank of Montreal stock at 136; the stock yielding half-yearly dividends of 4 per cent?

(9) Which would be the better investment, Bank of Montreal stock at 136, or Bank of Toronto stock at 104; half-yearly dividends being 4 and 3\frac{3}{4} per cent. respectively?

(10) If a person lay out £4650 in the $3\frac{1}{2}$ per cents, when they are at * per cent. discount, what will be his loss of property by the stocks falling $\frac{1}{2}$ per cent. ?

(11) If a person were to transfer £29000 stock, from the 3½ per cents. at 99 to the 3 per cents. at 90§, what difference

would it make in his income?

(12) A person invests \$2000 in Bank of Toronts stock at 115, shortly afterwards he sells when the stock rose to 123

find his gain?

(13) If the 3 per cents, are at 95, and Government offer to receive tenders for a loan of £5016000, the lender to receive five millions in the 3 per cents, together with a certain sum in the 3½ per cents, what sum in the 3½ per cents, ought the lender to accept?

(14) A man sells out of the 3½ per cents, at 93½ and realizes £18700, if he invest one-fifth of the produce in the 4 per cents, at 96, and the remainder in the 3 per cents, at 90; find the alteration in his income.

- (15) A person invests £5460 in the 3 per cents at 91; he sells out £2000 stock when they have risen to 93½, and the remainder when they have fallen to 85; he then invests the produce in the 4½ per cents at 102. What is the difference in his income?
- (16) A person has an income of £350 from money invested in the new 3 per cents., he sells out at 87\frac{3}{6}, and invests in the India 5 per cents. at 104\frac{3}{4}. How will his income be affected, it here cents being allowed for brokerage?

APPLICATIONS OF THE TERM "PER CENT."

133. There are many other cases in which the term Pen Cent. occurs besides those already mentioned; we will mention certain cases, and give examples in each by way of illustration.

COMMISSION is the sum of money which a merchant charges for buying or selling goods for another.

BROKERAGE is of the same nature as Commission, but has relation to money transactions, rather than dealings in goods or merchandise.

INSURANCE is a contract, by which one party, on being paid a certain sum or *Premium* by another party on property, which is subject to risk, undertakes, in case of loss, to make good to the cwner the value of that property The document which expresses the contract is called the *Policy of Insurance*.

LITE ASSUMANCE is a contract for the payment of a certain sum of money on the death of a person, in consideration of an annual premium to be continued during the life of the Assured, or for a certain number of years.

Questions on Commission, Brokerage, and Insurance, these charges being usually made at so much per cent., amount to the same thing as finding the interest on a given sum of money at a given rate for 1 yr., and may therefore be worked by the Rule for Simple Int. or by the Rule of three.

Ex. 1. What is the brokerage on the purches of \$4300 per cents, stock at \(\frac{1}{6} \) per cent. ?

Ex. 2 What is the premium on a policy of insurance for £9626. 11s. 3d., at £2. 12s. per cent.?

£100: £9626. 11s. 3d. :: £2. 12s. : premium req^d.

... premium reg⁴ = £ $\frac{9626 \frac{9}{3} \times 2\frac{3}{5}}{100}$ = £250. 5s. $9\frac{3}{4}d$.

Ex. 3. What is the annual cost of insuring property to the amount of \$1600, the premium being \$1.50 per cent.?

 $\$100:1600:1.50:ann^{1}.cost; ...ann^{1}.cost=\$1.50\times16=\$24.$

134. All questions which relate to gain or loss in mer-

cantile transactions fall under the head of Profit and Loss.

Tradesmen measure their Profit or Loss by the actual amount gained or lost, or by the amount gained or lost on

every \$100 of the capital they invest.

Ex. 4. If tea be bought at 84 cts. per lb., and sold at 93 cts. per lb., find the gain per cent.

(93 cts. -84 cts.) = 9 cts.; ... gain on 84 cts. = 9 cts

... 84 cts. : \$100 :: 9 cts. : gain per cent. ;

... gain per cent. = $\frac{100 \times 9}{54}$ cts. = \$10.71\$.

Ex. 5. If tea be bought at 93 cts. per lb. and sold at 84 cts. per lb., find the loss per cent.

In this case 9 cts. is lost on 93 cts.,

.. 93 cts. : \$100 :: 9 cts. : loss per cent. whence loss per cent. = $$9.67\frac{2}{3}$.

Ex. 6. By selling cheese at £3. 13s. 6d. a cwt. a grocer realized a profit of 22½ per cent., what did it cost him per cwt.? He sells cheese for which he gave £100 for £122½.

 $£122\frac{1}{2}$: £3. 13s. 6d. or £3 $\frac{27}{40}$:: £100 : prime cost per cwt.;

 $\therefore \text{ prime cost per cwt.} = £\frac{3\frac{27}{45} \times 100}{122\frac{1}{4}} = £3.$

Ex. 7. By selling cheese at £3. 13s. 6d. a cwt. a grocer lost $22\frac{1}{2}$ per cent., find the prime cost of the cheese per cwt.

In this case he sells cheese, for which he gave £100, for $£100-£22\frac{1}{2}$), or for £77\frac{1}{2}.

 \mathcal{L}_{1} : £3 $\frac{2}{4}$:: £100 : prime cost of cheese per cwt. :

... prime cost per cwt. = £ $\frac{3\frac{27}{45}\times100}{77\frac{1}{2}}$ = £4. 14s. $10\frac{2}{10}$

Ex. 8. By selling sheep for \$19 the seller loses 5 per cent. on his outlay; what would have been his loss or gain per cent. if he had sold the sheep for \$23.75?

2nd. \$20: \$100:: \$3.75: gain per cent., if the sheep he sold for \$23.75;

... gain per cent. = $\$ \frac{100 \times 3\frac{3}{4}}{20} = \18.75 .

This sum might have been worked thus,

\$19: \$23\frac{2}{3}:: \$95, i. c. what \$100 will realize if the sheep be sold for \$19: what \$100 will realize if the sheep be sold for \$23\frac{2}{3}.

.:. \$100, if sheep sold for \$23\frac{2}{2}\$ will realize \$\frac{95 \times 23\frac{2}{4}}{19}\$, or \$118\frac{2}{3}\$:

... gain per cent. = $$118\frac{2}{4} - $100 = $18\frac{2}{4} = 18.75 .

135. Tables respecting the increase or decrease of Popu lation, &c., are constructed with reference to the increase or decrease on every 100 of such population; Education returns are constructed in the same way; and so are other Statistical Tables.

Ex. 9. In 1852 the population of the County of Wellington was 26796, in 1861 it was 49200; find the increase per cent 49200—26796=22404; ... 26796: 100:: 22404:incr. per cent.

 \therefore increase per cent. = $\frac{2240400}{26796}$ = 83.609....per cent.

Ex. 10. Between the years 1841 and 1851 the population of England increased 14.2 per cent. In 1851 it was 21121290 what was it in 1841?

For every 100 persons in 1841 there were 114.2 in 1851; ... 114.2: 21121290:: 100: population in 1841;

... population in $1841 = \frac{21121250 \times 100}{114.2} = 18495000.$

Ex. 11. If of a regiment of 750 men, 26 per cent. are in hospital, 32 per cent. in trenches, and the rest in camp, how many are in hospital, trenches, and camp, respectively

100:750::26:no. in hosp!.;...no. in hosp!. = $\frac{750 \times 26}{100}$ =195

100:750::32: no. in trenha.;... no. in trenha. = $\frac{750 \times 32}{100}$ = 240

.: number in camp = 750 - (195 + 240) = 315.

Ex. 12. The percentage of abildren who are learning to

write is 65 in a school of 60 children, and 78 in another school of 10, what is the percentage in the two schools together? In the 1st school.

100:60::65:no. who write; no. who write = $\frac{60 \times 65}{100}$ = 39.

In the 2nd school,

$$100:70::78:$$
 no, who write; ... no. who write $=\frac{70\times78}{100}=54\frac{1}{8}$.

... in a school of 130, there are 933 who write;

... 130:100::93%: percent. reqd.; ... percent. reqd.

$$= \frac{100 \times 93\frac{3}{5}}{130} = 72.$$

Ex. LXXIV.

(1) What will be the broker's commission on the purchase of \$4300 6 per cents, at 901, at 1 per cent.?

(2) What is the premium on a policy of insurance for

\$9626.55 at \$2.60 per cent.?

(3) The commission on the purchase of \$1560 Dominion stock at 104 amounted to \$4.60, what was the rate per cent.?

(4) For what sum would the life of a person aged 23 be insured by the annual payment of \$45.60, the premium for

that age being \$2.40 per cent. ?

(5) A draper at Hamilton buys 25 pieces of calico, each containing 36 yds., for £32. 16s. 3d.; the carriage costs him 6s. 3d.; (1) What will be gain by selling the calico at 101d. a yard? (2) What will he gain per cent.?

(6) A merchant bought 1280 bus. of wheat at \$1.20 a bu., the expenses of carriage, &c., averaged 32 cts. a bu.; he sold the wheat at \$1.40 a bu. (1) What was his gain? (2) What was his gain per cent.? (3) At what price a bu. should he have sold the wheat in order to gain \$400 ?

(7) (1) A man buys a pig for 6s. 8d., and sells it for 7s. 4d., and his gain per cent. (2) What would have been the loss per cent. had he bought the pig at 7s. 4d. and sold it at 6s. 8d. ?

(8) Tea is bought at \$96 per cwt., at what price per lb. must it be sold to gain 25 per cent.?

(9) Sugar is bought at \$6 per cwt., what will be the gain

per cent. if it be sold at 10 cts. per lb. ?

(10) At what price must a yd, of cloth be sold, which cost M. 8d.. so as to gain 121 per cent. ?

(11) If a yd. of cloth, sold at 4s. 8d., give a profit of 15, per cent.; find the prime cost.

(12) A grocer buys 40 lbs. of tea at 84 cts., 44 lbs. at 93 cts., and 55 lbs. at \$1.08; and sells the mixture for \$188.16, what

is his gain per cent.?

(13) A grocer mixes 26 lbs. of tea at 5s. 3d., 32 lbs. at 5s. 7d., and 36 lbs. at 6s. 1d.; at what rate per lb. must he sell the mixture in order to gain 40 per cent. on his outlay?

- (14) If I sell for 15s. I lose 10 per cent., what must I sell at to gain 10 per cent.?
- (15) A person buys a certain number of eggs and sells them again at such a price, that 11 are sold for the money 18 cost him. Find his gain per cent.
- (16) A boy sells another boy a cricket-bat for \$1.56, gaining thereby 30 per cent.; what did it cost him?

APPLICATIONS OF THE TERM "AVERAGE."

136. Questions are often given, in which the term "Average" occurs; two such examples will be worked by way of illustration, and others subjoined for practice.

Ex. 1. A gentleman in each of the following years expended the following sums: in 1845 \$650, in 1846 \$675, in 1847 \$680, in 1848 \$690, in 1849 \$700, in 1850 \$715, in 1851

\$790. Find his average yearly expenditure.

The object is to find that fixed sum which he might have spent in each of the seven years, so that his total expenditure in that case might be the same as his total expenditure was in the above question.

Adding the various sums together we find that the total expenditure amounted to \$4900; this sum divided by 7 gives

\$700 as the average yearly expenditure.

Ex. 2. In a school of 27 boys, 1 of the boys is of the age of 17 years, 2 of 16, 4 of $15\frac{1}{2}$, 1 of $14\frac{3}{4}$, 2 of $14\frac{1}{2}$, 5 of $13\frac{3}{2}$, 10

of $12\frac{1}{4}$, and 2 of 10; find the average age of the boys.

The object is to find, what must be the age of each boy, supposing all to be of the same age, that the sum of their ages may equal the sum of the ages in the question. Sum of ages

= $17 + 32 + 62 + 14\frac{3}{4} + 29 + 68\frac{3}{4} + 122\frac{1}{2} + 20 = 366$ • average age = 366 yrs. ÷ $27 = 13\frac{5}{6}$ years.

Ex. LXXV.

(1) The highest temperature registered in the shade on

Monday 13th July, 1868, in the following towns, was :- Ottawa, 104; Montreal, 96; Toronto, 92; New York, 90; Buffalo, 82; New Orleans, 81 Find their average highest temperature ?

- (2) On Sunday I spent no money, on Mond. \$4.25, on Tues. \$5.75, on Wed. \$6.60, on Thurs. \$7.80, and Frid. \$3.50. on Sat. \$5.58; find my average daily expenditure during the week?
- (3) The highest temperature registered in the shade in the week ending on Midsummer-day, 1865, in the following towns, was: Birmingham, 87.8; Manchester, 87.7; London, 87.6; Bristol, 86.8; Leeds, 85.0; Salford, 84.5; Dublin, 83.8; Edinburgh, 78.0; Liverpool, 77.9; Glasgow, 77.6. Find their average highest temperature?
- (4) In a school, 17 children average 6 years.; 26, 7½ yrs., 25, 9½ yrs.; 20, 10 yrs.; and 8 12½ yrs. Find the average ge of all the children.
- (5) The average age of 27 men is 57 years, that of the first eleven is 53 years, and that of the last eight 591 years. Find the average age of the rest.
- (6) The populations of 3 towns in 1851 were 31326, 42324, and 6706; in 1861 the first two had increased 12, and 10 per cent. respectively, and the last had decreased 18 per cent : find the average population of the 3 towns in 1861.
- (7) A tradesman's average annual gain from the year 1853 to 1863, both inclusive, was £184. 11s. 6d.; in 1853 he lost £76. 8s. 4d., and in 1864 he gained £151. 9s. 10d. What was his average annual gain from 1854 to 1864, both inclu-Rive "

DIVISION INTO PROPORTIONAL PARTS.

137. To divide a given number into parts, which hall be proportional to certain other given numbers.

This is an application of the Rule of Three; still it may be well to state a general Rule, by which such Ex. may be worked.

RULE. As the sum of the given parts : any one of them :: the entire quantity to be divided : the corresponding part of it.

This statement must be repeated for each of the parts, or

found by the Rule, or by subtracting the sum of the values of the other parts from the entire quantity to be divided.

Ex. 1. Divide 40 dollars among A, B, C, so that their shares may be as 7, 11, and 14 respectively.

By the Rule. Sum of shares = 7 + 11 + 14 = 32. $\therefore 32:7::\$40: A's sh^*:; 32:11: \$40: B's sh^*:;$ whence $A's sh^*.=\$8.75$, $B's sh^*.=\$13.75$. $C's sh^*.=\$40-\$(8.75+\$13.75)=\17.50 .

Ex. 2. Divide £45 among A, B, C, and D, so that A's share: B's share:: 1:2, B's: C's:: 3:4, and C's:: D's:: 4:5. The L. c. M., of 1, 2, 3, 4, and 5. is $60, \cdots$ if D has 60 shares, C will have $\frac{4}{5}$ of 60, or 48; B will have $\frac{3}{5}$ of 48, or 36: and 4 will have $\frac{1}{5}$ of 36, or 18.

.: (18 + 36 + 48 + 60), or 162 : 18 :: £45 : A's sh.; whence A's sh. = £5. Similarly B's = £10. C's = £13. 6s. 8d., and D's = £16. 13s. 4d.

FELLOWSHIP OR PARTNERSHIP.

138. Fellowship or Partnership is a method by which the respective gains or losses of partners in any mercantile transactions are determined.

Fellowship is divided into SIMPLE and COMPOUND FEILOWSHIP: in the former, the sums of money put in by the several partners continue in the business for the same time; in the latter, for different periods of time.

The Rule in the last Art. applies for SIMPLE FELLOWSHIP.

Ex. Two merchants, A and B, form a joint capital; A puts in \$240, and B \$360; they gain \$30. How ought the gain to be divided between them?

(240 + 360): 240:: 80: A's sh. in \$'s. A's sh. = \$32, and B's sh. = \$(80 - 32) = \$48.

COMPOUND FELLOWSHIP.

139. RULE. Reduce all the times into the same denomination, and multiply each man's stock by the time of its continuance, and then state thus:

The sum of all the products: each particular product:: the whole quantity to be divided: the corresponding share.

Ex. A and B trade together; A puts in \$300 for 9 mo., and B \$240 for 6 mo; they gain \$115. How ought they to divide it:

By the Rule,

\$(300 \times 9 + 240 \times 6) : \$(200 \times 9) :: \$115 : A's sn., \$(300 \times 9 + 240 \times 6) : \$240 \times 6) :: \$115 : B's sh., whence, A's sh. = \$75, and B's = \$40.

Reason. \$300 for 9 mo. = 9 times \$300 for 1 mo., and \$240 for 6 mo. = 6 times \$240 for 1 mo.: the example then becomes one of Simple Fellowship.

EQUATION OF PAYMENTS.

140. When a person owes another several sums of money, due at different times, the Rule by which we determine the just time when the whole debt may be discharged at one payment, is called the EQUATION OF PAYMENTS.

Note. It is assumed in this Rule that the sum of the interests of the several debts for their respective times equals the interest of the sum of the debts for the equated time.

RULE. Multiply each debt into the time which will elapse of ore it becomes due, and then divide the sum of the products by the sum of the debts; the quotient will be the quated time required.

Ex. 1. A owes B \$100, whereof \$40 is to be paid in 3 ao., and \$60 in 5 mo.; find the equated time.

By the Rule,

equated time in mo. =
$$\frac{40 \times 3 + 60 \times 5}{40 + 60} = \frac{420}{100} = 4\frac{1}{5}$$
.

Ex. 2. A owed B \$10, to be paid at the end of 9 mo.; he pays however \$2 at the end of 3 mo., and \$3 at the end of 8 mo.; when ought the remainder to be paid?

In this case, $2 \times 3 + 3 \times 8 + 5 \times \text{no.}$ of mo. req^d. = 10×9 , or

 $6 + 24 + 5 \times \text{no. of mo. req}^{d} = 90$;

or, $30 + 5 \times \text{no.}$ of mo. req⁴. = 90, or $5 \times \text{no.}$ of mo. req⁴. = 90 - 30, or 60, ... no. of mo. req⁴. = 12.

Ex. LXXVI.

(1) Divide (.) 1008 into 3 parts, which shall be to each other as the numbers 2, 3, 4, respectively. (2) \$260 into 3 parts, which shall be to each other as 5, 11, and 16. (3) 145 ac. 3 ro. 33 po. between two persons in the ratio of 5:6. (4) £110 between 4 persons, whose shares shall be as \frac{1}{2}, \frac{1}{3}, \frac{1}{4}, and \frac{1}{4}.

(2) (1) A, B, and C contribute to a fund \$320, \$560, \$720, respectively. How are they to divide a profit of \$680? (2) A, who has £422. 10s., owes B, £175; C, £210; and D, £265;

what sam ought C to receive?

ARITHMETIC

- (3) Sugar being composed of 48.856 per cent. of oxygen, 43.265 per cent. of carbon, and the rest hydrogen; how many lbs. of each of these materials are there in 1 ton of sugar?
- (4) Archimedes discovered that the crown made for King Hiero consisted of gold and silver in the ratio of 2:1. How much per cent. was gold, and how much per cent. was silver?
- (5) Find the equated time of payment of \$150 due in 2 mo., \$210 due in 6 mo., and \$120 due in 7 ro.
- (6) A owes B \$1000 to be paid at the end of 6 mo.; A pays \$400 at the end of 3 mo.; when ought he to pay the remainder?
- (7) A, B, and C remained partners for 2 years; A brought in \$4000, which remained the whole time; B began with \$300, and 6 months after put in \$300 more; C began with \$200, and one year after put in \$500 more. The whole gain was \$7960. Determine each partner's share.
- (8) A is a working, B a sleeping partner in a bookseller's business. Their capital amounts to £6400; of which £2400 belongs to A, the rest to B. Their profits, at the end of the first year, amounted to £1600. A receives 10 per cent. of the profits for managing the business. How ought the remaining part of the profits to be divided?
- (9) A, B, and C rent a field for \$60; A puts in 20 horses, B 15 oxen, and C 10 sheep; supposing the keep of a horse, ox, and sheep to be in the ratio of 3, 2, and 1; shew how the rent should be divided.
- (10) Some broth was distributed among a certain number of old men, 9 widows, and 6 single women; the men had twice as much broth given among them as was given among the women; also an old man's share was to a widow's share :: 6:5, and a widow's share to a single woman's share :: 10:9. Each single woman received 1½ pints. How many old men were there?

SQUARE ROOT.

- 141. The SQUARE of a given number is the product of that number multiplied by itself. Thus 6×6 or 36 is the square of 6, or $36 = 6^2$. Art. 86.
 - 142. The SQUARE ROOT of a given number is a number,

which, when multiplied by itself, will produce the given number. Thus 6 is the square root of 36; for $6 \times 6 = 36$.

The square root of a number is sometimes denoted by placing the sign \checkmark before the number, or by placing the fraction $\frac{1}{2}$ above the number a little to the right. Thus $\sqrt{36}$, or $(36)^{\frac{14}{3}}$ denotes the square root of 36; so that $\sqrt{36}$, or $(36)^{\frac{14}{3}} = 6$.

143. Rule for extracting the Square Root of a number.

Place a point or dot over the units' place of the given number; and thence over every second figure to the left of that place; and thence also over every second figure to the right, when the number contains decimals, annexing a cypher when the number of decimal figures is odd; thus dividing the given number into periods. The number of points over the whole numbers and decimals respectively will shew the number of whole numbers and decimals respectively in the square root.

Find the greatest number whose square is contained in the first period at the left; this is the first figure in the root, which place in the form of a quotient to the right of the given number. Subtract its square from the first period, and to the remainder bring down, on the right, the second period.

Divide the number thus formed, omitting the last figure, by twice the part of the root already obtained, and annex the

result to the root and also to the divisor.

Then multiply the divisor, as it now stands, by the part of the root last obtained, and subtract the product from the number formed, as above mentioned, by the first remainder and second period.

If there be more periods to be brought down, the operation

must be repeated.

Ex. 1. Find the square root of 1369.

1369 (37

3'=
9
469
469
469
469
5'rice the square of 3 is 9, and that

of 4 is 16, it is clear that 3 is the greatest number whose aquare is contained in 13, therefore place 3 in the form of a quotient to the right of the given number. Square this number, and put down the square under the 13; subtract it from the 13, and to the remainder 4 affix the next period 69, thus forming the number 469. Take 2 × 3, or 6, for a dirisor; di-

vide the 469, omitting the last figure, that is, divide the 46 by the 6, and we obtain 7. Annex the 7 to the 3 before obtained, and to the divisor 6; then multiplying the 67 by the 7 we obtain 469, which being subtracted from the 469 before formed, leaves no remainder; therefore 37 is the square root of 1369.

Find the square root of 282475249. 282475249 (16807 $\{2 \times 1 = 2\}$ 18-2=9, but 9 will be found to 156 large, so also 8 or 7. . . try 6. $\{2 \times 16 = 32\}$ $264 \div 32 = 8$ $\{2 \times 168 = 336\}$ 33607 | 235249 336 is greater than 235; . . . put 235249 0 after the 8 in the quotient, and the 6 in the divisor, bring down the next period. Then $23524 \div 3360 = 7$.

Find the square root of 7.929856.

7.929556 (2.816

Place the first dot over the 7, the units' place of whole numbers, and then over every second figure to the right.

898 561 561 33756 **5**626 33756

There is 1 dot over the integral part, and 3 dots over the decl. part, ... the root is 2.816.

Find the square root of '001 to 3 places of decis. .001000 (.031

 $\{2+3=6\}$ 61 100 61 39 We affix 3 cyphers in order to have 3 periods, and . . . 3 dec!. places in root; since there is no number in the units' place, the first dot will be over the second cypher from the

units' place, and since first period is '00 we place '0 as the first figure in the root.

Ex. 5. Find the square root of 529. 529 (23 2401 (49 16

891 801 sq. root = 11 Ex. 6. Find the square root of $\frac{5}{7}$ to 3 places of dec¹.

Ex. LXXVII.

Find the square roots of (1) 196; 289; 625. (2) 841; 900; 1764. (3) 2401; 7569; 9604. (4) 12321; 40000; 388129. (5) 494209; 582169; 259081. (6) 1234321; 28547649. (7) 62504836; 33016516; 49112064. (8) 182493081; 47·61. (9) 400836; 445·336609. (10) 400633679929; 40000000009.

Find the source roots, each to four places of decimals, of (11) 51; 51. (12) 51; 051. (13) 806.52; 95304.993.

Find the square roots, each to 3 places of decimals where the root does not come out exactly, of (14) 3. (15) 027.

(16)
$$4\frac{36}{49}$$
. (17) $\frac{2304}{3481}$. (18) $\frac{4.41}{.64}$.

(19) A father left his child a box, containing sovereigns, and shillings; the sovereigns were worth as many times the shillings, as the shillings were worth the box; the value of the box was 2s. 6d., and there were 5832 sovereigns in the box. How many shillings were there?

CUBE ROOT.

144. The CUBE of a given number is the product which arises from multiplying that number by itself, and then multiplying the result again by the same number. Thus $6 \times 6 \times 6$, or 216 = 63. Art. 86.

145. The CUBE ROOT of a given number is a number, which, when multiplied into itself, and the result again multiplied by it, will produce the given number. Thus 6 is the cube root of 216; for $6 \times 6 = 36$, and $36 \times 6 = 216$.

The cube root of a number is sometimes denoted by plac-

ing the sign $\sqrt[3]{}$ before the number, or placing the fraction $\frac{1}{8}$ allowe the number, a little to the right. Thus $\sqrt[3]{216}$ or $(216)^{19}$ denotes the cube root of 216; so that $\sqrt[3]{216}$ or $(216)^{19} = 6$.

146. Rule for extracting the Cube Root of a number.

Place a point or dot over the units' place of the given number, and thence over every third figure to the left of that place; and thence also over every third figure to the right, when the number contains decimals, affixing one or two cyphers, when necessary, to make the number of decimal places a multiple of 3; thus dividing the given number into periods. The number of points over the whole numbers and decimals respectively will shew the number of whole numbers and decimals respectively in the cube root.

Find the greatest number whose cube is contained in the tirst period at the left; this is the first figure in the root, which place in the form of a quotient to the right of the given

uumber.

Subtract its cube from the first period, and to the remainder bring down, on the right, the second period.

Divide the number thus formed, omitting the two last figures, by 3 times the square of the part of the root already

obtained, and affix the result to the root.

Now calculate the value of 3 times the square of the first figure in the root (which of course has the value of so many tens) + 3 times the product of the two figures in the root + the square of the last figure in the root. Multiply the value thus found by the second figure in the root, and subtract the result from the number formed, as above mentioned, by the first remainder and the second period. If there he more periods to be brought down the operation must be repeated

Ex. 1. Find the cube root of 15625.

15625(25 $2^3 = 8$ After pointing we 7625 take the first period, or $3 \times 2^2 = 12$ 15, and find the great- $3 \times (20)^3 = 3 \times 400 = 1200$ est number whose $3 \times 20 \times 5 = 300$ cube is contained in $5^2 = 25$ it. Since the cube of 1525 2 is 8, and that of 3 is 7625 27, it is clear that 2 is Multiply by the greatest number 7625 whose cube is con.

tained in 15; ... place 2 in the form of a quotient to the right

of the given number.

Cube 2, and put down its cube, viz. 8, under the 15; subtract it from the 15, and to the rem. 7 affix the next period 625, thus forming the number 7625. Take 3×2^2 , or 12, for a divisor; divide 76 by 12, 12 is contained 6 times in 76 but when the other terms of the divisor are brought down 6 would be found too great, therefore try 5. Affix the 5 to the 2 before obtained; and calculate the value of $3 \times (20)^2 + 3 \times 20 \times 5 + 5^2$, which is 1525; multiplying 1525 by 5 we obtain 7625, which being subtracted from 7625 before formed leaves no rem.: ... 25 is the cube root read.

Ex. 2. Find the cube root of 219:365327791. Place the first dot over the 9 in the units' place.

$$\begin{array}{c} 219 \cdot 365327791 \ (6 \cdot 031) \\ 6^{3} = 216 \\ 3 \times 6^{7} = 108 \\ 3 \times (70)^{2} = 10800 \\ 3 \times (600)^{2} = 108000 \\ 3 \times 600 \times 3 = 5400 \\ 3^{2} = 9 \\ 1085409 \\ \hline 3 \times (6030)^{2} = 10908270 \\ 3 \times (6030)^{2} = 109082700 \\$$

1. 0.031 is the cube root required.

1. 3. F. d the cube root of 000007 to three places of 000007000 (-019)

$$3 \times (10)^{2} = 300
3 \times 10 \times 9 = 270
9^{2} = 81
65'
9
5859$$
5859

147 Higher roots than the square and cube can some times he extracted by means of the Rules for square and cube coot; thus the 4th root is found by taking the squar root of the square root; the 6th roct by taking the squar root of the cube root, and so on.

Ex. LXXVIII.

Find the cube roots of

1728; 8000; 5832.

(2) 74088; 421875; 778688.

- (3) 912673; 1092727. (4) 134217728 : 64·481201.
- (5) 444194 947; 000202262003.
- (6) 131 019108039; 408518488000.

Find the cube roots, to three places of deciroals in those cases where the root does not terminate, of

 $(7) \quad \frac{27}{63}$. (10) (8) 🔩. (9) $3\frac{4}{5}$. (11) ·1. (12) ·01. (13) 10. (14) ·037.

MISCELLANEOUS QUESTIONS.

Ex. LXXIX.

PAPER I.

- 1. Subtract 2057312 from 5287201, and 2057312 again from the remainder. Explain how this is the same as dividing 5287201 by 2057312.
- 2. (1) Reduce 553553 oz. to tons, cwts., &c. (cwt. = 112 (bs.) (2) Find the proportion of the Avoird and Troy oz. when the respective lbs. are as 175: 144.
- 3. Find, by Practice, the cost of 16 cwt., 3 grs., 16 lbs. at £2. 7 cents a cwt., (112 lbs. = cwt.) f^1 being = 10 florins = 100 cept -= 1000 mils.
- 4. Define (1) the G. C. M., (2) the L. C. M., of two or more numbers. (3) a Vulgar Fraction. Find the G. C. M. of 20803 and 67273; and the L. C. M. of 8, 9, 10, 12, 15, 18, 35 and 84.
- 5. (1) Add together \(\frac{3}{5} \) of \(\frac{5}{15} \) of \(\frac{9}{15} \), \(\frac{5}{5} \) of \(\frac{3}{5} \) of \(\frac{3}{5} \) of \(\frac{5}{3} \) of \(\frac{5}{3} \) of 3061. (2) Express 13s. 11d. as the fraction of 1 of 11 guinea. (3) Find the value of 197 ton (cwt. = 112 lbs.).

6. State the Rule for the division of one decimal by another. Divide (1) 7792.2 by 37, (2) 0077922 by 370; rerify each result by vulgar fractions.

PAPER II.

1. Define Interest, Simple and Compound. How does Interest differ from Discount? Find (1) the int. on \$7300 at 3\frac{3}{4} per cent. for 120 days, (2) the discount on £3204. 14s. 1d. at 2\frac{3}{4} per cent. simp. int. for 2\frac{3}{4} yrs.

2. A house built for \$2656 is sold for \$3320, find the gain per cent. If it had been built for \$3320 and sold for \$2656, find the loss per cent.? Why do the rates differ?

3. Define a square. Find (1) the sq. root of 930372004, (2) the cub. root of 16777216, (3) the perimeter of a square whose surface is 2533 sq. ft., 64 sq. in.

4. Multiply 365 separately by 5, by 20, and by 300, and dd the products together. Point out how the ordinary method of multiplying 365 by 325 agrees step by step with the above.

5. Define prime and composite numbers. Resolve 22932

nto its prime factors.

6. A person left Toronto for Guelph at 9 A.M., and ravelled the first 20 miles by rail, at the rate of ?21 miles an hour; he then walked the remaining 32 miles at \(\frac{1}{6}\) of shat rate. At what o'clock did he arrive?

PAPER III.

- 1. A and B fire at targets, having 55 cartridges each. A ures twice in 3 minutes, and B three times in 5 minutes; now many times will B have to fire after A has finished?
- 2. $\sqrt{(1)}$ Convert $\frac{17}{20 \times 8}$ into a decimal; why is the result a terminating, and not a recurring decimal? (2) Express 3s. $0\frac{1}{2}d$. as the decimal of £5. (3) Which is greater, '26 of a guinea or '36 of £1? (4) By how much?
- 3. What sum of money will amount to \$552.50 in 12 mo at 5 per cent, simp. int.?
- 4. A room whose height is 11 ft., and length twice its breadth, takes 143 wds. of paper 2 ft. wide for its four walls how much carpet will it require?
 - 5. Twoclocks strike o together on Tuesday morning

On Wednesday morning one wants 10 minutes to 11 when the other strikes 11. How much must the slower be put on that they may strike 9 together in the evening?

6 A person bought 43 shares in a coal time at 354, and and kept them till they declined to 11' when he sold out and bought with the proceeds 6 per cent, bank stock at 28 permium, find his annual income from the latter investment.

PAPER IV.

- 1. Define a fraction, and show from your definition that $\frac{1}{2} = \frac{3}{6}$ (1) Add together $\frac{1}{6}$, $\frac{3}{3}$, $\frac{1}{15}$, and $\frac{5}{27}$, and find what fraction the sum is of $\frac{1}{6}$ of $\frac{4}{2\frac{7}{6}}$ (2) How many times cap 027 be taken from 3:33? What fraction is the remainder of the former?
- 2 A person left a sum of money which was divided equally amongst 43 poor people, such that after a deduction of 6d, in the pound, each received £3. 3s $4\frac{1}{2}d$. What sum did he leave?
- 3. (1) If the carriage of 13 cwt., 2 qrs., 19 lbs. for 35 miles cost £4 178 6d., what must be paid for the conveyance of 41 cwt., 1 lb for 49 miles? (A cwt.= 112 lbs.) (2) A bankrupt owes \$2085, of which \$235 is due to A, \$325 to B, \$525 to C, and the rest to D. How much must he pay in the \$ so that D may receive as much as is due to C?
- 4. A merchant buys 2 butts of wine, one for £120, and one for £110, he also buys a third, and after mixing the three, retails the wine at 45s per dozen, making 12½ per cent. on his outlay: supposing the number of dozens in a butt to be 52, find the price of the third butt
- 5 The price of 2 turkeys and 9 fowls is £2 18s 6d and the price of 5 turkeys and 2 fowls is £4.8s 2d, find the price of a turkey and 2 fowl.
 - 6. How long will it take to walk round a square field ontaining 13 ac., 81 yds, at the rate of 3½ miles an hour?

PAPER V.

1 Find the product of the following numbers:—
(1) 3916 × 769. (2) 98367 × 9876. (3) 60706 × 7095.
(4) 968175 × 39078. (5) 9487918 × 7982.

ě.

- ✓ 2. A merchant bought 974 yds. cloth, and sold it all for
 \$847.38, gaining \$301.94; what was the cost per yard!
- 3. A and B own together 120 acres, A having 24 acres more than B. A sells his share for \$84 per acre. B sells his share for the same amount as A; how much does B get per acre?
- 4. If potatoes be bought at \$20.35 and sold at \$21.32 per load, how much will be made on a sale amounting to \$6332.04?
- 5. A merchant sold 45980 bushels of grain that cost him 98 cents at a gain of 29 cents per bushel, and with the money bought 2299 head of cattle; how much did he pay for each?
- 6. If a milkman use a false measure containing '93 of a pint instead of a pint, out of how much will be have cheated his customers when he has really sold 23 gallons? pints?

PAPER VI.

- **1.** Find an length of a street in which the wheel of a barrow revolves exactly 150 times, the diameter of the wheel being $1\frac{1}{2}$ ft., and the ratio of the circumference to the diameter, 5.14159.1.
- 2. France is 128 millions of English acres, and the Pyrenees agreed over it would cover it to the depth of 115 feet; find the bulk of the Pyrenees in cubic feet.
- 3. What is the height of a closet 8 ft. 4 in., by 6 ft. 8 in., which will exactly contain 12 boxes 4 ft. 6 in. long, 3 ft. 4 in. wide, 2 ft. 6 in. deep?
- 4. What sum of money must be left, in order that after a reduction of ten per cent. has been made, the remainder being invested in the 5 per cents. at 91½, may give a yearly income of \$100?
- 5. A ship worth \$6000 is entirely wrecked. \$3000 belonged to A, \$2000 to B, and the rest to C. What are the respective losses to A, B and C, supposing the ship to have been insured only to the amount of \$4500.
 - 6. A can do a piece of work in 27 days, and B in 12 days

A works at it alone for 12 days, B then works 5 days, and afterwards C finishes it in 4 days. Find the time in which C alone could do the whole work.

PAPER VII.

- 1. Find the product of the following numbers :—(1) 78398670×90785 . (2) 9703978×679458 . (3) 96870×708963 . (4) 897463287×30974 . (5) 906870690×90087 .
- 2. Two boys go fishing: one catches 40 chub, 30 perch, and 26 trout; the other catches an equal number of each, in all 90 fish. They sell them, a chub for 5c., a perch 8c., and a trout, 12c.; how much does each receive?
- 3. A case of strawberries contains 54 boxes, each 1 lb. in weight at 7c. a box. What will be the cost of canning 2 cases, allowing 1 lb. sugar at 10c. to every 2 lbs. berries?
- 4. Each man in an army of 60000 men gets two pairs of socks per year. How many sheep, each fleece 6 lbs., are necessary to supply wool for the socks, 1 lb. wool making 8 socks!
- 5 Jones and Smith are farmers. Jones sold last year 200 bush. oats at 38c., 73 bush. peas at 81c., 580 bush. wheat at 98c., 156 bush. potatoes at 29c., 138 bush. barley at 87c. Smith sold 45 sheep at 85, 60 lambs at \$3.30, 18 young cattle at \$15, 18 large cattle at \$29, and 26 tons hay at \$19. What sum did each receive?
- 6. A merchant sold a cargo of wheat valued at \$40000 for $\frac{1}{8}$ less than this amount, thus making a profit of only $\frac{1}{6}$ on cost. At what advance on cost was the wheat valued at in the first instance?

PAPER VIII.

- 1. Find the product of the following numbers:—(1) 987798640×10970. (2) 793289765×40097. (3) 7968×8679. (4) 874598×39076.
- 2. A shopkeeper bought \$9.60 worth of steel pens at 32 cents per box, each containing 12 dozen, and retailed them at 5 cents per dozen. How much did he gain on his outlay!

- 3. A person distributes \$22.68 amongst six men, eight women and twelve boys. Each woman had three times as much as each boy, and each man half as much again as each woman. Find what each received.
- 4. Goods were bought for 8648 dollars; there was further paid for packing, 20 dollars; for lake carriage, 55 dollars; for land carriage, 115 dollars; and for other charges, 350 dollars. The goods were then sold for 10000 dollars. What was the profit made on the sale?
- 5. Divide 1120 cents between three boys, Alfred, Benjamin and Charles, so that Alfred may have three times as much as Benjamin, and Charles as much as Alfred and Benjamin together.
- 6.. In 1871 the population of England and Wales was 22704108; of Scotland, 3358613; of Ireland, 5402759; of islands in the British seas, 144430; and of the army and navy, &c., 207198. Find the total population of the United Kingdom at that date.

PAPER IX.

- 1. Divide (1) 6022808 by 769; (2) 1942944984 by 987e (3) 55596055703076 by 15487; (4) 326789039400120 by 90087.
- 2. If a locomotive travelled from Toronto to Whitby at a uniform rate of 880 yards a minute, it could perform exactly the distance in 60 minutes; find the distance between the two places in yards.
- 3. Three men, A, B and C, start on a journey, each with 126 dollars in his pocket, and agree to divide their expenses equally. On their return home, A has 106 dollars, B has 56 dollars, and C has 66 dollars. What ought A to pay B and C to settle their accounts?
- 4. A farmer bought two farms, each of 130 acres, for 19500 dollars. What is the value of an acre of each farm, if two acres of one be worth three acres of the other?
- 5. A gentleman in Toronto remits \$10696.93\frac{1}{3} to a friend in Londov. How much does it amount to in London. exchange at '09\hat{k} commission \frac{2}{3} \frac{2}{3} \text{-xtra} \frac{1}{3}

6. Brown, in London, has £715 stg. He sends it to a friend in Toronto. How much does the friend realize, exchange at 100%, commission \(\frac{1}{2} \) \(\text{extra?} \)

PAPER X. (ADMISSION TO HIGH SCHOOLS.) 1877.

- 1. How often is 6 yds. 2 ft. contained in 25 furlongs .
- 2. If I buy 3 bushels, paying 5 cents for every 3 quarts, and sell at a profit of 10 cents per gallon, find the selling price of the whole.

3. Simplify
$$\frac{2\frac{1}{2} + \frac{5}{8} \text{ of } 12 - \frac{5}{6}}{3\frac{1}{3} \times 01 + \frac{9}{10}} \times \frac{11}{3\frac{5}{3}} \times \frac{18\frac{1}{12} + 5\frac{8}{15} - 22\frac{23}{30}}{\frac{1}{12\frac{1}{7}} \div (2\frac{7}{10} - \frac{5}{8} + 4)}$$

- Reduce 2 hrs. 20 min. to the decimal of 3½ weeks.
- 5. A sum of money was divided among A, B and C. A received $\frac{2}{5}$ of the sum; B, \$20 less than $\frac{2}{3}$ of what was left; and the remainder, which was $\frac{3}{4}$ of A's share, was given to C. Find the sum divided.
- 6. Trees are planted 12 feet apart around the sides of a rectangular field (40 rods 'ang) containing two acres. Find the number of trees.
- 7. I buy a farm contain. \mathcal{C}^{00} acres, and sell $\frac{3}{4}$ of it for $\frac{3}{2}$ of the cost of the farm; if then sell the remainder at 800 per acre, and neither gain nor lose by the whole transaction. Find the cost of the farm.
- 8. Find the amount of the following bill of goods:— $^{\bullet}$ $18\frac{3}{4}$ cords of wood, at \$3.50 per cord. 16 yards of cloth at \$1.12 $\frac{1}{2}$ per yard. 12 bush. 25 lbs. of wheat, at \$1.24 per bush. 1,490 feet of lumber, at \$12.50 per thousand. 65 tons 12 cwt. of coal, at 30 cents per cwt.

PAPER XI. (ADMISSION TO HIGH SCHOOLS.) 1878.

- 1. Define prime number, multiple of a number, highest common factor of two or more numbers, ratio between numbers. Find the prime factors of 1260.
- 2. The quotient is equal to six times the divisor; the divisor is equal to six times the remainder, and the three together, plus 45, amount to 561. Find the dividend.

- 3. I sell $12\frac{1}{2}$ tons of coal for \$80, which is one-seventh more than the cost. Find the gain per cwt.
 - 4. $.001 \times .001 \div .0001$.
- 5. A cistern is two-thirds full, one pipe runs out and two run in. The first pipe can empty it in eight hours, the second can fill it in twelve hours, and the third can fill it in sixteen hours. There is also a leak half as large as the second pipe. In how many hours will the cistern be half full?
- 6. Ten men can do a piece of work in twelve days. After they have worked four days, three boys join them in the work, by which means the whole is done in ten days. What part of the work is done by one boy in one day?
- 7. I buy a number of boxes of oranges for \$600, of which 12 boxes are unsaleable. I sell two-thirds of the remainder for \$400, and gain on them \$40. How many boxes did I buy?
- 8. Find the total cost of the following:—Cutting a pile of wood 80 ft. long, 6 ft. high, and 4 ft. wide, at 60c. per cord. Digging a cellar 44 ft. long, 30 ft. wide, and 8 ft. deep, at 18c. per cubic yard. Plastering a room 24 ft. long, 16 ft. wide and 10 ft. high, at 15c. per square yard. Sawing 6800 shingles, at 40c. per 1000.

The Independent Method, or the Method of Reduction to the Unit, introduced at page 89, may with advantage be employed to solve questions which can also readily be done by the Rule of Three. We subjoin a few more examples, showing how to apply the method referred to

1. If 27 men build a house in 63 days, in how many days will \$\pm\$2 men do the same !

27 men build a house in 63 days; \therefore 1 man " 63×27 days; \therefore 42 men " $\frac{63 \times 27}{42}$ days;

: Number of days required = $\frac{63 \times 27}{42}$ = $40\frac{1}{3}$.

- 2. A person rows down a stream in 20 minutes, but without the aid of the stream it would have taken him half an hour. What is the rate of the stream per hour, and how long would it take him to row against it !
 - 1st. Moving with stream:

In 20', distance rowed = $1\frac{1}{2}$ miles; \therefore in 1', "= $\frac{3}{40}$ miles.

2nd. Moving in still water:

In 30', distance rowed = $1\frac{1}{2}$ miles; in 1', $=\frac{1}{60}$ miles;

 \therefore rate of stream = $\frac{3}{40} - \frac{1}{20} = \frac{1}{40}$ miles;

.: rate of stream per hour, $\frac{1}{40} \times 60 = 1\frac{1}{2}$ miles. Rate of stream in $1' = \frac{1}{40}$ miles,

in still water, distance rowed $=\frac{1}{20}$ miles;

:. distance rowed against stream = $(\frac{1}{40} - \frac{1}{10})$ miles;

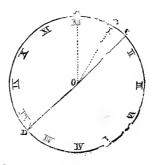
: time required to row $1\frac{1}{2}$ miles $=\frac{3}{2}$ $\div \frac{1}{40}$ $=\frac{3\times40}{2}$ =

60'=1 hour.

- 3. At what time between 1 and 2 are the hands of a clock opposite to each other?
- Let OC be the position of the hr. hand.
- Let OD be the position of the min. hand.
- At 1 o'clock OC overlapped OB, and OD overlapped OA.
- Then BC space passed over by hr. hand, and AD space passed over by min. hand.

12 times BC = AD (1).

But AD = AB + BC + CD. = a = 0.11in, a = BC + 30 min.



- . substituting this value or A D for A D in (1), we have 12 times BC = 35 min. + B. C.
- \therefore 11 times BC=35 min.,

or $BC = 35 \text{ min.} \div 11 = 3\frac{2}{11} \text{ min.}$

:. $AD=35 \text{ min.} + 3\frac{2}{11} \text{ min.}$

. time required is $38\frac{2}{11}$ min. past 1 o'clock.

In connection with the above we give the following statement: Since the minute hand moves twelve times as fast as the hour hand, therefore in 12 minutes the minute and gains 11 minute spaces on the hour hand.

The hands of a clock are together at 12, when will hey be together again?

The time must be after one; therefore the minute hand has 5' to gain.

- 11 minute spaces gained in 12';
- 1 minute space gained in \frac{12}{12};
- 5 minute spaces gained in $\frac{12 \times 5'}{11}$;
- :. time required is $5\frac{5}{11}$ past 1.
- After paying an income tax of \$10 on a \$100, a person has \$2700 a year. What was his entire income?
 - -10 on a $100 = \frac{1}{10}$ on a unit;

 - . po of every unit of income left.
 ∴ po = \$2700;
 ∴ po = \$300;
 ∴ po = \$300;
 ∴ 1, or whole income = \$300 × 10 = \$3000.
- 6. A stock of provisions will serve 75 men for 30 days. How many men must leave in order that the stock may held out 45 days for those left?

Provisions last 30 days for 75 men; 1 day for 75×30 men,

" 45 days for $\frac{75\times30}{45}$ men, or 50 men.

Hence the number of men who must leave = 75 - 50 = 25

Exercise LVI., &c., furnish examples.

EXCHANGE is the Rule by which we find how much money of one country is equivalent to a given sum of another country, according to a given Course of Exchange.

By the Course of Exchange is meant the variable sum of the money of any place which is given in exchange for a fixed sum of money of another place.

By the PAR OF EXCHANGE is meant the intrinsic value of the coin of one country as compared with a given fixed sum of money of another.

ARBITRATION, or COMPARISON OF EXCHANGES, is the method of fixing upon the rate of exchange, called the PAR OF ARBITRATION, between the first and last of a given number of places, where the course of exchange between the first and second, second and third, &c., of these places is known. It is called SIMPLE OF COMPOUND ARBITRATION, as three or more places are concerned. (For fuller information on Exchange, see Advanced Arithmetic, p. 227, &c.)

By an Act of Parliament passed many years ago, the sovereign was declared to be only equal in value to \$4.44, or £9 (sterling) = \$40; and this is the value which is almost invariably quoted in mercantile transactions; the premium on this depreciated value of the sovereign which will make it equal to its intrinsic value, is $9\frac{1}{2}$ per cent.

1. A person has to transmit to Britain £450 stg.; the rate of exchange is at 6 per cent. premium, and he is charged ½ per cent. for commission. What will the bill of exchange cost him in our currency?

Rate of exchange to the buyer is $106 + \frac{1}{2} = 106\frac{1}{2}$;

£1 =
$$\$^{40}_{9} \times \frac{106\frac{1}{2}}{100}$$
;
£450 = $\$^{40}_{9} \times \frac{213}{200} \times 450$,
= \$2130.

Hence the bill of exchange costs the buyer \$2150

2. A person sold in Paris a bill worth in London 1275 . 5s. for 32148f. 90c. What was the course of extange between these two cities.

£1275·75 = 32148·90f.;

$$\therefore £1 = \frac{3214890}{127575}f.$$
= 25f. 20c.:

therefore the course of exchange is 25f. 20c. for £1 stg

PAPER XII.

- 1. What would a currency draft on New York for \$504 cost in gold, if it be purchased when gold is quoted at \$ % premium, the broker charging \$\frac{1}{4}\$ % commission?
- 2. How much gold would one get for \$1234, U. S. cur rency selling at 2 % discount?
- 3. What would a person have to pay for \$400 U. S currency at 99?
- 4. You sell \$1127 in gold for currency--gold = 102 How much do you receive?
- 5. A, in Toronto, owes B, in London, £360 stg. Ex change, 1104. What will be the cost of a draft to cover the amount?
- 6. Jones, in London, sells 60 shares, £100 each, M R y stock, at a premium of 9 %, and invests the proceeds in O. B. stock, in Toronto, at 96. Exchange between London and Toronto, 109. How many dollars does he invest in O. B. stock.
- 7. A Toronto house owes £278 18s. 9d. in Manchester; how much will be required to discharge the debt in Canadian currency, rate of exchange being at 8\frac{3}{4}\% premium \(\)
- 8. A merchant in Montreal has to pay a bill of 1387f 18c. in Paris. Find the amount he will have to remit tor payment of the bill, it being known that the sovereign is worth 25f. 20c., and exchange on England in Montreal at a premium of $7\frac{\pi}{8}$ per cent.

- 9. If \$8800 are required in Toronto to pay £1800 in London, England, find the rate of exchange between the two cities.
- 10. A traveller for Paris wishing to provide himself with French money, calls at a broker and is informed that the sovereign in London is worth 25f. 25c., rate of exchange on London, $8\frac{1}{2}$ premium, and $\frac{1}{2}$ per cent. commission. Find the sum in French money he ought to receive for \$500 of our money.

PAPER XIII.

1. Divide

- (1) 36617079414410 by 160388.
- (2) 75732561476 by 9487918.
- 2. If a gallon contain 277 274 cubic inches, and a cubic foot of water weigh 1000 ounces, what quantity in gallons and what weight of water in pounds will fill a rectangular cistern 5 feet long, $3\frac{1}{2}$ feet wide, and 2 feet 9 inches deep?
- 3. Find the depth of the circular cistern which would hold the same quantity of water as that in question 2, supposing the diameter to be 6 feet.
- 4. A cubical box exactly holds 64 shot, each 3 inches in diameter. Find how many cubic inches are empty in the box when it is full of shot.
- 5. Find the length of the side of a square whose area is equal to that of a rectangle, the sides of which are 94.28 and 6720 yards.
- 6. Add together one million one thousand and ten, fifty thousand five hundred and five, ten millions, five hundred thousand and fifty, seventy millions seven hundred thousand and seventy, eight billions eight hundred thousand and eight. From the sum take 51643, and divide the remainder by 808.

PAPER XIV

Divide

(1) 369487500983860 by 1978

(2) 976875783291415 by 389

- Write Avoirdupois weight.
 Express 1 cwt. 2 qrs. 15 lbs., in Troy Weight.
- 3. In 2784583 inches how many miles, furlongs, poles, &c., are there? Find how long a man going at the rate of 4 miles an hour would take to walk the number of miles, &c., in your result?
- 4. Define the least common maltiple and the greatest common measure of two numbers. If the greatest common measure of two numbers be 103, and their least common multiple be 14729, find the numbers.
- 5. Define a vulgar fraction. Distinguish between a vulgar and a decimal fraction. Multiply together, expressing the resulting fraction in its lowest terms, $1\frac{3}{11}$, $\frac{9}{14}$, $\frac{4}{7}$, $9\frac{5}{12}$, and $\frac{6}{113}$.
- 6. Divide 238095 by 3428571, and extract the square root of the quotient.

PAPER XV

- 1. Write square or land measure. How many square inches in 2 ac. 3 r. 5 p. 5 yds.?
- 2. Define simple interest and amount. At what rate per cent. per annum will a sum of money double itself at simple interest in 10 years?
- 3. A school section is valued at \$13740. The section is required to raise by rate a sum of \$820.40. What is the rate per \$1?
- 4. A person invests \$6477 in the 6 per cent. Dominion of Canada stock at $101\frac{1}{4}$, and when it has risen to 106 he sells out and invests the proceeds in a $4\frac{1}{4}$ per cent. stock at 70. Find gain or loss in incorne.
- 5. A bill on London for £960 stg. costs \$4640. What in the rate of exchange?
- d. What will a bill on London for £1620 cost in Toronto, e change at 109½, commission ½ % extra?

The two following Tables may be added to those given on pp. 44-50.

TABLE & APOTHECARIES' WEIGHT.

Table as given in British Pharmacopæia.

$437\frac{1}{2}$	\mathbf{Grains}	make	16,000
16	Ounces		1 Pound

The grain is the same as the grain Troy; the ounce rathe same as the ounce evoirdupois.

APOTHECARIES' FLUID MEASURE.

In this measure, tounded on the fact that a pint of pure water weighs 20 ounces:

60 Minims make	1 Fluid Drachmfl. dr.
8 Fluid Drachms	1 Fluid Ouncefl. oz.
20 Fluid Ounces	1 Pmt o; octavius.
⊁ Pints	1 Gallonc; congius.

MENTAL ARITHMETIC.

SECTION VI.

MENTAL ARITHMETIC.

148. The following table will be found useful.

Multiplication and Division Table.

_																		-	_	_
	20	19	18	17	16	15	14	13	12	=	10	9	œ	7	င	O.	4	ယ	ю	
-	20	5	3	17	16	15	14	3	12	1	0	9	8	7	6	5	4	ယ	12	-
10	40	38	36	32	32	30	28	26	24	22	20	8	16	14	13	5	œ	င	4	ю
ဃ	8	57	54	51	48	45	42	39	36	<u>ಜ</u>	30	27	24	2	$\overline{\mathbf{s}}$	5	12	9	6	ಬ
4	80	76	72	68	2	60	56	52	48	44	40	36	32	83	24	20	16	12	8	4
51	8	95	90	85	SO	75	70	65	8	55			40	ည္	30	25	20	15	01	57
6	120	114	108	201	96	90	84		72		8	54	48	42	36	30	24	18	12	6
7	140	133	126	2 119	112	105	98	91	84				56		<u>3</u>		28		14	7
8	0 160	3 152	6 144	9 136	2 128	5 120	112	104	96	88	80	72	64	56	48	40	32	124		- 00
9									I —		_	_	4 72	63	_	_	36			9
-	180 2	171 1	1621	153 1	144 1	135 1	126 1	117,1	108	99	90	-	_	_	-			_	_	_
5	200	190	180		160	150	140	130	120 132	110	9	8	S	0	8	8	6		_	_
	220	209	198	187	176	165	154	143		121	10	99	88	77	6	55	4	ಜ	15	Ξ
2	240	228	216	204	192	180	168	5	144	132	120	108	96	84	72	60	8	36	24	12
3	260	247	234	221	208	195	182	169	156	143	130	711	101	91	3	9	52	39	25	- ئنة
4	082	266	252	238	224	210	196	182	168	151	140	126	112	98	20	_	56	42	Ser	14
15	300	285	2270	5 255	240	225	3210	195	8180	165	0 150	6 135	2 120	105	9	75	8	45	30	=
16	0330	5 304	0 288	5 272	0 256	5 240	0 224	5 208	0 192	5 176	0 60	5 144	0 128	5 112	96		64	48	32	إيّ
_				12	20	0		3										$\overline{}$	-	-
7	30	353	3063	289 3	272 2	255 2	238 2	221 2	204 2	187	170 1	153 1	136	191	102	85	68	51	34	7
18	360	342	324	306	288	270	252	234 :	216:	198	180	65	14.	126	<u>s</u>	9	72	54	36	18
5	380	361	342	323	304	285	266	247	228	209	190	171	155	$\frac{1}{2}$	14	95	6	5;	8	19
20	8	380	360	340	320	8	280	260	240	220	200	180	160	041	120	9	8	ଞ	3	20
		_			-	-					_				_					_

149. Such questions as 7+8+3, &c., are how many? and 29 less 7, less 6, &c., are how many? or questions in which addition and subtraction are combined, we omit; because, any teacher, by a little practice, can very easily give such exercises to the class, and, moreover, every practical teacher knows that much of the value of this part of the Arithmetic depends on the pupil not having seen the questions before the lesson begins.

150. To find the value of 12 things, the value of one thing

being given.

RULE. Reckon each penny in the given value as a shilling, and each farthing as 3d.

Ex. Find the value of 12 things at 15% d. cach.

By the Rule,

The value reqd. = 1s. \times 15 + 3d. \times 3 = 15s. 9d.

Reason for the Process.

12 things at 1d. each = 1s.; ... 12 at 15d each = 1s. × 15 = 15e 12 $\frac{1}{4}d$=3d.; ... 12 at $\frac{3}{2}d$=3d. × 3 = 9d.; ... 12 things at $15\frac{3}{4}d$. each = 15s. 9d.

151. To find the value of 24 things, the value of one thing being given.

Rule. Reckon each penny in the given value as 2s, and each farthing as 6d.

152. To find the value of 48 things, the value of one thing being given.

RULE. Reduce the given value into farthings, the result reckoned as so many shillings will be the value required.

Ex. Find the value of 48 things at 183d. each.

By the Rule, since $18\frac{3}{2}d$. = 75q.

the value req^d. = 75s. = £3. 15s.

Reason for the Process.

48 things at $\frac{1}{4}d. = 48q. = 18.$;

...48 things at 75q. = 1s. \times 75 = 75s. = £3. 15s.

153. To find the value of 144 things, the value of one thing being given.

RULE. (1) Find the value of 12 things by Rule 150: them consider this value as the value of one thing, and apply Rule 150 a second time.

Ex. Find the value of 144 things at 131d. each.

Value of 12 things = 13s. + 6d. = 13s. 6d.

Value of 144 things = $13s. \times 12 + 6s. = 156s. + 6s. = £8.2s.$

154. The following general Rule may be given "for finding the value of any number of things, the value of one thing reing given."

RULE. Reckon how many dozens are contained in the given number, and how many single things remain over. Then by Rule 150, find the value of one dozen, which value or ultiply by the number of dozens, and add to the result the price of the single things which remained over.

Ex. Find the value of 38 things at 4. 7d. each.

Ex. LXXX.

- 1. Find the value of 12 articles at the following prices for a single article. (1) $\frac{2}{4}d$. (2) 2d. (3) 5d. (4) 7d. (5) 11d. (6) $1\frac{1}{2}d$. (7) $2\frac{1}{4}d$. (8) $3\frac{3}{4}d$. (9) $6\frac{1}{2}d$. (10) $3\frac{1}{4}d$. (11) $10\frac{1}{2}d$. (12) 1s. $0\frac{3}{4}d$. (13) 1s. 4d. (14) 1s. $6\frac{1}{4}d$. (15) 1s. $9\frac{3}{4}d$. (16) 1s. 8d. (17) 1s. $11\frac{1}{2}d$. (18) 1s. $2\frac{3}{4}d$. (19) 2s. 7d. (20) 3s. $0\frac{1}{4}d$. (21) 4s. 4d. (22) 6s. $1\frac{3}{4}d$. (23) 7s. 9d. (24) 8s. $5\frac{1}{2}d$. (25) 11s. $7\frac{3}{4}d$. (26) 13s. 2d. (27) 16s. $3\frac{1}{4}d$. (28) 18s. $1\frac{1}{4}d$. (29) 19s. 9d. (30) 19s. $6\frac{3}{4}d$.
- 2. At the prices named as the value of a single article in (1) to (12) inclusive in the last question find the value of 24 articles; at the prices named in (13) to (20) inclusive find the value of 48 articles; and at the prices named in (21) to (30) inclusive find the value of 144 articles.
- 3. At the prices named as the value of one article in quest. 1. (6) to (20) inclusive, find the value of (1) 13; (2) 21; (3) 28; (4) 35; (5) 41; (6) 44; (7) 57; (8) 72; (9) 153; (10) 182 articles.
- 155. To find the value of 20 things, the value of one thing being given.

RULE. Reckon each shilling in the given value \approx 31, and if there be pence, reckon each penny as the twelfth of £1, thus 1d as 1s. 8d., and if there be farthings, each farthing as re-fourth the value of each penny, or 1q. as 5d. &c.

Fix. Find the value of 20 things at 2a 81d. each.

By the Rule,

The value required = £1 × 2 + (18. 8d.) × 8 + 5d. × 2. = £2 + 13s. 4d. + 10d. = £2. 14s. 2d.

Reason for the Process.

20 things at 1s. = 20s. = £1; \therefore 20 things at 2s. = £1 \times 2 = £2,

20 things at 1d = 1s. 8d.; ... 20 things at 8d. = 1s. 8d. $\times 8 = 13s$. 4d.

20 things at $\frac{1}{2}d = \frac{1s. 8d.}{2}$, or 20 things at $\frac{1}{2}d = 10d.$;

... value of 20 things at 2s. $8\frac{1}{2}d_1 = £2$. 14s. 2d.

156. To find the value of 100 things, the value of one thing being given.

RULE. Reckon each shilling in the given value as £5; reduce the pence and farthings in the given value to farthings, then reckon each farthing as equal to 2s. 1d.

Ex. Find the value of 100 things at 2s. 51d. each

By the Rule, since $5\frac{1}{4}d$, = 21q.

The value req^d. = £5 × 2 + 2s. × 21 + 1d. × 21. = £10 + £2. 2s. + 1s. 9d. = £12. 3s. 2s.

Reason for the Process.

100 things at $2\lambda = £5$; \therefore 100 things at $2s = £5 \times 2 = £10$.

Again since 1d. = 4q., taking 1q. as equal to 1d., we multiply by 4.

Also, since 2s. = 96q., taking 1q. as equal to 2s., we multiply by 96;

.: taking 1q = 2s + 1d, we multiply by 96 + 4, or 100.

157. To find the interest of any sum of money for any number of months at 6 per cent.

RULE. Divide the number of months by 2; the quotient is the interest in cents of \$1 for the given time; multiply the quotient by the given principal and the product is the interest required.

Ex. 1. Find the interest on \$78.56 for 2 yrs., 7 mo., at 9 per cent. per annum.

By the Rule,

2 yrs. 7 mo. = 31 months; $\frac{81}{3}$ = 15½ \therefore int. req⁴. = 15½ \times \$78.56 = \$12.1768.

Reason for the Process.

The interest of \$1 for 1 month = $\frac{1}{2}$ cent.

.. half the number of months will express the interest in cents of \$1 for the given time

Note 1. It will be quite easy to obtain from the above the interest at any other rate than 6 per cent.; by first obtaining the interest as directed above and then by Practice to add or subtract as the case may require.

Ex. 2. Find the interest of \$80 for 15 months at 8 per cent. per annum.

At 6 per cent. int. = \$6, as by the above Rule;

... at 8 per cent. int. = $\$6 + \frac{1}{3}$ of \$6.

= \$8.

Ex. 3. Find the interest on \$110 for 10 months at 5 per cent. per annum.

At 6 per cent. int. = \$5.50 by the Rule; ... at 5 per cent. int. = \$5.50 — \$5.50. = \$5.50 — \$13 cents. = \$4.584.

Note 2. If there are days in the question, the interest may be found for \$1 by dividing the days by 6 and reckoning the quotient tenths of a cent. which being added to the result obtained in the Rule, will give the interest of \$1 for months and days, and consequently for any amount.

Ex. 4. Find the interest on \$90 for 6 months and 24 days at 6 per cent per annum.

Int. on \$1 = 3.4 cents, by the Rule; ... int. on $$90 = 3.4 \text{ cents} \times 90$. = \$3.06.

Ex. LXXXI.

Find the interest at 6 per cent. per annum; (1) On \$37 for 4 months. (2) On \$42 for 6 months. (3) On \$55 for 8 months. (4) On \$75 for 10 months. (5) On \$110 for 7 months. (6) On \$38.50 for 9 months. (7) On \$84.25 for 12 months. (8) On \$120 for 15 months. (9) On \$228 for 18 months. (10) On \$678.50 for 8 months. (11) On \$422.25 for 9 months. (12) On \$328.50 for 9 months.

ANSWERS

Ex. I. (p. 10.)

1. 3, 4, 2, 7, 9, 6, 8. 2. 10, 1, 12, 19, 5, 11, 16. \$. 14, 20, 27, 33, 49, 60, 55, 17, 36. 4. 88, 35, 63, 29, 76, 80, 94, 13, 52. 5. 9, 10, 11, 12, 13, 14, 15, 16, 17; 46, 47, 48, 49, 50; 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98.

Ex. II. (p. 11.)

1. 106, 150, 200, 287, 310, 431, 555, 919, 867.

2. 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213; 612, 613, 614, 615, 616, 617, 618, 619; 948, 949, 950, 951, 952, 953, 954, 955, 956, 957, 958, 960, 961, 962, 963, 964, 965, 962, 967, 968, 969.

Ex. III. (p. 12.)

1. 4585, 7321, 9798, 7006.

2. 5004, 5400, 5040, 8036, 8306, 8360, 9909.

3. 75635, 90909, 10004, 87050, 90001, 64064, 53000.

Ex. IV. (p. 13.)

1. 105, 8790, 37071, 30402, 77700, 24817.

2. 105409, 8008013, 7650090, 64000400, 89044001. 504623024, 900300800, 53000503.

3. 6006070007, \$3401001010, 7004089200, 99000000\square

Ex. V. (p. 14.)

1. Seven, thirteen, four, nine, eighteen, five, twenty, eleven, five, fifty, thirty-four, twenty-nine, three, seventeen, fifty-three.

2. Nineteen, eight, forty-one, eighty-eight, twenty-seven, seventy-two, ninety-four, forty-nine, sixteen, sixty-one, nine-

ty-eight, eighty, fifty-six, twenty-eight.

3. One hundred and seven, one hundred and seventy seventeen, four hundred and thirty, six hundred and ninety one, eighty, eight hundred, eight, sine hundred and fifty-six, eight hundred and three, six hundred and eighty-four.

4. Four thousand five hundred and six, five thousand eight

hundred and seventy, five thousand and eighty-seven, six thousand rine hundred, six thousand and nine, two thousand five hundred and eighty, seven thousand and forty-five, seven thousand five hundred and ninety-one, six thousand two hundred and seventy-five.

5. Twenty-four thousand seven hundred and fourteen, twelve thousand five hundred, ten thousand and twenty-five, ten thousand two hundred and five, seventy thousand four hundred and fitty-seven, seventy-four thousand and seven.

seventy-seven thousand.

6. Three hundred thousand eight hundred and sixty-three, shirty millions eighty thousand six hundred and thirty, nine-ty-six millions four hundred thousand two hundred and fifty, eight hundred millions four hundred thousand three hundred and seven, five hundred and seventy-two millions sixty thousand four hundred and ninety-five.

7. One hundred and twenty millions one hundred and ninety-two thousand seven hundred and three, eight hundred and ninety millions six hundred and forty-seven thousand five hundred and sixty, one billion and fifty millions sixty thousand four hundred and twenty-nine, one hundred

billions and one.

Ex. VI. (p. 16.)

1. 19. 2. 27. 3. 26. 4. 11; 16; 18; 18; 23; 17; 15; 18; 25. 5. 25; 20; 34; 28; 36; 45; 46. 6. 29 boys. 7. 12 vrs. 8. 30 chickens.

Ex. VII. (p. 19.)

4. 99. 1. 37. 2. 69. 99. 5. 95. 6. 71. 7. 115. **8.** 110. **9.** 200. 10. 214. 11. 213. 12. 186. 13. 214. 14. 241. 15. 503. 16. 1741. 17. 2133. 18. 1540. 19. 2201. 20. 1364. 21, 1920, 22. 1549. 23, 1551, 24. 2514. 25. 166**5**. 26, 2451. 28, 2018, **29.** 14658. **30.** 27640. **31.** 27832. 32. 35735. 33, 28260. 34. 29635. 35. 28207. 36. 100 marbles. **37.** 287. 38. 9770. 39. \$42068. 40. 3554 oranges.

Ex. VIII. (p. 20.)

2 316. 3, 295. 4. 291. 1. 148. **5. 340. 6.** 1851. 7. 2124. 9. 3166. 11. 336508. 8. 3216. 10. 2974. 13. 400257. **12**. 323915. 14. 358064. 15, 152375, 16. 37155818. 17. 24601758. 18. 171357568. 19. 260342506, 20. 222275 21. 186839. 22. 72268. 23. 194207.

Ex. IX. (p. 21.)

 1. 2643560.
 2. 5074223.
 3. 226987.
 4. 9948524,

 5. 80169315.
 6. 1642844613.
 7. 5481487220.
 8. 3582727022.

 9. 5198944018.
 10. 2553242166.
 11. 4803131181

 12. 6137065059,
 13. 434883345.
 14. 100.
 15. 982

 16. 83185.
 17. 165802.

Ex. X. (p. 25.)

Ex. XI. (p. 26.)

1. 1921. 2 3711. 3 999 4 2239. 5 4484. 6 1929. 7. 3205. 8. 4684. 9. 3401. 10. 7889. 11. 3025 12. 896. 13. 25184. 14. 21023. 15. 8. 16. 18173 17. 168079. 18. 8639494. 19. 19075299. 20. 555939946 21. 2899; 997833. 22. 5986. 23. 15022. 24. 1891; 72 25. 68; 140. 26. 8217 in debt. 27. 19th step from bottom, 26th step from the top. 28. 5 officers, 58 children, 47 able-bodied, 23 infirm. 29. 682. 30. 45718. 31. 7096305 32. 56289613. 33. 66291414. 34. \$260. 35. \$8337588.

Ex. XII. (p. 28.)

2. three, 3; six, 6; eight, 8; thirteen, 13; fifteen, 15; seventeen, 17; twenty, 20; fifty-four, 54; eighty-one, 81; one hundred and eleven, 111; six hundred and five, 605; five thousand and two, 5002; one million one hundred thousand, 100000; two thousand, 2000; seven hundred and forty-nine, 749; one thousand eight hundred and sixty-five, 1865.

Ex. XIII. (p. 30.)

 1. 106.
 2. 94.
 3. 176.
 4. 112.
 5. 144.
 6. 180.

 7. 87.
 8. 225.
 9. 108.
 10. 204.
 11. 332.
 12. 450.

 13. 335.
 14. 215.
 15. 216.
 16. 594.
 17. 468.
 18. 189.

 19. 371.
 20. 360.
 21. 616.
 22. 621.
 23. 486.
 24. 200.

25. 990. 26. 583. 27. 957. 28. 1001. 29. 720. 30. 588⁻ 31. 1374. 32. 2400. 33. 2091. 34. 1104. 35. 3885. 36. 2982. 37. 3353. 38. 6335. 39. 6680. 40. 4383. 41. 5600. 42. 5918. 43. 10656. 44. 8448. 45. 429 bushels, 2574 shillings. 46. 756 pence, 1764 pence, 3024 pence. 47. 44 cents. 48. 44. 49. 885.

Ex. XIV. (p. 31.)

 1. 18096.
 2. 11698.
 3. 29619.
 4. 114228.
 5. 24228.

 6. 485340.
 7. 416160.
 8. 404825.
 9. 3073630.
 10. 388064.

 11. 231483.
 12. 346284.
 13. 590592.
 14. 833184.

 15. 234927.
 16. 1098444.
 17. (1) 7740984, 19352460,

 11611476, 27093444, 15481968, 34834428, 23222952, 30963926,
 42575412, **46445904**. (2) 9219516, 23048790, 13829274, **32268306**, **18439032**, **41487822**, 27658548, 36878064, 50707338, 55317096. (3) 171947728, 429569320, 257921592, 601817048, 343895456, 773764776, 515843184, 687790912, 945712504, 1031686368. (4) 18181706, 45454265, 27272559, 63635971, 36363412, 81817677, 54545118, 72726824, 99999383, 109090236. (5) 111760184, 279400460, 167640276, 391160644, 223520368, 502920828, 335280552, 447040736, 614681012, 670561104, (6) 1975308642, 4938271605, 2962962963. 6913580247, **3950617284**, 8888888889, 5925925926, 7901234568, 10864197531, 11851851852. 18. 98 miles. 19. 888 miles.

Ex. XV. (p. 34.)

1. 8334. 2. 18306. 3. 9108. 4. 32454. 5. 57706. 6. 32643. 7. 23790. 8. 22385. 9. 77341. 10. 42182. 11. 50516. 12. 79992. 13. 218075. 14. 281504. 25. 45468. 16. 303102. 17. 6964704. 18. 4328192. 19. 183150. 20. 331200. 21. 308163. 22. 250200. 23. 725912. 24. 1619723. 25. 52470000. 26. 492463028. 27. 7851033000. 28. 244366672. 29. 140645085. 30. 353440772. 31. 344115512. 32. 736924245. 33. 663503082. 34. 593928090000. 35. 8106030522. 36. 622439160. 37. 33146651; 1368500000; 791627400; 2808128627515. 38. 148672. 39. (1) 61299; (2) 51480000. 40. See 15, 16, 17, 18,

Ex. XVI. (p. 34.)

1. 43042883. 2. 131296032. 3. 4916047312. 4. 43506216.

 5. 31884470.
 6. 88789950848.
 7. 66260991808

 8. 40880656300.
 9. 69312233476002.
 10. 18381130075.

 11 100453365411.
 12. 157593610868.
 13. 8943214059.

 14. 27416327796.
 15. 109588282650.
 16. 60435674536845.

 17. 495562849756.
 18. 67226401140.
 19. 18834779670.

Ex. XVII. (p. 37.)

1. 14\$, 97, 11; 15\$, 10\$, 11\$; 16\$, 10\$, 12\$; 17\$, 11\$, 12\$; 16\$, 11\$, 12\$.

2. 21, 9_{11}^{6} , 10_{10}^{6} ; 22, 10, 11; 23_{6}^{4} , 10_{11}^{9} , 11_{10}^{9} ; 25_{6}^{3} , 11_{11}^{7} ,

 $12\frac{8}{10}$; $23\frac{2}{6}$, $10\frac{7}{11}$, $11\frac{7}{10}$.

3. $21\frac{4}{5}$, $10\frac{1}{12}$, $11\frac{9}{11}$; $23\frac{3}{5}$, $11\frac{9}{12}$, $12\frac{9}{11}$; $25\frac{3}{5}$, $12\frac{9}{12}$, $13\frac{9}{12}$; 28, 14, $15\frac{3}{11}$; $24\frac{3}{5}$, $12\frac{3}{12}$, $13\frac{4}{11}$.

4. $28\frac{1}{6}$, $21\frac{1}{6}$, $14\frac{7}{12}$; $32\frac{1}{6}$, $24\frac{1}{6}$, $16\frac{1}{12}$; $34\frac{1}{6}$, $25\frac{1}{6}$, $17\frac{1}{12}$; $42\frac{1}{6}$, $32\frac{1}{6}$, 30, 20.

 $5. 115\frac{1}{4}, 46\frac{1}{6}, 42; 170\frac{3}{4}, 68\frac{2}{16}, 62; 210, 84, 76\frac{1}{16}; 101\frac{1}{4}, 40\frac{1}{16}, 36\frac{1}{17}; 138\frac{3}{4}, 55\frac{1}{16}, 50\frac{1}{17}.$

6. 54_{11}° , 75, 50; 69_{11}° , 95_{8}° , 63_{12}° ; 76_{11}° , 105_{8}° , 70_{12}° ; 90_{11}° ,

 $124\frac{7}{8}$, $83\frac{3}{12}$; $65\frac{2}{11}$, $89\frac{5}{8}$, $59\frac{9}{12}$.

7. $134\frac{4}{5}$, $100\frac{1}{19}$, 110; 764, 573, $625\frac{1}{17}$; $784\frac{7}{5}$, $588\frac{7}{12}$, $642\frac{1}{17}$; $555\frac{1}{5}$, $416\frac{1}{18}$, $454\frac{1}{17}$.

8. $345, 230, 276; 1200\frac{4}{8}, 800\frac{4}{12}, 960\frac{4}{10}; 1033\frac{8}{8}, 688\frac{11}{12}, 826\frac{7}{10};$

8184, 5453, 6548.

9. $7187\frac{7}{12}$, $862\frac{7}{12}$, $12320\frac{9}{12}$; $6052\frac{1}{12}$, $7263\frac{9}{16}$, $10376\frac{3}{2}$; $712\frac{1}{12}$, 8549, $12212\frac{5}{2}$; $2941\frac{7}{12}$, $3529\frac{7}{16}$, $5042\frac{5}{2}$.

10. 6909_{11}^{3} , 9500_{8}^{2} , 6333_{12}^{4} ; 8182_{11}^{7} , 11251_{8}^{1} , 7500_{12}^{2} ;

4820₇₇, 66283, 441811.

11. 683837_{5}^{2} , 547069_{15}^{2} , 497336_{17}^{2} ; 11712585_{5}^{2} , 9370068_{16}^{2} . 8518243_{17}^{2} ; 257524_{5}^{2} , 206019_{16}^{2} , 187290_{17}^{2} .

12 1194292 $\frac{3}{4}$, 928894 $\frac{1}{3}$, 696670 $\frac{7}{12}$; 969949, 754404 $\frac{7}{3}$,

 565803_{12}^{7} ; 14128554, 10988876, 824165_{12}^{9} .

13. 66725 times. 19871. 14. (1) 9. (2) 1613. 15. 54 cents. 16. 7 plums. 17. 506. 18. 11946419. 19. Cook received \$561, man-servant \$1122, housekeeper \$2244 20. 1728. 21. 6. 22. 26 oranges. 23. 35 penknives.

Ex. XVIII. (p. 41.)

1. 12; 40; 53; 94. 2. 45; 29; 65; 97. 3. 57; 79; 88; 75. 215; 798; 885; 102. 5. 805; 682; 127; 357; 460; 7090. 6. 379; 407; 940; 738; 93845796; 580073. 7. 347; 569; 3094. 8. 1987; 7071; 650. 9. 9009; 5436; 388. 10. 21503 rem. 5; 3450; 124 rem. 477. 11. 57096; 76542; rem. 136; 4655 rem. 603. 12. 103944; 175971 rem. 66; 87039; 84003; 967427210 rem. 61. 13. 190182; 4623; 50301; 87366 rem. 6076. 14. 2007 rem. 1; 20300; 65839 rem. 2; 31352. 15. 902468; 1754 rem. 129; 14957000; 770071. 16. 27810; 3250460. 73086413. 37. 1799. 18. 180 pairs.

19. N. 20. 360 rem. 52. 21. \$3\frac{11}{275}. 22. \$3. 23. 1000. 74. 420. 25. 403. 26. 372547. 27. 17129. 28. \$10.

Ex. XIX. (p. 43.)

- 1. 3_{10}^{4} , 4_{10}^{3} , 5_{10}^{6} , 8, 13_{10}^{5} , 26, 150_{10}^{4} ; $1\frac{14}{20}$, $2\frac{3}{20}$, $2\frac{16}{20}$, 4, $6\frac{16}{20}$, $(3, 75\frac{4}{30}; 1\frac{4}{30}, 1\frac{13}{30}, 1\frac{26}{30}, 2\frac{20}{30}, 4\frac{15}{30}, 8\frac{20}{30}, 50\frac{4}{30})$
- 2. 537, 21, 1633, 743, 15048, 19548, 203048, 8195; 357, 14, $1\frac{1}{8}\frac{3}{6}$, $4\frac{5}{6}\frac{1}{6}$, $100\frac{1}{6}\frac{5}{6}$, $130\frac{2}{6}\frac{9}{6}$, $1353\frac{4}{6}\frac{9}{6}$, $5463\frac{2}{6}\frac{9}{6}$; $3\frac{2}{7}\frac{7}{6}$, 12, $9\frac{4}{7}\frac{3}{6}$, $4\frac{1}{7}\frac{1}{6}$, 35^{99}_{70} , 111^{99}_{70} , 1160^{99}_{70} , 4682^{50}_{70} ; 2^{37}_{100} , 8^{40}_{100} , 6^{73}_{100} , 2^{91}_{100} , 60^{19}_{100} 78_{100}^{20} , 812_{100}^{29} , 3278; $1_{\overline{200}}^{37}$. $4_{\overline{200}}^{40}$, $3_{\overline{200}}^{73}$, $1_{\overline{200}}^{91}$, $30_{\overline{200}}^{19}$, $39_{\overline{200}}^{20}$, $406_{\frac{29}{200}}$, 1639.
- 3. $329_{\overline{240}}^{88}$, $28_{\overline{240}}^{150}$, $3708_{\overline{240}}^{141}$; $79_{\overline{1000}}^{48}$, $6_{\overline{1000}}^{870}$, $890_{\overline{1000}}^{61}$; $52\frac{1948}{1500}$, $4\frac{870}{1500}$, $593\frac{551}{1500}$; $30\frac{1048}{2600}$, $2\frac{1670}{2600}$. $342\frac{861}{2600}$: $8306_{1000000000}^{78103490}$.
- **4.** $88976\frac{2}{5}\frac{2}{5}\frac{2}{5}$ **. 5.** $8678\frac{2}{5}\frac{4}{5}\frac{610}{2}$ **. 6.** $66970\frac{7}{1}\frac{1}{2}\frac{6}{5}$ **. 7.** $7096\frac{2}{5}\frac{2}{5}\frac{2}{5}\frac{3}{5}$ **8.** $9992461\frac{2}{5}\frac{2}{6}\frac{2}{5}$ **. 9.** $2144\frac{2}{5}\frac{2}{5}\frac{1}{2}\frac{2}{6}$ **.** 10. $1302\frac{2}{5}\frac{2}{6}\frac{7}{47}$ **.** 11. 1100, 916 and 800 men over. 12. 956, \$200.

Ex. XX. (p. 51.)

- 1. 681440 far. 1085070 inches. 3. 4167680 drs. 1. 681440 1ar. 2. 10e3010 linenes. 3. 4101000 drs. 4. 3842027640 sq in. 5. 8092505 ls. 6. 31518306 sq. in. 7. 24480 mins. 8. 16820 grs. 9. 15620 yds. 10. 1074088 c. in. 11. 440 gills. 12. 7040 qts. 13. 2930400 mins. 14. 158304 grs. 15. 276400 grs. 16. 96425 half-pence. 17. 1062864 sq. yds. 18. 3499 nls. 19. 2281906 far. 20. 21667 lbs. 21. 92160 secs. 22. 530784 in. 23. 300362 far. 24. 604800 grs. 25. 520 nls.
- 26. 888 nls. 27. 544345 far. 28. 52800 scs. 29. 378 galls 30. 192938 far.

Ex. XXI. (p. 53.)

- 2. 2 lbs. 3 cz. 8 dwt. 20 grs. 1. £128 8s. 6½d. 3. 2273 galls. 3 qts. 1 pt. 4. 403 lea. 2 mls. 7 fur. 16 po
- 5. 3 tons 18 cwt. 1 gr. 14 lbs. 14 oz. 6 586 ac. 1 ro. 27 po
- 7. 29 lbs. 1 oz. 12 dwt. 4 grs.
- 8. 11517 mls. 1 fur. 27 po. 2 yds. 11 in. 9 ls.
- 9. 14997 tons 8 ewt. 1 qr. 14 lbs. 10 oz. 12 drs.

- 9. 14997 tons 5 cwt. 1 qr. 14 lbs. 10 02. 12 drs.
 10. 1 ml. 7 fur. 14 po. 2 ft. 9 in 11. 17 lbs. 3 dwt. 14 grs.
 12. 3 tons 19 cwt. 1 lb. 6 oz. 13. 122 lbs. 3 drs. 17 grs.
 14. 2 wks. 5 dys. 23 hrs. 58′ 13″. 15. 15 ac. 2 ro. 20 po.
 16. 297 c. yds. 17. 198 ac. 1 ro. 15 po. 16½ yds.
 18. 31 yds. 1 qr. 19. 36° 24′ 35″. 20. 365 dys. 6 hrs.
 21. 508 hhds. 19 gals. 2 qts. 22. 596 hhds. 14 gals. 1 qt.
 23. 15211 bu. 55 lbs. 24. 29411 bu. 26 lbs. 25. 121 bu 3 lbs.
- 26. \$307.47. 27. £1014 4s. 3\(\frac{3}{2}\)d.

Ex. XXII. (p. 4.)

1. \$94.64. 2. £20. 12s. 3d. 3. 0 qrs., 24 lbs., 1 os.

4. 107 lbs., 1 oz., 10 dwt., 17 grs.

- 5. 55 lbs., 1 oz., 5 drs., 2 sc., I gr. 6. 817255.22. 7. 285 tons, 2 cwt., 2 qrs., 23 lbs.
- S. 578 vds., 2 grs. 9. 79 mls., 3 fur, 9 per., 3 yds. 10. £145. 178. 1½d. 11. 116 dys., Shrs., 35', 12". 12. \$8470.12
- 13. 42 ac., 2 ro., 25 po., 5 ft., 40 in.
- 14. 99 tons, 8 cwt., 3 grs., 12 lbs., 11 oz., 15 ars.
- 15. \$11040.

./8

Ex. XXIII. (p. 56.)

- 1. £15. 8s. 6d. 2. 9 lbs., 11 oz., 3 drs., 16 grs.
- 3. 2 lbs., 10 oz., 7 dwt. 4. 2 mls., 6 fur., 35 po., 1 yd.
- 5. 13 yds., 1 qr., 2 nls., 2 n. 6. 28 c. yds., 23 c. ft., 1443 in.
- 7. 1 ac., 2 ro., 38 po., 1 ya., 2 ft., 142 in.
 - 8. 5 dys., 9 hrs., 49 min., 57 sec. 9. £53. 17s. 103d.
- 10. 2 grs., 15 lbs., 11 oz., 14 drs. 11. \$1068.89.
- 12. 95 cords, 110 c. ft. 13. \$27.69.
- 14. 107 ac., 2 ro., 34 po., 29 yds., 7 ft., 118 in.
- 15. 79 c. vds., 21 c. ft., 1377 c. in.
- 16. 27 mls., 29 per., 1 ft., 10 in. 17. 6°, 39′, 39″.
- 18. 5 tons, 16 cwt., 2 qrs., 23 lbs., 11 oz., 1 dr.
- 19. 10 yds., 2 qrs., 2 nls., 2 in. 20. 70 bu., 2 pks., 1 gal., 2 qts.
- 21. 673 bu., 1 gal., 2 qts.

Er. MXIV. (p. 58)

- 1. £24. 19s. 2. 52 lbs., 5 oz., 4 drs.
- 3. 74 lbs., 1 oz., 1 dwt., 16 grs. 4. 139 yds., 2 qrs., 3 nls.
- 5. 167 mls., 6 fur., 1 per., ½ yd. 6. \$1660.33.
- 7. 129 cwt., 1 qr., 11 lbs., 7 oz., 8 drs.
- 8. 58 mls., 5 fur., 18 po., 1 yd., 9 in. 9. \$6099.30.
- 10. 86 wks., S hrs., 56 min. 11. 95 ac., 36 per., 3 ft. 12. £146. 3s. 61d. 13. 899 lbs., 8 oz., 4 drs.
- 14. 23 bu., 1 pk., 3 qts. 15. 21 dys., 15 krs., 50 min.
- 16. 50103 gals., 2 qts., 1 pt.
- £312. 153. 014 17. 4382 dys., 21 hrs., 47 min., 24 sec. 18.
- 19. 134 ac., 3 ro., 31 po. 20. \$3572.16.
- 21. 25043 bu., 2 pks., 1 gal. 22. £840. 11s. 6d.
- 23. 219 lbs., 8 oz., 10 dwt., 12 grs. 24. \$7342.
- 25. £159. 158. 6\(\frac{2}{4}\)d. 26. \(\frac{2}{2}2503\). 27. 381 mis., 12 po., 2 yds.

Ex. XXV. (p. 59.)

1. 1583 ac., 2 ro., 12 po. 2. 1500 mls., 6 po. 3. £2817. 128. 5. £351. 13s. 9d 4, 1621 lbs., 4 oz., 15 dwt., 13 grs.

- 6. 1484 yds., 2 qrs., 2 nls. 7. 188 cwt., 22 lbs., 11 oz., 10 drs. 8. £5912. 4s. 9\(\frac{3}{4}d\). 9. \$7321.30.
- 10. 1493 c. yds., 11 c. ft., 1332 in.
- 11. 182 lbs., 10 oz., 1 dwt., 13 grs. 12. £3743. 7s. 10d.
- 13. 688 dys., 6 hrs., 40 min. 14. 6297 lbs., 11 oz., 4 drs.
- 15. 33272 lbs., 1 oz., 18 dwt., 6 grs. 16. £3676, 13s, 10½d. 17 1319 ac., 0 ro., 0 po., 13 yds., 4 ft., 48 in.
- 18. 1034 mls., 2 fur., 4 po., 3 in. 19. £2100. 18s. 9d. 20. \$118575. 21. 8500 bushels.

Ex. XXVI. (p. 61.)

- 1. 352 cwt., 2 qrs., 21 lbs., 13 oz.
- 2. 33772 lbs., 10 oz., 18 dwt., 15 grs. 3. £2194. 10s. 7d.
- 4. 1870 cwt., 3 qrs., 23 lbs., 4 oz., 5 drs. 5. £2771. 2s. 11d.
- 6. 10826 lbs., S oz., 5 drs., 2 sc., 4 grs. 7. \$470.25. 9. \$97.50. 10. 12 cwt., 1 qr., 7 lbs., 8 oz. 8. \$66.04.
- 11. \$40000.

Ex. XXVII. (p. 63.)

- 1. £55, 158, 18d. 2. 29 lbs., 8 oz., 3 dwt., 6 grs
- 3. 24 mls. 1 fur., 19 po., 3 yds., 10 in. 4. 23 yds., 2 nls.
- 5. 144 lbs., 3 oz., 4 drs., 8 ½ grs. 6. £188. 19s. 94d.
- 7. 2 tons, 10 cwt., 12 lbs., 10 oz., 103 drs.
- 8. 17 ac., 1 ro., 30 po., 10 yds., 6 ft., 5513 in.
- 9. 3 qrs., 11 lbs., 13 oz., 5199 drs.
- 10. 6 mls., 7 fur., 14 po., 3, 217 in.
- 11. 6 bu., 1 pk., 1 gal., 44 pt. 12, £52, 16s, 22d.
- 13. 4 lbs., 4 oz., 1 dr., 1 scr., 1157 grs.
- 14. 7 fur., 23 po., 5 yds., 1 in., 1 35 ls.
- 15. 1 ac., 1 ro., 9 po., 22 yds., 5 ft., 14192 in.
- 16. 1 ton, 1 cwt., 3 qrs., 2 lbs., 12 oz., 10561 drs.
- 17. 5 c. yds., 11 c. ft., 961123 c. in.
- 18. 4 lbs., 4 oz., 3 drs., 1 sc., 11 12 5 grs.
- 19. 4 lbs. 10 oz., 1 dwt., 9330 grs. 20, £2, 10s, 61 37d,
- 21. 13s. 7\d. 22. 115 dys., 5 hrs., 54 min., 22534 sec.
- 23. \$8 $49\frac{101}{267}$. 34. \$13.39 $\frac{305}{25}$. 25. \$1.641 28. \$1.91 11.
- 26. \$4.65. 27. \$1.15. 28. \$2.53\$4.

Ex. XXVIII. (p. 64.)

- 1. 9 times. 2. 3 times. 3. 436 times. 4. 3 times 5. 25 1 5 1 times. 6. Sig times. 7. 9 times. 8. 24 times.
 - 9. 75 times. 10. 65 times. 11. 100 times.

Ex. XXIX. (p. 65.)

1. \$101.25, **2.** \$231.85. 3. \$831.53\frac{1}{2}. 4. \$615.681

 5. \$871.40.
 6. \$1279.12\frac{1}{2}.
 7. \$2451.98\frac{3}{2}.
 8. \$253.96\frac{1}{2}.

 9. \$3650.50.
 10. \$2845.09\frac{1}{2}.
 11. \$4468.12\frac{1}{2}.
 12. \$189.55.

 13. \$8069.33\frac{1}{2}.
 14. \$301.94\frac{1}{2}.
 15. \$151.72\frac{1}{2}.
 16. \$350.75.

Ex. XXX. (p. 66.)

1. £54. 6s. 3d. 2. £81. 17s, 9d. 3. £4. 6s. 9d. 4. £21. 2s. 6d. 5. £18. 19s. 9d. 6. £31. 6s. 10½d. 7. £216. 19s. 41d. 9. £348. 8s. 13d. £290, 12s. 10. £484. 6s. 11. £555. 1s. 5\(\frac{2}{5}\)d. 12. £946. 78. 44d

Ex. XXXI. (p. 66.)

PAPER I.

 1. 117984.
 2. 107766.
 3. 3653012.
 5. 2 mls., 6 fur., 15 per., 5 yds., 1 ft., 10 in.
 6. 1st, \$5.60, \$17.17; 2nd, \$11.57. 4. 1898307

PAPER II.

1. £362. 19s. 9d. 2. \$63.47. 3. 183 ac., 1 ro., 24 per., 26 yds., 7\frac{155}{397} ft.

4. \$9.48 ... 5. 5 dresses, £2. 15s. 7\d. each. 6. \$3227.42

PAPER III.

£46. 14s. 6d.
 \$7000, \$21000, \$35000.
 £13. 12s. 9d

4. 1 ro., 18 po., 5 yds., 2 ft., and 16½ ft. over. 5. 17 cwt., 1 qr., 8 lbs., 10 oz., 5 drs., and 89 drs. over.

6. 6 hours, 54 min.

PAPER IV.

1. \$148.15. 2. 11, 18. 3. 9, 18, 27. 4. owner of net, 8 dozen; owner of boat, 16 dozen; each man, 32 dozen 2301696 pores.
 42000, 42889.

PAPER V.

1. 6255647664981. 2. 861447920. 3. 11904. 4. 12752.

5. 465335. **6.** 95587.

PAPER VI.

1. 657872. 2. \$16496471. 3. \$10444830.63. 4. 6228\$ lbs 5. 136 ac., 3 ro., 14 po., $24\frac{375}{1270}$ yds. 6. 634338.

Ex. XXXII. (p. 71.)

1. 2. 2. 3. 3. 2. 4. 4. 5. 4. 6. 3. 7. 2. 8. 6. 9. 4. 10. 2. 11. 58. 12. 63. 13. 2. 14. 30. 15. 10. 16. 8. 17. none. 18. 8. 19. 26. 20. 352. 21. 131. 22. none. 23. 7056. 24. 11. 25. 17. 26. 31.

Ex. XXXIII. (p. 72.)

 1. 20
 2. 72.
 3. 144.
 4. 1260.
 5. 240.
 6. 168.
 7. 525.

 8. 1056.
 9. 1050.
 10. 2520.
 11. 11088.
 12. 450.
 13. 1080

 14. 840.
 15. 840.
 16. 16380.
 17. 1386.
 18. 21000.

 19. 43890.
 20. 95040.

Ex. XXXIV. (p. 74.)

(1)
$$\frac{4}{7}$$
, $\frac{6}{7}$, $\frac{10}{7}$, $\frac{14}{7}$, $\frac{18}{7}$, $\frac{24}{7}$; $\frac{34}{19}$, $\frac{51}{19}$, $\frac{85}{19}$, $\frac{119}{19}$, $\frac{153}{19}$, $\frac{204}{19}$.

Ex. XXXV. (p. 75.)

(1)
$$\frac{8}{8}$$
, $\frac{3}{12}$, $\frac{3}{20}$, $\frac{3}{24}$, $\frac{3}{36}$, $\frac{3}{48}$; $\frac{7}{18}$, $\frac{7}{27}$, $\frac{7}{45}$, $\frac{7}{54}$, $\frac{7}{81}$, $\frac{7}{108}$.

Ex. XXXVI. (p. 75.)

(1)
$$\frac{6}{2}$$
, $\frac{27}{9}$, $\frac{39}{13}$; $\frac{10}{2}$, $\frac{45}{9}$, $\frac{65}{13}$; $\frac{16}{2}$, $\frac{72}{9}$, $\frac{104}{13}$
 $\frac{30}{2}$, $\frac{135}{9}$, $\frac{195}{13}$.

(2)
$$\frac{72}{8}$$
, $\frac{90}{10}$, $\frac{514}{57}$; $\frac{96}{8}$, $\frac{120}{10}$, $\frac{684}{57}$; $\frac{136}{8}$, $\frac{170}{10}$, $\frac{969}{57}$; $\frac{296}{8}$, $\frac{370}{10}$, $\frac{2109}{57}$

Ex. XXXVII. (p. 76.)

1. 3. 2. $2\frac{1}{2}$, 3. $4\frac{1}{3}$, 4. 4. 5. $3\frac{1}{6}$, 6. $6\frac{1}{7}$, 7. $5\frac{1}{8}$, 8. $6\frac{1}{7}$, 9. 7. 10. 8. 11. $8\frac{1}{4}\frac{1}{7}$, 12. $18\frac{3}{4}\frac{1}{7}$, 13. $9\frac{1}{107}$, 14. $102\frac{1}{7}\frac{1}{6}$, 15. $12\frac{1}{7}\frac{1}{7}\frac{1}{7}$.

Ex. XXXVIII. (p. 76.)

1.
$$\frac{4}{3}$$
. 2. $\frac{25}{12}$. 3. $\frac{16}{15}$. 4. $\frac{88}{8}$. 5. $\frac{89}{5}$. 6. $\frac{3874}{19}$

7. $\frac{141}{65}$. 8. $\frac{239}{8}$. 9. $\frac{88716}{126}$. 10. $\frac{360931}{401}$. 11. $\frac{3407}{680}$

42. $\frac{3376}{63}$. 13. $\frac{26253}{1250}$. 14. $\frac{69057}{465}$. 15. $\frac{29160}{2160}$.

16. $\frac{60389}{2400}$. 17. $\frac{608543}{3084}$.

Ex. XXXIX. (p. 77.)

1. $\frac{3}{5}$. 2. $\frac{2}{3}$. 3. $\frac{9}{19}$. 4. $\frac{12}{55}$. 5. $\frac{35}{16}$. 6. $\frac{5}{6}$. 7. $\frac{5945}{6}$.

8. $\frac{3363}{35}$. 9. $\frac{35}{2}$. 10. $\frac{15}{2}$. 11. $\frac{1}{36}$. 12. $\frac{1}{11}$. 13. $\frac{375}{44}$.

14. $\frac{175}{8}$. 15. $\frac{14}{15}$. 16. $\frac{6399}{22}$.

1. $\frac{1}{2}$. 2. $\frac{2}{3}$. 3. $\frac{2}{3}$. 4. $\frac{5}{8}$. 5. $\frac{4}{9}$. 6. $\frac{16}{21}$. 7. $\frac{7}{11}$.

8. $\frac{3}{17}$. 9. $\frac{7}{13}$ 10. $\frac{11}{13}$. 11. $\frac{7}{8}$. 12. $\frac{13}{20}$. 13. $\frac{31}{84}$.

14. $\frac{3}{4}$. 15. $\frac{35}{114}$. 16. $\frac{8}{9}$. 17. $\frac{191}{279}$. 18. $\frac{827}{7337}$.

19. $\frac{235}{397}$. 20. $\frac{103}{136}$. 21. $\frac{2}{7}$. 22. $\frac{945}{1529}$. 23. $\frac{20}{21}$.

24. $\frac{23}{33}$.

Ex. XLI. (p. 79.)

9. $\frac{10}{12}$. 2. $\frac{9}{12}$. 8. $\frac{8}{12}$. 2. $\frac{6}{8}$. 7. $\frac{427}{67}$. $\frac{35}{63}$. 5. $\frac{33}{48}$. 4. $\frac{42}{33}$. 3. $\frac{110}{120}$. 18. $\frac{827}{7337}$. 19. $\frac{9}{10}$. 10. 11. 18. 38. 2. $\frac{8}{8}$. 2. $\frac{6}{8}$. 7. $\frac{7}{8}$. 4. $\frac{27}{67}$. $\frac{35}{63}$. 5. $\frac{33}{48}$. 4. $\frac{42}{33}$. 5. $\frac{9}{12}$. 10. $\frac{11}{120}$. 10. $\frac{11}{130}$. 11. $\frac{9}{12}$. 12. $\frac{11}{120}$. 13. $\frac{110}{120}$. 14. $\frac{11}{120}$. 15. $\frac{110}{120}$. 16. $\frac{11}{120}$. 17. $\frac{110}{120}$. 18. $\frac{110}{120}$. 19. $\frac{110}{120}$. 19. $\frac{110}{1200}$. 19. $\frac{110}{120$

cake. 14. (1) $\frac{8}{9}$. (2) 5_{10}^{7} . 15. $\frac{5}{72}d$.

Ex. XLV. (p. 84.)

1. $12\frac{1}{21}\frac{1}{6}$. 2. $\frac{1}{6}$. 3. $20\frac{9}{17}$. 4. $36\frac{2}{4}\frac{3}{6}$. 5. 1. 6. $1\frac{1}{2}\frac{9}{2}$. 7. $3\frac{1}{2}\frac{5}{6}$.

8. B, C, D, and A had respectively $\frac{1}{4}$, $\frac{1}{6}$, $\frac{1}{9}$, and $\frac{2}{9}$ of cheese.

Ex. XLVI. (p. 86.)

1.
$$\frac{1}{12}$$
. 2. $\frac{35}{72}$. 3. $\frac{5}{26}$. 4. $\frac{7}{12}$ 5. 25 6. 28. 7. $\frac{13}{40}$

8. 10. 9. $4\frac{5}{7}$. 10. $329\frac{1}{16}$. 11. $4\frac{5}{7}$. 12. $0\frac{11}{16}$. 13. $\frac{17}{32}$.

14. 5 3 6. 15. 7 2.

Ex. XLVII. (p. 86.)

1.
$$1\frac{1}{20}$$
. 2. $\frac{2}{3}$ 3. $\frac{10}{11}$. 4. $\frac{116}{165}$. 5. 9\frac{2}{3}. 6. $1\frac{11}{4}$. 7. $\frac{2}{3}$.

8.
$$1\frac{1}{9}$$
 9. $3\frac{1}{8}$ 10. $\frac{27}{88}$ 11. $\frac{1}{32}$ 12. $\frac{3}{8}$ 13. $\frac{13}{15}$

Ex. XLVIII. (p. 87.)

1.
$$1\frac{1}{1}\frac{3}{1}$$
 2. 24. 3. $\frac{3}{8}$ 4. $1\frac{3}{4}$ 5. $1\frac{1}{2}\frac{5}{1}$ 6. $\frac{28}{725}$ 7. $2\frac{1}{2}$

8.
$$\frac{76}{153}$$
. 9. $12\frac{11}{18}$. 10. $1\frac{3.97}{24.68}$. 11. $\frac{8}{9}$. 12. $\frac{810}{102949}$.

13. $\frac{25}{144}$. 14. $3\frac{1166}{168}$.

Ex. XLIX. (p. 88.)

1. 40 cents. 2 3 fur. 3. 1 qr., 17 lbs., 13 cz., 11\$ drs.
4. 19 cwt., 1 qr., 10 lbs. 5. 4 fur., 35 per. 6. 2 sc., 1 ro.,
25 per., 20 yds., 4 ft., 136\$ in. 7. 4 lbs., 2 oz., 10 dwt. 20 grs.
5. 59 yds., 2 qrs., 1\$ nls. 9. £7. 4s. 3d. 10. 109 lbs., 8 oz.,
5 drs. 8\$ grs. 11. 5 hrs., 36 min. 12. 7 lbs., 9 oz., 9\$ drs.
13. \$24. 14. 7 hrs. 12 min. 15. 13 cords, 64 c. ft.

1.
$$\frac{1}{6}$$
. **2.** $\frac{31}{160}$. **3.** $\frac{15128}{15}$. **4.** $\frac{263}{480}$. **5.** $\frac{408}{577}$. **6.** $\frac{175}{44}$

7.
$$\frac{1}{45}$$
. 8. $\frac{19}{70}$. 9. $\frac{6}{11}$. 10. $\frac{1}{27}$. 11. $\frac{1}{28}$. 12. $\frac{144}{175}$. 13. $\frac{3}{224}$. 14. $\frac{3}{14960}$. 15. $\frac{325}{7850601}$. Ex. Lf. (p. 89.) 1. $\frac{1}{2}$. 2. $\frac{1080}{241}$. 3. $\frac{5445}{5762}$. 4. $\frac{357}{160}$. 5. $\frac{3}{4}$. 6. $\frac{56}{3}$. 7. $\frac{18}{35}$. 8. $\frac{21}{2}$. 9. $\frac{27}{14}$. 10. $\frac{156}{5}$. 11. $\frac{21625}{432}$. 12. $\frac{8}{7}$. 13. $\frac{351}{224}$. 14. $\frac{115}{96}$.

Ex. LIL (p. 92.)

1. A will have $\frac{1}{15}$ of the farm, B $\frac{1}{15}$ of farm, and $C\frac{3}{5}$ of farm. 2. (1) 24 boys; (2) $7\frac{1}{5}$. 3. $\frac{3}{10}$ and $\frac{1}{50}$. 4. (1) $1\frac{1}{8}$; (2) $2\frac{1}{3}$. 5. A has twice as much as D. 6. \$25.20. 7. \$110. 8. \$900. 9. \$36. 10. £70. 11. $385\frac{5}{10}$ rounds. 12. \$33.60. 13. $13\frac{1}{10}$ days. 14. (1) A has \$56.70, B has \$37.80; (2) A has \$63, B has \$31.50. 15. \$ $\frac{1}{3}$, \$255. $10\frac{1}{3}$, 16. $\frac{3}{5}$. 17. 250 boys 18. $5\frac{1}{10}$, days. 19. Elder son received \$3250, younger son \$1560, and widow \$1440. 20. A has 24 ac., 3 ro.; B has 13 ac., 2 ro.; and C has 47 ac., 1 ro. 21. 48 boys. 22. 42 min. 23. (1) $52\frac{1}{2}$ days; (2) $\frac{1}{2}$. 24. $15\frac{1}{3}$ days. 25. 1st cask contains 140 gals.; 2d, 60 gals.; 3d, 45 gals.; 4th, 80 gals. 26. 20 days.

1. '4; 2·3; 23·5; '04; '147; '047. **2.** 500·1; 9·51; '00951: 5·02; '005002. **3.** 35·6; 17·60701: '0056005 · '0000002

20.76854; 00000053052. **4.** ·7; ·030. **5.** 300·003; ·0002. **6.** 4·000504; ·0000070.

- 7. Six tenths; seventeen hundredths; seven hundredths.
- 8. Seven thousandths; seven hundred thousandths, or seven tenths; six and three thousand and four ten thousandths.
- 9. Thirty-five and two hundred and five hundred thousandths; four hundred and thirty-four thousand one hundred thousandths, or four hundred and thirty-four hundredths

Ex. LV. (p. 97.)

1. 560·34603. 4. 345·608037. 5. 40·23111. 6. 585·07805. 7. 7332·0773. 8. 93·69602912. 9. 1393·7111.

Ex. LVI. (p. 98.)

1. $2 \cdot 258$. 2. $7 \cdot 0456$. 3. $5 \cdot 9697$. 4. $1 \cdot 0991$. 5. (1) 1 \(^17\); $204 \cdot 93$. (2) $68 \cdot 67$; 2803. (3) $72 \cdot 09544$; $5270 \cdot 76$. (4) $4 \cdot 41958$; 0069993. 6. $20 \cdot 93$. 7. 095; $19 \cdot 98$. 8. 613 of it left. 9. $\frac{1}{2} \frac{2}{6} \frac{7}{3}$. 10. (1) $79 \cdot 8665$. (2) $82 \cdot 9319$.

Ex. LVII. (p. 98.)

1. 1·1375. 2. 16·2945. 3. 81·20812. 4. 8·333715. 5. 4246·48449. 6. 667·81: 114·364272; 3752; 356·40164745. 7. ·01778479; 488·745015255; ·000642. 8. (1) ·9150625. i2) ·3689. 9. 278·1975 yds. 10. 346½ loaves.

Ex. LVIII. (p. 100.)

1. 12:36. 2. 1:236. 3. :01236. 4. 123600. 5. 123600000. 6. 1737:1. 7. 17371000. 8. 17371. 9. 173710000. 10. 170:01; 170010. 11. :00521; 521. 12. :00003; 03; 000000003. 13. $108971 \cdot 3$; $1\cdot 08971$ 6. 14. :011; -:00011; 110. 15. 2040×00 ; 204; :00204. 16. 18030; :001803. 17. $213\cdot2$; :002132. 18. :0101. 19. :0008. 20. 12½ days. 21. $85\cdot5$ times. 22. :03054.

Ex. LIX. (p. 101.)

1. 6333; 63:333; 006. 2. 031; 3:105; 003. 3. 6221:584; 62215849:056; 62:215.

Ex. LX. (p. 102.)

1. '25; '6; 1·5; 6·2; 7·8; '625; 5·3. 2. '1875; 8·9375; '95; '96875; 7·925. 3. '94; 4·056; '006; ·1584; 84·0029296875. **4.** '5078125; 8·75; 76·234375. 5. 3·9125; 16·36.

Ex. LXI. (p. 104.)

49 $\frac{1}{15}$; 20 $\frac{7}{15}$; 6. 6 $\frac{4223}{5}$; 15 $\frac{7}{15}$; 7. 96·523114. 8. 37·443543 9. 1·817686. 10. 44·34309. 11. 40·8; ·258722.....; **60**185. 12. 2·5416; ·136; ·0743; 30·833953.

Ex. LXII. (p. 105.)

1. 75 cents. 2. \$4.37\frac{1}{2}\$ cts. 3. 62\frac{1}{2}\$ cts. 4. 2 qr., 12 lbs., 8 oz. 6. 3 fur. 6. 3 cwt., 2 qr. 7. £1. 3s. 5\frac{1}{4}d. 8. 5\frac{1}{2}d., 5 q. 9. 3 lbs., 2 oz., 2 dwt. 10. 20 ac., 3 ro., 28 po. 11. 6 ac., 1 ro., 4 po. 12. £1. 8s. 13. 17 wks., 6 days, 5 hrs., 15 min. 14. 16 dys., 12 hrs., 5 min., 45 6 sec. 15. 15 lbs., 3 oz., 2 drs., 2 grs. 16. £12. 3s. 8\frac{1}{4}d. 048q. 17. 12 ac., 2 ro., 4 po., 20 yds., 7 ft., 122-76 in. 18. 80 lbs., 6 oz., 13-23 grs. 19. 66\frac{2}{3}\$ cents. 20. 9 shillings. 21. 4 cwt., 3 qr. 11 lb., 10 oz., 10\frac{2}{3}\$ dr. 22. £34. 3s. 4d. 23. 5 lbs., 11 oz., 10 dwt., 24. 6 c. yds., 6 c. ft. 25. 18 ac., 2\frac{1}{3}\$ ro. 26. £2166. 10s. 27. £5. 34. 3\frac{2}{3}d. 28. 3 ro., 11 po., 9 yds., 1 ft., 72 in. 29. 14. 5\frac{5}{3}4d.

Ex. LXIII. (p. 106.)

1. '3. 2. '25. 3. '14583. 4. '81875. 5. '5416. **6.** '00022095. **7.** '22083 8. 48 '083 3. '2785493827160. **10.** '82285714. **11.** '5375. 12. '87916. "3. 4.90. 14. '15972.

Ex. LXIV. (p. 107.)

PAPER 1.

2. Seventy thousand three hundred and forty, one hundred and twenty-five millions four thousand three hundred and twenty one; five trillions six hundred and seven billions six hundred and thirteen thousand four hundred and three.

3. (1) 54502043294; (2) 99276. **4.** (1) 1529981369865;

(2) 38753981374. 5. 1372669823. 6. 777348.

PAPER II.

1. 3024. 3. \$0 pints. 4. 56 feet; 17 times. 5. (1) 239\(\frac{1}{2}\), \$22540000 (3) \$91870.42 and \$8.06 over.

PAPER III.

1. (1) 2_{151}^{163} , (2) 2_{153}^{63} . 2. \$5000. 3. (1) 3_{11}^{7} ; (2) 3_{151}^{161} . 4. £24. 15s. 6. 58 yards 6. $\frac{1}{8}$ of the orange.

PAPER IV.

1. 60.
 2. 84:675 or 84½.
 3. 01236.
 4. \$416.27½.
 5. 21 on smaller side, 24 on larger side, and 72 lookers on.
 6. One side scores seven times as many hans as the other, and therefore that side wins.

PAPER V.

1. 12s. 6d. 2. 275s. 3. 42₁4. 4. \$19.90. 5. \$5.92-6. \$48.27\frac{1}{2}.

Ex. LXV. (p. 112.)

1. 27. 2. 63. 3. 15. 4. 3. 5. 12.64. 6. 15. 7. 3. 8. 36. 9. 3. 10. 3.2.

Ex. LXVI. (p. 115.)

1. \$48. 2. \$18.15, 3. \$17.33\frac{1}{3}\$. 4. 38 bus., $21\frac{7}{1}$ lbs. 5. 20 bus., $28\frac{1}{7}$ lbs. 6. £82. 2s. 8d. 7. 28 cwt., 3 qr., 14 lbs. 12 oz. 8. 44 cents. 9. 29 cents. 10. \$8126 \cdot 01\frac{9}{1}\$. 11. 21 cwt., 3 qr., 18 lbs., 12 oz. 12. \$1638 \cdot 40\frac{53}{158} \cdot 8. 13. 61\frac{1}{4}\$. 14. 2 mo. 15. 15s. $9\frac{3}{4}d$. 16. £2675. 8s. 17. 3420 steps. 18. £4754. 10s. $10\frac{1}{2}d$. 19. \$560\frac{7}{5}\$. 20. 20 min. 21. 26 yds. 2 ft. 22. 528 pairs. 23. 171 men. 24. 3\frac{1}{4}\$ cts. \$57.812\frac{1}{2}\$. 25. \$4.12\frac{1}{4}\$. 26. 135 men. 27. 11 hrs., 38 mt 28. \$2234.31. 29. 7\frac{1}{4}d\$. 30. 12 days. 31. 5s. 6d. 32. \$151.14\frac{1}{13}\frac{3}{3}\$ 33. £900. 34. (1) £1000; (2) £960. 35. £8. 14s. $11\frac{1}{4}d$. $\frac{4}{3}\frac{4}{3}\frac{1}{4}q$. 36. 30 days. 37. \$1902.56\frac{1}{3}\frac{8}{3}\$. 38. 6d. 39. £90. 40. 104 lbs., 2\frac{9}{3}\$ oz. 41. 11 hr., 53\frac{3}{3}\frac{1}{4}\$. £4005. 46. £132.0s. 4\frac{4}{2}d.\frac{1}{4}q. 47. 21 days. 48. $10\frac{1}{2}\hrac{1}{2}\frac{1}{2}\$

Ex. LXVII. (p. 121.)

1. 8 wks. 2. 112 men. 3. 64 days. 4. \$307.44. 5. \$87500. 6. 174 miles. 7. \$202.50. 8. 200 horses. 9. 100 months. 10. 2808 qrs. 11. 39 ac., 1 ro. 20 po. 12. 9 mo. 13. 60 men. (cwt. = 112 lbs.) 14. 91 men. 15. 2½ days. 16. 45 men. 17. 178 qrs., 4 bus. 18. \$1.608. 19. \$7.20. 20. 4 days. 21. 2 days. 22. 13½ days. 23. 3 lba, 11 oz., 7½ drs. 24. 25 korses. 25. 180 men. 26. 2½ ft.

Ex. LXVIII. (p. 124.)

 1. \$168.75.
 2. \$157.50.
 3. \$1592.50.
 4. \$1927.20.

 5. \$3493.75.
 6. \$2396.25.
 7. £416. 17s.
 8. £600.

 9. \$4965.
 10. £6360. 5s.
 11. £812. 17s. 2½d.

 12. £1722. 6s. 2d.
 13. £86663. 1s. 9d.
 14. £155668. 10s. 11½d.

 15. \$267911.87½.
 16. \$715024.80.
 17. \$72562.35.

 18. \$9611.25.
 19. £2764. 11s. 3d.
 20. £14. 1s. 9½d.

Ex. LXIX. (p. 126.)

Ex. LXX. (p. 128.)

1. \$17.38, \$234.63. 2. \$34.76, \$252.01. 3. \$110.74875, \$638.12375. 4. \$11.22, \$104.72. 5. \$13.25625, \$89.00625. 6. £17. 12s. $5\frac{1}{2}d$. +, £80. 11s. 3d. 7. \$365.755, \$1441.505. 8. \$310.08, \$994.08. 9. £111. 14s. $7\frac{1}{7}s$. d. £7611. 14s. $7\frac{1}{7}s$. d. £111. 9s. 9.94...d. 11. 6 years 12. 8 $\frac{1}{2}$. 13. £130. 14. £32; 5 d., 3 c., 0.078125 m. 15. 4.

Ex. LXXI. (p. 130.)

1. \$115.92, \$915.92. 2. \$192.70, \$934.70. 3. \$341.88, \$901.88. 4. \$28.78, \$336.78. 5. \$103.61, \$713.61. \$ \$229.25, \$1229.25. 7. (1) £1. 1s. $6\frac{1}{2}d$. 88q., (2) £6. 19s. $2\frac{3}{2}d$. 136q.

Ex. LXXII. (p. 133.)

1. \$200. 2. \$800. 3. \$1200. 4. \$209.53 + . 5. \$900. 5. £129. 6s. 9d. 7. £179. 12s. $10\frac{3}{2}d$. $\frac{7}{2}\frac{3}{5}q$. 8. £456. 9s. $11\frac{3}{2}d$. $\frac{7}{2}\frac{3}{5}\frac{3}{4}q$. 9. \$42. 10. \$2100. 11. \$95. $23\frac{1}{2}\frac{7}{4}$. 12. \$99.05\frac{3}{2}\frac{3}{2}\frac{7}{4}. 15. $47\frac{3}{6}7\frac{5}{2}\frac{7}{4}7d$. 16. 5 per cent.

Ex. LXXIII. (p. 137.)

1. \$416.79 + . 2. \$780.48 $\frac{2}{1}$; 3. \$1524.88. 4. \$37.15 $\frac{2}{9}$; \$15069. 6. \$1391. 7. (1) £10. 16s. 4d.; (2) £3. 4s. $11\frac{2}{3}\frac{7}{3}$, d. 6. \$6 per ct. per aun. nearly. 9. Bank of Toronto. 10. £25. 11. His income less by £64. 12s. 12. \$139 $\frac{2}{3}$, 13. £240000 stock. 14. Loss of income £45. 10s. 15. £52. 10s. 16. Increase of income £135. 5s. $11\frac{2}{3}d$. $\frac{2}{3}\frac{2}{3}q$.

Ex. LXXIV. (p. 141.)

1. \$5.37\frac{1}{2}. 2. \$250 \cdot 2903. 3. 29\frac{1}{2}\$ cents. 4. \$1900. 5. (1) £6. 5s.; (2) £18. 17s. 4\frac{1}{4}. \frac{1}{4}q. 6. (1) \$208; (2) \$13. \frac{1}{3}.

(3) \$1.55. 7. (1) 10 per cent.; (2) £9. 1s. $9\frac{3}{2}d$. $\frac{1}{12}\frac{1}{2}$; 6. \$1.20 9. $66\frac{3}{3}$. 10.'5s. 3d. 11. $\frac{4}{3}s$. $1\frac{3}{2}d$. $\frac{1}{3}q$. 12. $49\frac{1}{2}\frac{4}{3}$. 13. 7s. $11\frac{1}{4}d$. $\frac{4}{3}\frac{1}{4}q$. 14. 18s. 4d. 15. £63. 12s. $8\frac{1}{2}d$. $\frac{1}{3}q$. 16. \$1.20.

Ex. LXXV. (p. 142.)

1. 90.83. 2. \$5.58. 3. 83.67. 4. 8.667...yrs. 5. 601 yrs. 8. 29046.813. 7. £191. 8s.

Er. LXXVI (p. 145.)

1. (1) 224, 336, 448; (2) \$40.62\frac{1}{2}, \$89.37\frac{1}{2}, \$130; (3) 66 ac., 1 ro., 15 po., 79 ac., 2 ro., 18 po.; (4) £42. 17s. $1\frac{1}{2}d$. \$q., £28. 11s. $5\frac{1}{2}d$. \$q., £28. 11s. $5\frac{1}{2}d$. \$q., £28. 11s. $5\frac{1}{2}d$. \$q. £28. 10s. 2. (1) \$A\$ is \$40.00 \text{ have \$\frac{1}{2}\$136. 18s. of oxygen, 969·136 lbs. of carbon, 176·4896 lbs. of hydrogen, (cwt. = 112 lbs.). 4. 33\frac{1}{2}\$ per cent. silver. 5. 5 mo. 6. 8 mo. 7. \$A\$ ought to have \$\frac{1}{2}\$6400. \$B\$ \$\frac{1}{2}\$840, \$C\$ \$\frac{1}{2}\$720. 8. \$A\$ ought to have received £700, and \$B\$ \$\frac{1}{2}\$900. 9. \$A\$ should pay \$\frac{1}{2}\$36, \$B\$ \$\frac{1}{2}\$18, and \$C\$ \$\frac{1}{2}\$6. 10. 24 men.

Ex. LXXVII. (p. 149.)

 1. 14; 17; 25.
 2. 29; 30; 42.
 3. 49; 87; 98

 4. 111; 200; 623.
 5. 703; 763; 509.
 6. 1111; 5343.

 7. 7906; 5746; 7008.
 8. 13509; 6-9.
 9. 9094; 21·103.

 10. 025173; 00003.
 11. 7·1414; 7141.
 12. 2·2583; ·2258.

 13. 28·3/92; 310·3304.
 14. 577.
 15. ¹166.
 16. 2·175.

 17. ‡3. 18. 2·625.
 19. 5408.

Ex. LXXVIII. (p. 152.)

1. 12; 20; 18. 2. 42; 75; 92. 3. 97; 103. 4. 512; 4·01. 5. 76·3; ·0587. 6. 5·079; 7420. 7. 2. 8. ·643. 9. 1·560. 10. 1. 11, ·464. 12. ·215. 13. 2·154. 14. ·333.

Ex. LXXIX. (p. 152.)

PAPER I.

1. 2 rem. 117257. 2. (1) 15 tons, 8 cwt., 3 qrs., 17 lbs., 1 os (cwt. = 112 lbs.) (2) 1 oz. Avcird. = $\frac{1}{15}\frac{5}{2}$ of 1 oz. Troy 3. £31. 7 ft. 6 c. 8·2142857 lm. 4. 1; 2520. 5. (1) 63 (2) $\frac{5}{2}$. (3) 3 cwt., 3 qrs., 3 lbs. (cwt. = $\frac{1}{15}\frac{5}{2}$ lbs.) 6. (1) 21060 (2; 0000)2166.

PAPER II.

1. (1) \$90. (2) £281. 7s. 5d. 2. Gain per cent. =\$25; Loss per cent. =\$20. 3. (1) 30502. (2) £56. (3) 67 yds., 4 in. 4. 118625. 5. $2 \times 2 \times 3 \times 3 \times 7 \times 7 \times 13$. 6. 34′. $27\frac{37}{37}$ ″ past 6 o'clock P. M.

PAPER III.

1. 6 2. (1) 10625; (2) 030416; (3) The first: (4) $\frac{7.9}{5.15}$. 3. 8520. 4. $37\frac{5}{9}$ square yards. 5. $13\frac{1}{13}$. 6. $\$22.37\frac{11}{32}$.

PAPER IV,

1. (1) $\frac{110}{2}$; $\frac{17}{85}$; (2) 123 times; $\frac{1}{3}$. 2. £139 15s. 3. (1) £20 9s. 6d.; (2) 52 $\frac{1}{5}$. 4. £82. 5. Turkey, 16s. 6d.; fowl, 2s. 10d. 6. $10\frac{59}{220}$.

PAPER V.

1. (1) 3011404; (2) 971472492; (3) 430709070; (4) 37834342650; (5) 75732561476. 2. 56c. 3. 8126. 4. \$288.09. 5. \$25.40. 6. 1 gal. 2 qts. 1 02 pts.

PAPER VI.

1. 706.85775 feet. 2. 641203200000000 cubic feet, 3. 8 ft. $1\frac{1}{8}$ in. 4. 82025. 5. 4, 8750; B, 8500; C. \$250. 6. 18 days.

PAPER VE.

1. (1) 7117423255950; (2) 6593445483924; (3) 68677245810; (4) 27798027851538; (5) 81697259850030. 2. 87.50; 87.52. 8. \$12.96. 4. 5000. 5. 8868.57; \$1709. 6. \frac{1}{3}.

PAPER VIII.

PAPER IX.

1. (1) 7832; (2) 196734; (3) 3589353148; (4) 3627452760. 2. 52800 yds 3. \$20 to B; \$10 to C. 4. \$600; \$900. 5. £2190. 6. \$3463.85.

PAPER X.

1. 825. 2. \$4.20. 3. 312\frac{15}{2}. 4. 604125.061// 5. \$200. 6. 130. 7. \$3000. 8. \$509.62\frac{1}{2}.

PAPER XI.

PAPER XII.

PAPER XIII.

PAPER XIV.

1. (1) 186798534370; (2) 2511248800235. 2. 200 lbs. 6 oz. 5 dwt. 3. 43 mls. 7 fur. 23 per. 3 yds. 1 in. 10 hrs. 50 min + . 4. 1133, 1339. 5. $\frac{18}{15}$ 6. $\frac{5}{5}$.

PAPER XV.

1. 5817600 inches. 2. 10 per cent. 3. $16\frac{1839}{20.8}$ \$27.8+. 5. $108\frac{2}{3}$. 6. \$7920.







2011: 33 1664 272 040 sq. in staile 240

19360



ZIEWENIARI

